Mechanical behaviour of gas-charged fine sediments: model formulation and calibration

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Multi-phase fluid conditions encountered in geotechnical and geo-environmental problems have led to the development of models that account for the influence of gas solubility and compressibility on the behaviour of soils of various grain sizes. Yet, no consideration has been given to damages related to the nucleation and growth of gas bubbles in fine-grained soils. The purpose of this paper is to present a Cam Clay based constitutive model extended to incorporate such detrimental effects on gassy soils. This is achieved by deriving an analytical expression relating the preconsolidation pressure to a damage parameter dependent on the gas content. That expression is coupled to a deviatoric yield surface accounting for inherent and stress-induced anisotropy. Comparisons of simulations and experimental results attest that introducing a single additional parameter to a conventional Cam Clay type model allows key behavioural features of gas-charged fine sediments to be reproduced.

KEYWORDS: compressibility; constitutive relations; offshore engineering; shear strength

INTRODUCTION

Free gases partially saturating underwater sediments are produced biogenically or thermogenically (Fleischer et al., 2001; Sills & Thomas, 2002). Direct observations in marine sediments have shown the gas phase to be discontinuous, forming discrete, isolated bubbles or voids within a continuous water phase (Sills et al., 1991; Anderson et al., 1998; Boudreau et al., 2005). Following Nageswaran (1983), the term 'gassy soil' is used to refer to this type of multi-fluid phase condition and sediment macrostructure. Sparks (1963) and subsequently Nageswaran (1983) argue that the critical water saturation level for the gas phase to be discontinuous is about 0.85. The presence of gas bubbles can have significant effects on the consolidation behaviour and strength properties. with gassy soils reacting differently compared to saturated soils to environmental changes in load and temperature (Esrig & Kirby, 1977; Sills & Wheeler, 1992; Grozic et al., 1999; Sills & Gonzalez, 2001; Amaratunga & Grozic, 2009; Puzrin et al., 2011; Rebata-Landa & Santamarina, 2012; Sultan et al., 2012). Accordingly, gas-charging has important consequences for slope stability assessment, waste management and in turn for the planning of on- and offshore engineering operations (Wheeler et al., 1991; van Kessel & van Kesteren, 2002; Tjelta et al., 2007; Mabrouk & Rowe, 2011).

In the following, the effect of free gas on the consolidation and strength properties of fine-grained soils and marine sediments is discussed. This serves as a basis to compare a number of constitutive models that have attempted to predict the behaviour of gassy soils. A new simple constitutive model is then presented to account for the effects of gas exsolution and expansion on the stress–strain response of soils.

ON THE BEHAVIOUR OF GASSY, FINE-GRAINED SOILS Structure of fine-grained, cohesive, gassy soils

Observational and theoretical results have pointed out that following gas exsolution (nucleation), bubble growth

Manuscript received 22 July 2013; revised manuscript accepted 30 September 2014. Published online ahead of print 11 November 2014. Discussion on this paper closes on 1 April 2015, for further details see p. ii.

(gas expansion) may mainly occur in fine-grained soils by compressing and fracturing the saturated matrix or by reopening pre-existing fractures (Boudreau (2012) and references therein). This can be reconciled with the arguments presented by van Kesteren & van Kessel (2002) concerning the dependence of bubble nucleation and growth on the tensile fracture toughness and undrained shear strength of the soil matrix. Therefore, the main process behind the de-saturation of fine-grained soils is rarely related to expulsion of water from capillary-type pores as described by Van Genuchten type models (van Genuchten, 1980), giving a unique relation between the degree of water saturation and the gas and water pressures.

Undrained unloading of gassy soils

The most detrimental effects of gas on marine soils are encountered during undrained unloading, as it may imply gas exsolution and expansion (Hardy & Hemstock, 1963). Because of these two processes, under undrained unloading conditions, changes in volume of gassy soils may occur, with pore pressure responses being dramatically different from those of saturated soils (Sobkowicz & Morgenstern, 1984). Sobkowicz & Morgenstern (1984) developed a detailed theoretical model based on a closed-form solution for undrained pore pressure responses to changes in total stress, by applying volume compatibility and considering gas expansion and exsolution.

Elastic properties

Experimental measurements on gassy, reconstituted, silty-clay samples presented by Wheeler & Gardner (1989) clearly showed that the undrained shear modulus, $G_{\rm u}$, and the undrained bulk modulus, $K_{\rm u}$, both decrease along with the degree of water saturation ($S_{\rm r}$). Sultan *et al.* (2012) noted that the presence of gas has a similar effect on the $G_{\rm u}$ of natural Gulf of Guinea (GoG) clay samples. Other results of triaxial tests reported by Wheeler *et al.* (1991) revealed that the normalised Young's modulus measured at an axial strain of 0·25% decreases with increasing the degree of gas saturation.

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Consolidation properties

Owing to the high compressibility of gas bubbles, the application of a load to a fine-grained gassy soil causes volume change even in undrained conditions (Thomas, 1987; Sills *et al.*, 1991). Oedometer results reported by Puzrin *et al.* (2011) confirm that the saturated clayey matrix and the gas make independent contributions to the overall gassy soil compressibility. Most importantly, the works of Thomas (1987) and Puzrin *et al.* (2011) both point out that, although the presence of a highly compressible gas phase results in enhanced immediate settlement, total consolidation values may be almost identical for specimens with or without gas. Accordingly, fine-grained gassy soils consolidate along the normal consolidation line (NCL) of their fully saturated equivalent.

Yield properties

Based on a series of constant rate of strain (CRS) oedometer tests on samples of Lierstranda and Bothkennar clays, Lunne *et al.* (2001) emphasised that the preconsolidation pressure (p_c') tends to decrease when the degree of gas saturation increases. Similar results from Hight *et al.* (2002) on Nile delta clay samples led Hight & Leroueil (2003) to ascribe the observed decreases in p_c' to bubble-growth-induced damages to the soil's structure. They proposed that the degree of damage depends on the initial level of structure. Sultan *et al.* (2012) furthered this view by defining a damage parameter d in the form

$$d = n(1 - S_{\rm r}) \tag{1}$$

where n is the porosity. Note that d is equivalent to the volume fraction of bubbles, f, used by Wheeler (1988a).

Experimental data presented in Fig. 1 were used by Sultan *et al.* (2012) to define a relation between $p_{\rm c}'$ of fine-grained gassy soils and d in the form

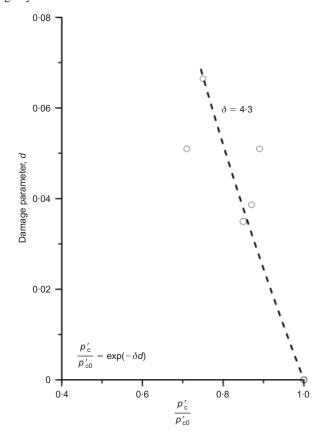


Fig. 1. Yield loci in the d (damage parameter)– p^\prime (mean effective stress) plane

$$\frac{p_{\rm c}'}{p_{\rm c0}'} = \exp\left(-\delta d\right) \tag{2}$$

where p'_{c0} is the preconsolidation pressure in the water-saturated condition and δ is a shape parameter found to be equal to 4·3 for GoG clays (Sultan *et al.*, 2012).

Strength properties

Wheeler (1988a) found that the undrained shear strength ($S_{\rm u}$) of reconstituted silty-clay samples may be increased or decreased by the presence of methane bubbles depending on the specific values of total and effective stresses. He concluded that the effects of gas bubbles on strength properties were most detrimental at low values of effective stress (corresponding to shallow depth below seabed) and high values of total stress (corresponding to deep water location). Wheeler (1988a) also noted that, while the degree of water saturation ($S_{\rm r}$) increased during undrained shearing, many gassy samples reached full saturation before failure but their structure remained permanently affected by the earlier presence of the bubbles.

In addition to these triaxial test results, those presented by Lunne *et al.* (2001), Hight *et al.* (2002) and Sultan *et al.* (2012) on natural clays all point out that the gas presence: (a) promotes a more contractive response and (b) significantly reduces the peak shear strength. These authors have also noted that gas may have the effect of producing a discontinuity in the effective stress path. According to Hight & Leroueil (2003), such a discontinuity (illustrated in Fig. 2) arises from a rapid increase in pore pressure, presumably resulting from the collapse of the pores enlarged (damaged) by gas exsolution and expansion.

In the following, the notion of 'enlarged pore' will be referred to as 'gas-formed void', in a similar sense to what Boudreau (2012) interchangeably calls crack, fracture or bubble. Additionally, the processes of gas exsolution and expansion will simply be referred to as 'bubble growth'.

With these specifications in mind, it is worth stressing that, while Lunne *et al.* (2001) presented results where the different stress paths join the same critical state line (CSL) after the gas-formed voids collapsed, GoG clays reach ultimate conditions on two different CSLs (Sultan *et al.*, 2012). In view of the results presented by Le *et al.* (2008), Sultan *et al.* (2012) and Hattab *et al.* (2013) on fully saturated specimens, this is inherent to the sensitivity of GoG clay and to structural damages upon pre-shear consolidation to high stress levels.

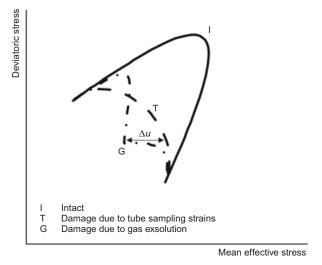


Fig. 2. Schematic effect of gas exsolution on effective stress path in triaxial compression (modified from Hight & Leroueil (2003))

MODELS ACCOUNTING FOR THE BEHAVIOUR OF FINE-GRAINED, GASSY SOILS

Based on the concept that, when soil particles are much smaller than gas-formed voids, the saturated matrix can be treated as a continuum, Wheeler (1988b) proposed the socalled 'large bubble model'. By analysing this continuum model Wheeler (1988a) derived theoretical expressions for the normalised undrained shear strength $S_u/S_{u,sat}$ (where $S_{u,sat}$ is the undrained shear strength in the fully saturated condition). In this approach, the saturated matrix was assumed to be a rigid-perfectly plastic von Mises type material containing empty spherical cavities. Wheeler (1988a) proposed that lower bound values of $S_u/S_{u,sat}$ can be estimated by ignoring the increase in strength caused by bubble flooding and the work-hardening effect caused by bubble shrinkage. He added that higher bound values may also be obtained by considering complete flooding of all the gas-formed voids. Various experimental results have been shown by Wheeler et al. (1991) to fit neatly within those theoretical bounds. However, Sultan et al. (2012) recently emphasised that the accuracy of the predictions from the Wheeler's approach tends to decrease inversely with the consolidation stress level achieved after bubble growth.

Pietruszczak & Pande (1996) and Grozic *et al.* (2005) proposed constitutive models to predict the response of gassy soils under undrained triaxial compression loading. Although these two models differ in complexity, they are both based on the critical state concept and on the idea that, because of its compressibility and solubility, gas only affects the volume change of a soil without damaging its structure. Both of these models predict that the higher the initial gas content, the less significant the total increase in pore pressure during shearing. This in turn leads to predictions that S_u should increase with increasing gas content.

A NEW CONSTITUTIVE MODEL FOR GASSY SOILS/SEDIMENTS

The present authors' proposed constitutive model is based on Cam Clay theory (Roscoe & Burland, 1968) with a few additions to account for the following key features of fine-grained, gassy soils' behaviour.

- Bubble growth due to undrained unloading simultaneously reduces the effective stress and the degree of pore water saturation.
- Damage due to bubble growth increases the compressibility and decreases the preconsolidation pressure, as well as the shear strength, of the initially saturated soil.
- The collapse of gas voids upon shearing may produce a discontinuity in the effective stress path.

The model is based on the uniqueness of the CSL, which is recognised as a limitation to reproduce accurately the behaviour of some sensitive clays, such as those from the GoG as previously discussed (see earlier section on 'Strength properties').

Model formulation

Isotropic stress states. The formulation is carried out in the specific volume (V)/mean effective stress (p') space based on what Alonso et al. (1990) formulated for unsaturated soils. In this V/p' space, the isotropic behaviour imposes a limiting condition to the formulation of the gassy soils model. Under undrained unloading conditions, the Sobkowicz & Morgenstern (1984) model allows calculation of the change in specific volume, $V_{\rm d}$, and mean effective stress, $p'_{\rm int}$, due to bubble growth (Fig. 3). Accordingly, the following identity may be established from Fig. 3

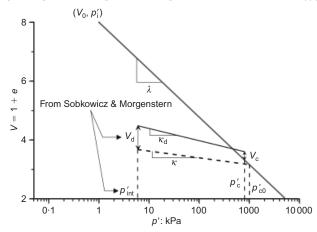


Fig. 3. Compression curve for damaged sediments after undrained unloading. The mean effective stress $p_{\rm int}'$ and the swelling $V_{\rm d}$ are generated after the undrained unloading path and are calculated from the Sobkowicz & Morgenstern (1984) model

$$V_{0} - \lambda \ln \frac{p'_{c0}}{p'_{0}} + \kappa \ln \frac{p'_{c0}}{p'_{int}} + V_{d} - \kappa_{d} \ln \frac{p'_{c}}{p'_{int}} - V_{c}$$

$$= V_{0} - \lambda \ln \frac{p'_{c}}{p'_{0}}$$
(3)

The Cam Clay parameters κ and λ are, respectively, the intact swelling coefficient and the compression index. p_c' is given by equation (2) and κ_d is a damaged swelling coefficient accounting for the effect of bubble growth. The quantity V_c is seen as a collapse required to reach the NCL. It can be calculated from

$$V_{c} = \ln \left(\frac{p'_{c0}}{p'_{int}} \right) (\kappa - \kappa_{d}) + V_{d} + \delta d(\kappa_{d} - \lambda)$$
 (4)

Given the lack of detailed experimental investigations concerning κ_d , two limit cases can be considered following undrained unloading and consequent bubble growth, as described below.

Case 1: κ_d increases and the compression curve reaches the NCL at the yield locus (Puzrin *et al.*, 2011) defined by equation (2). In this case, V_c is equal to 0 and, according to equations (2) and (4), κ_d can be calculated as follows

$$\kappa_{\rm d} = \frac{-\kappa \ln (p'_{\rm c0}/p'_{\rm int}) - V_{\rm d} + \lambda \delta d}{-\ln (p'_{\rm c0}/p'_{\rm int}) + \delta d}$$
 (5)

Case 2: $\kappa_{\rm d}$ remains constant ($\kappa=\kappa_{\rm d}$) and a collapse $V_{\rm c}$ takes place at the yield locus defined by equation (2). The compression curve reaches the NCL after the collapse of gas-formed voids. The collapse can be calculated from equation (4) with κ equal to $\kappa_{\rm d}$.

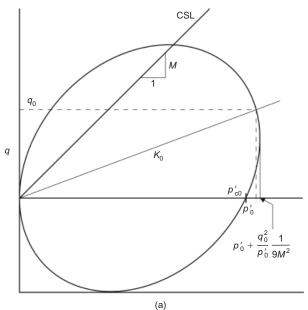
Triaxial stress states. On extending the model to triaxial states of stress and strain, the deviatoric stress q is introduced. The model adopted to simulate the saturated (limit) condition is that developed by Banerjee et al. (1985) to account for inherent and stress-induced anisotropy of natural clays. It is based on the modified Cam Clay model where, in addition to the isotropic hardening law, a further stress tensor is introduced in the yield curve expression. Under axisymmetric loading (radial stresses are equal – condition of triaxial test), the Banerjee et al. (1985) yield curve is given by the following equation

$$q = \frac{2}{3}p'\frac{q_0}{p'_0} \pm \sqrt{M^2(p'p'_0 - p'^2) + \frac{1}{9}\frac{p'}{p'_0}q_0^2}$$
 (6)

where q and p' are respectively the deviatoric and mean effective stress invariants, M is the slope of the CSL, and q_0 and p'_0 are the projection of the additional stress tensor in the q-p' space (Fig. 4(a)). q_0 is related to p'_0 through the following equation

$$q_0 = -3p_0' \frac{K_0 - 1}{2K_0 + 1} \tag{7}$$

where K_0 is the coefficient of earth pressure at rest; and q_0 and p'_0 are the maximum stresses to which a saturated soil has previously been loaded. For a soil with a purely isotropic stress history (q_0 equals zero), the yield curve of the Banerjee *et al.* model is similar to that of the modified Cam Clay model.



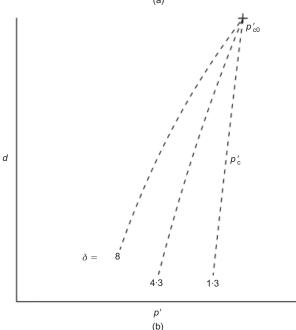


Fig. 4. (a) Yield curve in the deviatoric stress—mean effective stress diagram (from Banerjee *et al.* (1985)); and (b) yield locus in the d/p' diagram. The damaged isotropic preconsolidation pressure (p'_c) decreases with the increase of the δ parameter

The use of the Banerjee *et al.* (1985) yield curve, as presented in Fig. 4, is justified by the initial anisotropy of most natural sediments. The isotropic preconsolidation pressure p'_c of the damaged gassy sediment can be calculated from p'_0 according to the following equation

$$\frac{p_{\rm c}'}{p_0'} = \frac{M^2 \exp\left(-\delta d\right)^2 (4K_0^2 + 4K_0 + 1) + (K_0 - 1)^2}{\exp\left(-\delta d\right) \left[(2K_0 - 2)^2 + M^2 (2K_0^2 + 1)^2\right]}$$
(8)

The isotropic preconsolidation pressure p'_{c0} of the saturated sediment is given by the following equation

$$\frac{p'_{c0}}{p'_0} = \frac{4M^2K_0(K_0+1) + M^2 + K_0^2 - 2K_0 + 1}{4(K_0^2 + 1 + M^2 - 4K_0 + M^2K_0^2 + M^2K_0)}$$
(9)

Hardening law, consistency conditions and flow rule

Similarly to the modified Cam Clay model, the hardening law here adopted is isotropic. It gives dp_c' as a function of the volumetric plastic strain increment $d\epsilon_v^p$ according to the following equation

$$dp'_{c0} = \frac{1 + e_0}{\lambda - \kappa} p'_{c0} d\varepsilon_v^p$$
 (10)

The shrinkage of the yield curve is also induced by bubble growth. As previously discussed, it leads to a decrease of $p_{\rm c}'$ and therefore to a decrease of p_0' and q_0 .

The increment of plastic volumetric strain de_{ν}^{p} can be calculated by applying the consistency condition, defined by $dF_{1} = 0$ if

$$\frac{q}{p'} > \frac{q \left(p'_0 + \frac{q_0^2}{p'_0} \frac{1}{9M^2}\right)}{p'_0 + \frac{q_0^2}{p'_0} \frac{1}{9M^2}}$$

and $dF_2 = 0$ if

$$\frac{q}{p'} < \frac{q\left(p'_0 + \frac{q_0^2}{p'_0} \frac{1}{9M^2}\right)}{p'_0 + \frac{q_0^2}{p'_0} \frac{1}{9M^2}}$$

where

$$F_1 = q - \frac{2}{3}p'\frac{q_0}{p'_0} - \sqrt{M^2(p'p'_0 - p'^2) + \frac{1}{9}\frac{p'}{p'_0}q_0^2}$$
 (11)

and

$$F_2 = q - \frac{2}{3}p'\frac{q_0}{p'_0} + \sqrt{M^2(p'p'_0 - p'^2) + \frac{1}{9}\frac{p'}{p'_0}q_0^2}$$
 (12)

The two consistency conditions $dF_1 = 0$ and $dF_2 = 0$ are given by the following equation

$$dF_{1-2} = \left(\frac{\partial F_{1-2}}{\partial p'}\right) dp' + \left(\frac{\partial F_{1-2}}{\partial q}\right) dq + \left(\frac{\partial F_{1-2}}{\partial d}\right) dd + \left(\frac{\partial F_{1-2}}{\partial p'_0} \cdot \frac{\partial p'_0}{\partial p'_{c0}}\right) dp'_{c0}$$
(13)

where $\partial p_0'/\partial p_{c0}'$ can be determined from equation (2).

The partial differential terms in equation (13) are given in Table 1 and Table 2. Therefore $d\varepsilon_v^p$ can be calculated by combining equations (10) and (13).

In most constitutive models for saturated soils, the plastic

Table 1. Differential terms associated with F_1 used in equation (13)

$$\frac{\partial}{\partial \downarrow} \qquad F_{1} \\
p' \qquad \frac{2(K_{0}-1)}{2K_{0}+1} - \frac{0.5}{\sqrt{M^{2}[p'p'_{0}\exp(-\delta d) - p'^{2}] + p'\frac{p'_{0}}{\exp(-\delta d)}\frac{(K_{0}-1)^{2}}{(2K_{0}+1)^{2}}}} \left\{ M^{2}[p'_{0}\exp(-\delta d) - 2p'] + \frac{p'_{0}}{\exp(-\delta d)}\frac{(K_{0}-1)^{2}}{(2K_{0}+1)^{2}} \right\}$$

$$q \qquad 1$$

$$\frac{-0.5}{\sqrt{M^{2}[p'p'_{0}\exp(-\delta d) - p'^{2}] + p'\frac{p'_{0}}{\exp(-\delta d)}\frac{(K_{0}-1)^{2}}{(2K_{0}+1)^{2}}}} \left[M^{2}p'\exp(-\delta d) + \frac{p'}{\exp(-\delta d)}\frac{(K_{0}-1)^{2}}{(2K_{0}+1)^{2}} \right]$$

$$d \qquad \frac{-0.5}{\sqrt{M^{2}[p'p'_{0}\exp(-\delta d) - p'^{2}] + p'\frac{p'_{0}}{\exp(-\delta d)}\frac{(K_{0}-1)^{2}}{(2K_{0}+1)^{2}}}} \left[-M^{2}p'p'_{0}\delta\exp(-\delta d) + \frac{p'p'_{0}}{\exp(-\delta d)}\frac{(K_{0}-1)^{2}}{(2K_{0}+1)^{2}}\delta \right]$$

Table 2. Differential terms associated with F_2 used in equation (13)

potential only depends on the stress inclination q/p' (Roscoe & Burland, 1968; Wong & Mitchell, 1975; Nova & Wood, 1979). For this reason, the flow rule can be investigated by plotting the direction of the plastic strain ratio $d\varepsilon_{\rm p}^{\rm p}/d\varepsilon_{\rm s}^{\rm p}$ as a function of the stress ratio q/p'. Here, the following expression proposed by Lagioia *et al.* (1996) is used

$$\frac{\mathrm{d}\varepsilon_{\mathrm{v}}^{\mathrm{p}}}{\mathrm{d}\varepsilon_{\mathrm{s}}^{\mathrm{p}}} = \mu \left(M_{\mathrm{c}} - \frac{q}{p'} \right) \left(\frac{\alpha M_{\mathrm{c}}}{q/p'} + 1 \right) \tag{14}$$

where M_c corresponds to the value of q/p' at which $d\epsilon_v^p/d\epsilon_s^p$ is equal to 0.

Parameters of the model and their determination

In total, ten parameters (κ , κ_d , G, λ , M, μ , α , M_c , δ , K_0) are introduced in the proposed model.

They can be determined as follows.

- (a) κ , G, λ , M are common Cam Clay parameters, which can be determined in a common fashion.
- (b) κ_d can be determined from isotropic compression tests after gas exsolution. Alternatively, κ_d can be taken equal to κ or derived from equation (5) for the two limit cases presented in the earlier subsection on 'Isotropic stress states'.

- (c) μ , α and M_c , which define the flow rule, are calculated by using the $d\varepsilon_v^p/d\varepsilon_s^p-q/p'$ curve obtained from a drained triaxial test on a fully saturated sample.
- (d) δ , which governs the shape of the yield locus in the p'-d space, can be derived from at least two isotropic compression tests at two different damage levels (or two different initial S_r values).
- (e) For the yield curve the K₀ parameter corresponds to the coefficient of earth pressure at rest.

The determination of the degree of water saturation, undrained volume change and pore water pressure due to the gas compressibility and solubility are calculated using the Sobkowicz and Morgenstern model, which requires input soil and water compressibilities, as well as the Henry's coefficient.

Model performance

The aim of this section is to show the capability of the model to simulate different drained and undrained stress paths. The following set of model parameters is used for the different simulations

- (a) flow rule: $\mu = 1.2$, $\alpha = 0.001$, $M_c = 1.75$
- (b) yield locus in the d/p' plane: $\delta = 4.2$

(c) Banerjee yield curve: $K_0 = 0.6$.

The gas saturating the medium is carbon dioxide, which has Henry's coefficient of solubility equal to 0.86.

In addition, the void ratio at 1 kPa (e_0) was taken as equal to 5·1, while the initial total stress was taken as equal to 10 MPa with a p'_{c0} equal to 0·1 MPa.

Case 1: Drained isotropic loading. Four samples are unloaded, undrained, from 10 MPa to four different lower effective stresses. Upon undrained unloading the initially normally consolidated samples become overconsolidated (Fig. 5). The four samples are characterised by four different effective stresses, void ratios and degrees of water saturation before compression (Fig. 5). In Fig. 5, the four compression curves follow different damaged swelling coefficients κ_d to converge towards the NCL at four different mean effective stresses p'.

In Fig. 6, the four compression curves follow the same swelling coefficients κ before converging towards the NCL after a volumetric collapse V_c proportional to the initial S_r at four different mean effective stresses p'. Fig. 5 and Fig. 6 illustrate the way the two different possibilities concerning κ_d ($V_c = 0$ or $\kappa_d = \kappa$) can be considered in the proposed model.

Case 2: Drained triaxial tests at different initial degrees of water saturation $- V_c = 0$. The three stress paths considered

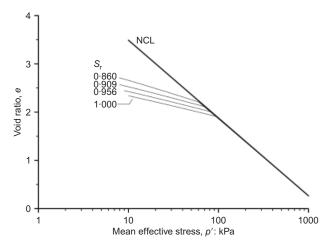


Fig. 5. Undrained unloading followed by isotropic drained loading with $V_c = 0$. Void ratio-mean effective stress relationships

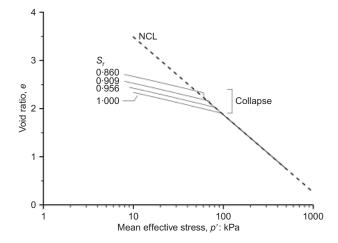


Fig. 6. Undrained unloading followed by isotropic drained loading with $\kappa_{\rm d} = \kappa$. Void ratio-mean effective stress relationships

for this case are presented in Fig. 7(a). Two of the three samples are first unloaded, undrained, to cause bubble growth. Following the consequent decreases in p' and $S_{\rm r}$, the two gassy samples as well as the saturated one are submitted to a drained triaxial stress path with a typical dq/dp'=3. Fig. 7(b) shows that the peak shear strength of overconsolidated sediments depends strongly on the size of the yield curve and increases with $S_{\rm r}$. The increase of $\kappa_{\rm d}$ due to bubble growth is illustrated in Figs 7(c) and 7(d) as causing increased compressibility.

Case 3: Undrained triaxial tests at different initial degrees of water saturation $-\kappa_d = \kappa$. The four stress paths of this case are presented in Fig. 8(a) where three of the four samples are unloaded, undrained, before shearing. Fig. 8(a) also shows the yield curve of the saturated sediment (dashed curve). Using $\kappa_d = \kappa$ in the calculation allows simulation of the experimentally observed discontinuities in the stress paths. Each discontinuity corresponding to a sudden increase in pore pressure depends on the damage level d. The second important observation that can be drawn from Fig. 8(a) is that the slope of the stress path in the plastic domain changes once S_r becomes equal to 1 (this can be seen on only one stress path, second from the right, presented in Fig. 8(a)).

The simulation results in terms of deviatoric stress/shear strain are presented in Fig. 8(b) where the maximum deviatoric stress increases with $S_{\rm r}$. The simulation results are also presented in terms of volumetric strain/mean effective stress (Fig. 8(c) and volumetric strain/deviatoric strain diagram (Fig. 8(d)) to show that the sediment becomes incompressible when $S_{\rm r}$ reaches 1 (Figs 8(c) and 8(d)).

Case 4: Undrained triaxial tests at different initial degrees of water saturation – $V_c = 0$. The four stress paths followed for this case calculation are presented in Fig. 9(a). As previously, three of the four samples were unloaded, undrained, before shearing. Fig. 9(a) also presents the yield curves of the four samples (dashed curves). By contrast with the saturated sample, the three gassy ones follow inclined stress paths in the elastic domain. The use of $V_c = 0$ in the simulation prevents the sudden increase in pore pressure during shearing and therefore the discontinuity in the stress paths. Once again, the change in slope of the stress path in the plastic domain (for the second test from the right) corresponds to the limit where S_r becomes equal to 1 (Fig. 9(a)). The simulation results in terms of deviatoric stress/shear strain are presented in Fig. 9(b) where the maximum deviatoric stress increases with $S_{\rm r}$. The simulation results are also presented in terms of volumetric strain/mean effective stress (Fig. 9(c)) and volumetric strain/deviatoric strain diagrams (Fig. 9(d)).

The Wheeler (1988a) model compared to the proposed one

Although the model by Wheeler (1988a) is not adapted to predict $S_{\rm u}$ values when sediments follow complex stress paths before shearing, it was shown to correctly predict $S_{\rm u}$ when shearing occurs immediately after bubble growth (Sultan *et al.*, 2012). In order to compare and analyse the two models' sensitivity to their respective input parameters, 28 numerical simulations were carried out by considering stress paths where sediments are directly sheared after bubble growth. The response of sediments of varying properties to different initial total and effective stresses were thus tested (Table 3).

Figure 10 presents five examples (first five in Table 3) of numerical simulations of isotropically consolidated, undrained (CIU) tests at different initial S_r in a deviatoric

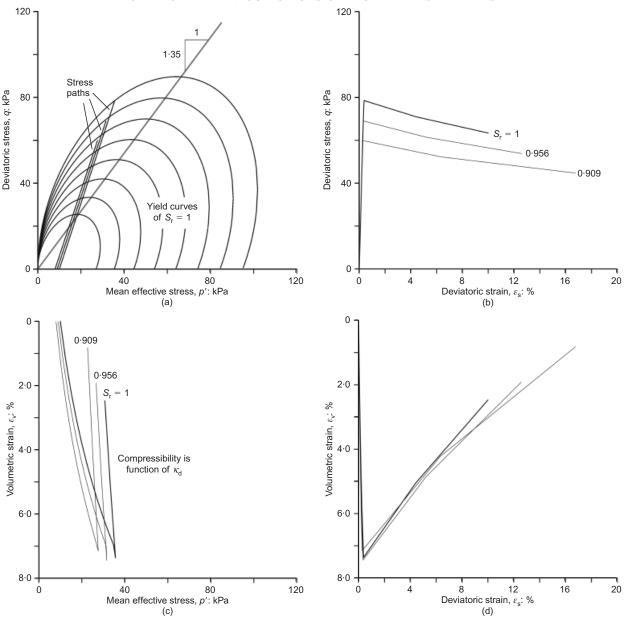


Fig. 7. Numerical simulations of three drained triaxial tests at three different initial degrees of water saturation plotted on: (a) deviatoric stress—mean effective stress diagram; (b) deviatoric stress—deviatoric strain diagram; (c) volumetric strain—mean effective stress diagram; and (d) volumetric strain—deviatoric strain diagram. The three samples are highly overconsolidated (OCR > 2)

stress/mean effective stress diagram where $S_{\rm u}$ is calculated from the deviatoric stress at yield $q_{\rm y}$ ($S_{\rm u}=q_{\rm y}/2$). Three key features are noticeable in this figure: the stress path inclination in the elastic domain, the discontinuity in the stress path and the excess pore pressures build-up during plastic shearing when the sediments become water fully saturated ($S_{\rm r}=1$).

Simulation results in Fig. 11(a) present the theoretical lower bounds of $S_{\rm u}$ using the model by Wheeler (1988a) and show $S_{\rm u}$ to be more sensitive to d for high values of $p'_{\rm c0}/S_{\rm u,sat}$. The 28 numerical simulations detailed in Table 3 are presented in Fig. 11(b) in terms of $S_{\rm u}/S_{\rm u,sat}$ as a function of d. The $S_{\rm u}/S_{\rm u,sat}$ values obtained with the present model are much less sensitive to the value of $p'_{\rm c0}/S_{\rm u,sat}$ when compared to the Wheeler's model. However, $S_{\rm u}/S_{\rm u,sat}$ depends strongly on the δ parameter so that, for similar values of $p'_{\rm c0}/S_{\rm u,sat}$ and d, $S_{\rm u}/S_{\rm u,sat}$ decreases strongly with increasing δ . Another important observation can be drawn from Fig. 11(b) where, for the same $p'_{\rm c0}/S_{\rm u,sat}$ and the same δ ,

 $S_{\rm u}/S_{\rm u,sat}$ decreases significantly with the increase of the κ values. This last observation was expected, since the stress path in a Cam Clay type model depends strongly on κ and λ . The comparison between five series of model predictions shows that the Wheeler's model generally overestimates the degradation in $S_{\rm u}$ for a given damage parameter d. This is also an expected result since the curves shown in Fig. 11 are predicted from the lower bound expression of $S_{\rm u}/S_{\rm u,sat}$ proposed by Wheeler (1988a).

Comparison of model simulations with experimental results Tests on Nile delta clay. Hight et al. (2002) presented results of CIU tests on Nile delta clay in which gas exsolution and expansion resulted from stress relief inherent to core sample recovery: two samples, BH10 and BH6A, come from 32·35 m and 45·0 m depth, respectively. Before shearing, the two samples were isotropically consolidated to their in-situ stress conditions. Hight et al. (2002) have not reported any in-situ

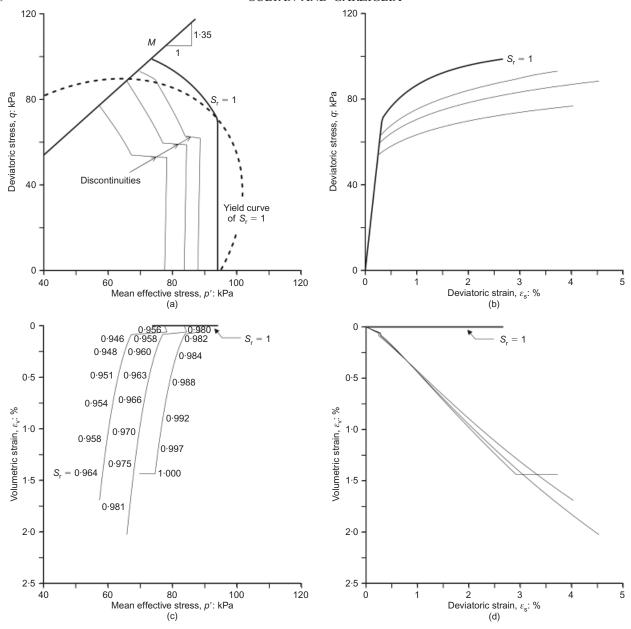


Fig. 8. Numerical simulations of four undrained triaxial tests at four different initial degrees of water saturation plotted on: (a) deviatoric stress—mean effective stress diagram; (b) deviatoric stress—deviatoric strain diagram; (c) volumetric strain—mean effective stress diagram (the plotted values correspond to S_r); and (d) volumetric strain—deviatoric strain diagram. The four samples are normally consolidated or slightly overconsolidated (OCR < 2)

values of S_r , but estimated that just before shearing, the samples had S_r ranging from 0.85 and 0.95.

The isotropic stress paths applied in the numerical simulations before shearing were chosen in order to fit with (a) the initial mean effective stress and (b) the elastic limits that can be easily defined from the changes in slope of the effective stress paths. Although this implies that simulations have no predictive significance, comparison of modelling results with experimental data provides insight into the four phases characterising the stress path of Nile delta clay gassy samples, as shown in Fig. 12.

- (a) Phase 1: shearing induces slight changes in mean effective stress in the elastic region (due to gas compressibility). This initial phase is well described by the modelling results.
- (b) Phase 2: the collapse of gas-formed voids at yielding induces an important progressive increase in pore pressure under a negligible increase in shear stress. Increases in

- pore pressure are a function of the initial gas-formed voids or $S_{\rm r}$. This second phase is well described by the proposed model but the pore pressure increase is simulated as a sudden process rather than a progressive one.
- (c) Phase 3: the compression and dissolution of remaining gas bubbles cause a progressive increase in S_r along with a decrease in compressibility (or increase in pore pressure).
- (d) Phase 4: after the complete collapse and disappearance of the gas bubbles, the sediment behaves as a saturated one, with an important increase in pore pressure during shearing.

Tests on Lierstranda clay. By conducting a series of anisotropically consolidated undrained compression (CAUc) tests on Lierstranda clay with various initial amounts of gas dissolved in the pore water (Fig. 13(a)), Lunne et al. (2001) evaluated the detrimental effects of stress relief due to deepwater sampling. In the Lunne et al. (2001) tests, the amount of gas initially dissolved in the water (η) was adjusted in the

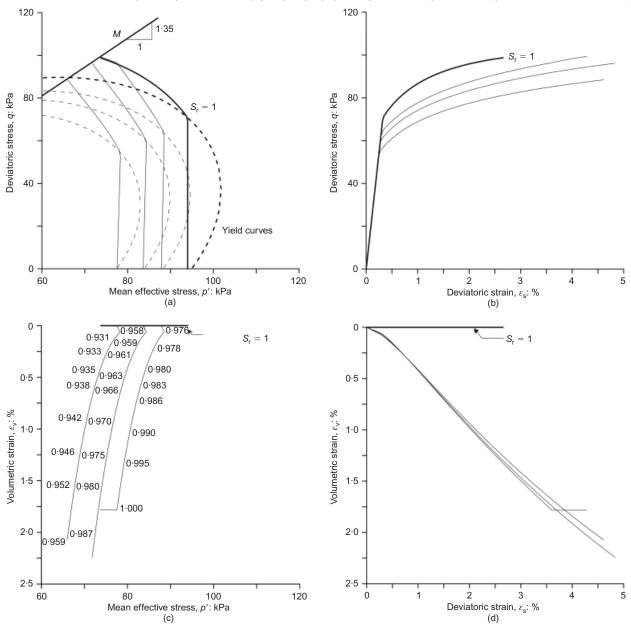


Fig. 9. Numerical simulations of four undrained triaxial tests at four different initial degrees of water saturation plotted on: (a) deviatoric stress—mean effective stress diagram; (b) deviatoric stress—deviatoric strain diagram; (c) volumetric strain—mean effective stress diagram (the plotted values correspond to S_r); and (d) volumetric strain—deviatoric strain diagram. The four samples are normally consolidated or slightly overconsolidated (OCR < 2)

laboratory before the samples were unloaded, undrained, and then sheared, but the change in $S_{\rm r}$ due to gas exsolution was not measured. Modelling results presented in Fig. 13(b) show the four phases listed in the previous subsection for the Hight *et al.* (2002) tests, going from elastic shearing to the complete collapse of gas bubbles.

Figure 14 illustrates the ability of the model to fit the experimental stress–strain curves and the decrease in peak deviatoric stress with $S_{\rm r}$. However, it is important to mention that predicting the post-peak softening presented in Fig. 13(a) and Fig. 14(a) is beyond the capability of the present model. Indeed, the softening of a slightly overconsolidated (OCR < 2) or normally consolidated sediment cannot be simulated without accounting for initial strength sensitivity and/or subsequent degradation of the structure during shearing.

Tests on GoG plastic clay. Sultan et al. (2012) reported results of CIU tests on natural GoG clay samples made gassy

by undrained unloading after saturation with carbonated water. The minimum S_r measured before shearing the samples A, B, C and D (in Fig. 15(a)) were respectively equal to 0.95, 0.93, 0.91 and 0.91. Tests results revealed that damages due to bubble growth have affected the compressibility, preconsolidation pressure and peak shear strength of those structured sediments (Sultan et al., 2012). Bubble growth might have also contributed to the change in CSL as illustrated in Fig. 15(a). Nevertheless, one cannot ignore that this change has been shown (Le et al., 2008) to be also related to destructuration by isotropic compression before shearing. The GoG plastic clays (plasticity index between 90 and 120) are composed of small-sized elementary clay particles (a few micrometres) assembled in much larger aggregates. The high effective friction angles (exceeding 40°) characterising the GoG natural clays (see, for instance, Le et al. (2008)) may be explained by their microstructure but also by a sand-like behaviour of the clay aggregates.

Therefore, simulating the four tests presented in Fig. 15(a)

Table 3. Summary of 28 numerical simulations carried out for different initial test conditions

q_{y}	S_{u}	$S_{\rm r}$	n	d	$S_{\rm u}/S_{\rm u,sat}$	M	δ	Δσ	$\sigma_{ m ini}$	K_0	λ	κ	$p'_{\rm c0}/S_{\rm u,sat}$
53.300	26.650	1.000	0.730	0.000	1.000	1	4.3	0	10000	1	0.5	0.05	3.732
50.530	25.265	0.992	0.731	0.006	0.948	1	4.3	-100	10000	1	0.5	0.05	3.732
43.366	21.683	0.957	0.738	0.032	0.814	1	4.3	-500	10000	1	0.5	0.05	3.732
32.350	16.175	0.912	0.747	0.066	0.607	1	4.3	-1000	10000	1	0.5	0.05	3.732
28.480	14.240	0.893	0.751	0.080	0.534	1	4.3	-1200	10000	1	0.5	0.05	3.732
72.200	36.100	1.000	0.730	0.000	1.000	1.35	4.3	0	10000	1	0.5	0.05	2.765
68.700	34.350	0.992	0.731	0.006	0.952	1.35	4.3	-100	10000	1	0.5	0.05	2.765
58.220	29.110	0.957	0.738	0.032	0.806	1.35	4.3	-500	10000	1	0.5	0.05	2.765
44.240	22.120	0.912	0.747	0.066	0.613	1.35	4.3	-1000	10000	1	0.5	0.05	2.765
39.300	19.650	0.893	0.751	0.080	0.544	1.35	4.3	-1200	10000	1	0.5	0.05	2.765
26.400	13.200	1.000	0.730	0.000	1.000	0.5	4.3	0	10000	1	0.5	0.05	7.464
25.180	12.590	0.992	0.731	0.006	0.954	0.5	4.3	-100	10000	1	0.5	0.05	7.464
21.300	10.650	0.957	0.738	0.032	0.807	0.5	4.3	-500	10000	1	0.5	0.05	7.464
15.780	7.890	0.912	0.747	0.066	0.598	0.5	4.3	-1000	10000	1	0.5	0.05	7.464
13.930	6.965	0.893	0.751	0.080	0.528	0.5	4.3	-1200	10000	1	0.5	0.05	7.464
26.400	13.200	1.000	0.730	0.000	1.000	0.5	2.15	0	10000	1	0.5	0.05	7.464
25.200	12.600	0.992	0.731	0.006	0.955	0.5	2.15	-100	10000	1	0.5	0.05	7.464
22.280	11.140	0.957	0.738	0.032	0.844	0.5	2.15	-500	10000	1	0.5	0.05	7.464
19.360	9.680	0.912	0.747	0.066	0.733	0.5	2.15	-1000	10000	1	0.5	0.05	7.464
26.480	13.240	1.000	0.730	0.000	1.000	0.5	5	0	10000	1	0.5	0.05	7.464
25.180	12.590	0.992	0.731	0.006	0.951	0.5	5	-100	10000	1	0.5	0.05	7.464
21.080	10.540	0.957	0.738	0.032	0.796	0.5	5	-500	10000	1	0.5	0.05	7.464
14.520	7.260	0.912	0.747	0.066	0.548	0.5	5	-1000	10000	1	0.5	0.05	7.464
12.360	6.180	0.893	0.751	0.080	0.467	0.5	5	-1200	10000	1	0.5	0.05	7.464
70.020	35.010	1.000	0.759	0.000	1.000	1	4.3	0	10000	1	0.4	0.2	2.828
68.260	34.130	0.992	0.761	0.006	0.975	1	4.3	-100	10000	1	0.4	0.2	2.828
54.460	27.230	0.958	0.767	0.032	0.778	1	4.3	-500	10000	1	0.4	0.2	2.828
32.080	16.040	0.913	0.776	0.067	0.458	1	4.3	-1000	10000	1	0.4	0.2	2.828

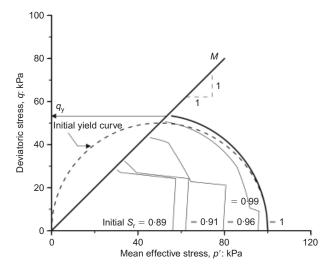


Fig. 10. Example of numerical simulations of five undrained triaxial tests at different initial degrees of water saturation plotted on deviatoric stress—mean effective stress diagram (first five in Table 3). The undrained shear strength $S_{\rm u}$ is calculated from $q_{\rm y}$ ($S_{\rm u}=q_{\rm y}/2$)

with the Cam Clay type model presented in this paper is only possible by considering two different values of M: equal to 0.8 for tests D and A; and equal to 0.65 for tests B and C. The use of two different M values, for the same initial sediment, suggests the presence of two different critical states.

Other parameters used for the simulation of CIU tests were derived from Sultan *et al.* (2012) and are as follows

- (a) compressibility: $\lambda=1.0$, $\kappa=0.1$ and $\kappa_{\rm d}$ calculated from equation (5) ($V_{\rm c}=0$).
- (b) flow rule: $\mu = 1.2$, $\alpha = 0.45$, $M_c = 1.75$

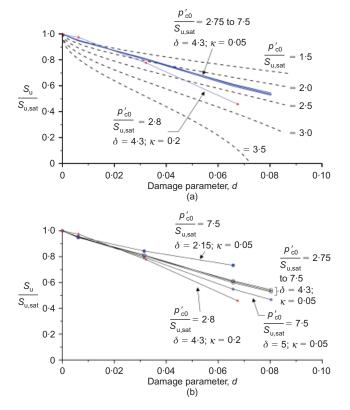


Fig. 11. (a) Prediction of $S_{\rm u}/S_{\rm u,sat}$ as a function of d using the lower bound model by Wheeler (1988a) (dashed lines) and the present developed model. (b) $S_{\rm u}/S_{\rm u,sat}$ as a function of d for the test conditions presented in Table 3

- (c) yield locus in the d/p' plane: $\delta = 4.2$
- (d) yield surface: $K_0 = 1.0$ and therefore q_0 in equation (7) is equal to 0
- (e) void ratio at 1 kPa $(e_0) = 7.7$.

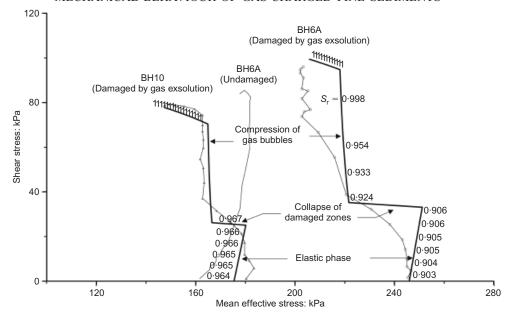


Fig. 12. Results of CIU triaxial tests on Nile delta clay (Hight *et al.*, 2002) in terms of effective stress paths. Bold curves correspond to numerical simulation results (the plotted values correspond to S_r)

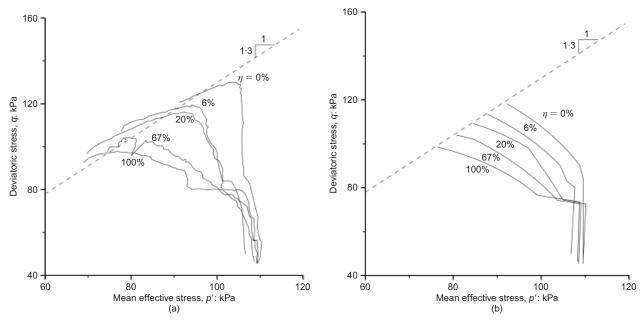


Fig. 13. Results of CAUc triaxial tests on Lierstranda clay with different degrees of dissolved gas, η (Lunne *et al.*, 2001). Effective stress paths: (a) experimental results; (b) modelling. Stress paths and Henry's coefficient before shearing were adjusted to fit with experimental data

The simulation results in Fig. 15(b) show the two last phases (phases 3 and 4 in the earlier subsection 'Tests on Nile delta clay') previously mentioned for the Hight *et al.* (2002) tests.

Simulations in Fig. 15(b) reproduce the observed peak strengths and effective stresses for the four tests (Fig. 15(a)). The use of $V_c = 0$ in the simulation of the GoG clays prevents the advent of discontinuities in the stress path as observed by Lunne *et al.* (2001) and Hight *et al.* (2002).

CONCLUSIONS

A Cam Clay based constitutive model was extended to reproduce features of fine-grained gassy sediments' behaviour not previously captured by existing models. In the light of experimental results, an analytical expression was derived to relate the preconsolidation pressure to a damage param-

eter inherent to the growth of gas bubbles. This expression was coupled to an anisotropic yield surface with the addition of a damaged swelling coefficient. The model outlined in this paper was able to fairly reproduce published results of triaxial tests under different loading conditions. Accordingly, the following features of behaviour observed experimentally were reproduced.

- (a) Upon undrained unloading, bubble growth causes important decreases in effective stress and degree of water saturation.
- (b) By reducing the preconsolidation pressure, damage due to bubble growth induces the contraction of the yield surface.
- (c) The onset of yielding may be marked by the collapse of

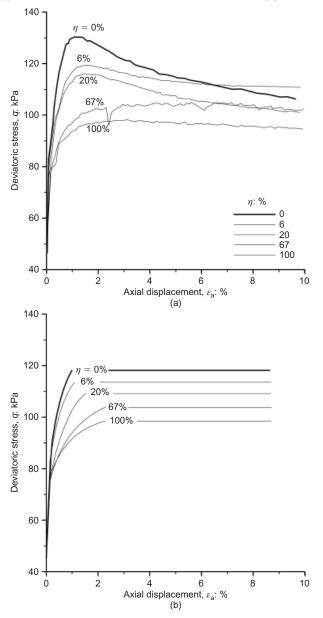


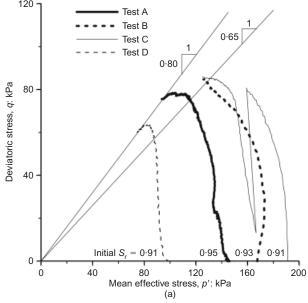
Fig. 14. Results of CAUc triaxial tests on Lierstranda clay with different degrees of dissolved gas (Lunne *et al.*, 2001). Stressstrain curves: (a) experimental results; (b) modelling

gas-formed voids and an associated significant and sudden increase in pore pressure.

- (d) Owing to the compressibility and solubility of gas, the degree of water saturation increases upon shearing so that fully saturated conditions may be reached before failure.
- (e) By contracting the size of the yield surface and therefore the pore pressure response, damage due to the growth of gas bubbles implies that fine-grained, gassy sediments reach ultimate conditions at lower shear stresses than their fully saturated equivalent.

ACKNOWLEDGEMENTS

The authors are thankful for fruitful discussions with Alain Puech. Funding support from the French CITEPH programme (http://gep-france.com/citeph/) is also greatly appreciated. A part of the research leading to these results has received funding from the European Union Seventh Framework Programme (FP7/2007–2013) under the MIDAS project, grant agreement no. 603418.



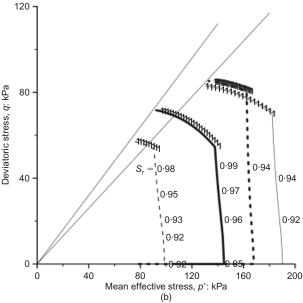


Fig. 15. Results of triaxial tests on gassy GoG clays with different initial degrees of water saturation (Sultan *et al.*, 2012). Effective stress paths: (a) experimental results; (b) modelling. The sudden decrease observed in the C curve corresponds to an accidental unloading during shearing. Henry's coefficients were adjusted to fit with the observed initial S_r shown in (a)

NOTATION

d damage parameter

 $d\varepsilon_s^p$ deviatoric plastic strain increment

 $d\varepsilon_{v}^{s}$ volumetric plastic strain increment

e void ratio

e₀ initial void ratio

 $\overset{\circ}{G}$ shear modulus

 G_{u} undrained shear modulus

K bulk modulus

 $K_{\rm u}$ undrained bulk modulus

 K_0 coefficient of earth pressure at rest

M critical stress ratio

 $M_{\rm c}$ flow rule parameter at which plastic strain ratio is equal to 0

n porosity

p' mean effective stress

 p_0' maximum mean effective stress supported by sediment

 p_c' preconsolidation pressure

 p'_{c0} preconsolidation pressure of water-saturated soils

 p'_{int} effective stress after undrained unloading

- q deviatoric stress
- maximum deviatoric stress supported by sediment
- $q_{\rm v}$ deviatoric stress at yield
- $S_{\rm r}$ degree of water saturation
- Su undrained shear strength
- V specific volume
- $V_{\rm c}$ collapse in terms of specific volume at yield
- V_d swelling in terms of specific volume after undrained unloading
- α first flow rule parameter
- δ shape parameter relating preconsolidation pressure to damage parameter
- ε_a axial strain
- $\varepsilon_{\rm s}$ deviatoric strain
- $\varepsilon_{\rm v}$ volumetric strain
- n degree of dissolved gas
- κ swelling coefficient
- κ_d damaged swelling coefficient
- λ compression index

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