Numerical and experimental characterisation of interactions between two marine current turbines

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Abstract:
The implantation and deployment of marine current turbine arrays depend on the understanding of their interactions. Based on \textit{a priori} suggestions about the layout of marine energy converter arrays, we propose to highlight interactions effects between two horizontal axis marine current turbines, in open water.

Experimental trials were run in IFREMER’s wave and current flume tank in Boulogne-sur-Mer (France), on marine current turbine models. Our study focuses on setups were the second turbine is axially aligned, at different distances, in the wake of the first one. Interaction effects are pointed out both in terms of performance and wake characterisation by means of a comparison with results on a single turbine. This study shows that the downstream turbine behaviour is deeply influenced by the upstream turbine wake.

We also present numerical results obtained on a single turbine from our tri-dimensional numerical software, which is developed at the \textit{Laboratoire Ondes et Milieux Complexes}, Le Havre (France). Those numerical results are validated by the comparison with the experiments, which allows us to foresee the modelling of several turbines and thus of turbine farms with a more complex layout.
1. Introduction

Marine current turbines behaviour, subject to different flow conditions, has now become well documented, mostly thanks to experimental (BATTEN et al., 2008 ; MAGANGA et al., 2010) or numerical studies (BALTAZAR & FALCÃO DE CAMPOS, 2008 ; PINON et al., 2012). However, while numerous projects concerning the implantation of turbine arrays are being launched, the interaction issue remains little discussed in the scientific literature.

It is likely that the implantation of marine current turbine arrays will be carried out in two steps. First, such arrays will only consist of one row, or two shifted rows so that no negative interaction occurs. Such farms are called first generation arrays. However, new rows will have to be implanted in order to increase the number of turbines. Negative interactions, due to the upstream turbines wakes and perceived by the downstream turbines, will then be unavoidable (see figure 1). These are called second generation arrays (MYERS et al., 2010 ; RAWLINSON-SMITH et al., 2010).

![Figure 1. Schematic top view of a turbine array with the different layout parameters involved.](image)

Although one may find some a priori suggestions regarding the implantation of marine energy converter arrays (MYERS et al., 2010 ; RAWLINSON-SMITH et al., 2010), to the authors’ knowledge, no real operating conditions study has been carried out to this day on horizontal axis turbines. We propose to mark a first milestone by studying the interactions between two marine current turbines, located one behind the other.

In the first part of this work, we present numerical and experimental results on a single turbine, which are used in the second part in order to point out the existence of interaction effects between two aligned turbines.
2. Single turbine setup
The behaviour of a marine current turbine is subject to several parameters, amongst others:
- The upstream velocity, uniform in this study, denoted by $U_\infty$;
- The Tip Speed Ratio (TSR), defined as the ratio between the tip velocity and the upstream velocity $U_\infty$:
  \[ \text{TSR} = \frac{\Omega R}{U_\infty}, \]  \[ (1) \]
  where $R = D/2$ is the rotor radius and $\Omega$ its rotation speed;
- The ambient turbulence intensity rate ($\text{TI}_\infty$), defined by:
  \[ \text{TI}_\infty = 100 \times \frac{\sqrt{u'^2 + v'^2 + w'^2}}{\sqrt{\bar{u}^2 + \bar{v}^2 + \bar{w}^2}}, \]  \[ (2) \]
  where $u$, $v$, $w$ are the three vector velocity components, $\bar{q}$ denotes the time-averaged value and $q'$ the standard deviation of any quantity $q$.

Trials were run in IFREMER’s flume tank in Boulogne-sur-Mer (France), on a 1/30 scale model of a turbine prototype. Figure 2 depicts a schematic view of the experimental setup. Wake measurements were performed with a LDV (Laser Doppler Velocimetry) system, while the force and moment were measured with a six-components load cell (three force and three moments components).

![Figure 2. Schematic view of the experimental setup.](image)

The flume tank is $18 \times 4 \times 2$ m, which is large enough to neglect any blockage effect. The turbine model description is given in table 1.
Table 1. Turbine model description.

<table>
<thead>
<tr>
<th>Feature</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Blade profile</td>
<td>NACA63418</td>
</tr>
<tr>
<td>Rotor diameter (D)</td>
<td>700mm</td>
</tr>
<tr>
<td>Hub diameter</td>
<td>92mm</td>
</tr>
<tr>
<td>Hub length</td>
<td>700mm</td>
</tr>
<tr>
<td>Studied TSR</td>
<td>[0;10]</td>
</tr>
<tr>
<td>Direction of rotation</td>
<td>Counter-clockwise</td>
</tr>
<tr>
<td>Reynolds (Re = U∞R/ν)</td>
<td>≈280 000</td>
</tr>
</tbody>
</table>

2.1 Wake characterisation

By means of the LDV system, the mean velocity is evaluated at different locations downstream of the turbine. With a fine enough grid, wake maps may thus be drawn. Figure 3 shows two downstream axial velocity maps; the first one (figure 3(a)) corresponds to a flow with a 5% turbulence intensity rate TI∞, while the second one (figure 3(b)), corresponds to a flow with a much higher TI∞ (25%). These maps point out that the ambient turbulence conditions deeply influence the turbine behaviour. As a matter of fact, with the highest TI∞ (25%), the downstream flow tends to recover its uniformity and its initial upstream velocity from seven diameters behind the turbine; on the contrary, with a 5% TI∞, the wake remains well pronounced even ten diameters behind the turbine.

![Figure 3. Axial velocity maps for two different TI∞, with TSR = 3.67.](image)

The downstream turbulence can be evaluated in the (O;x;y) plane by the downstream turbulence intensity rate, denoted by TI, and defined by:

\[
TI = 100 \times \frac{\sqrt{u'^2 + v'^2}}{\sqrt{u'^2 + v'^2}}. \tag{3}
\]

Thus, TI maps may be drawn downstream of the turbine in a flow with a 5% TI∞ (figure 4(a)) or a 25% TI∞ (figure 4(b)). These maps confirm the deep influence of the ambient turbulence and show, once again, that in a flow with a weak turbulence...
intensity, the disturbance caused by the turbine remains pronounced over more than ten diameters downstream (MAGANGA, 2011).

\[ \gamma(x) = 100 \times \left(1 - \frac{\bar{u}(x)}{U_\infty}\right). \]  

From these profiles, the axial velocity mean value \( \bar{u} \) can be assessed at some distance \( x \) from the turbine, by integrating the axial velocity on the turbine influence area, of radius \( R^* \), at this distance:

\[
\bar{u}(x) = \frac{1}{R^*} \int_{-R^*}^{R^*} \int_{-\infty}^{\infty} u(x, y) dy.
\]

In fact, this corresponds to an axi-symmetric approximation of the velocity integrated on the \( R^* \) radius disc, defined in the plane perpendicular to the turbine axis. Its centre is located on the turbine axis, at a distance \( x \) from the latter. Here, \( R^* \) is chosen a bit larger than \( R \) so as to take the whole velocity deficit into account. The mean deficit at \( x \) is then basically given by:

\[
\gamma(x) = 100 \times \left(1 - \frac{\bar{u}(x)}{U_\infty}\right).
\]

This quantity allows us to better compare our numerical and experimental results. The software is developed in the Laboratoire Ondes et Milieux Complexes of University of Le Havre, by our team. It is based on a vortex method and is described in detail in (PINON et al., 2005 ; PINON et al., 2012).

Figure 5 depicts a numerical axial velocity map, for a 0% equivalent TI \( \infty \) (figure 5(a)), and the velocity deficit comparison with the experiments (figure 5(b)). The numerical results agree globally well with the the experimental results. The observed discrepancies come from the fact that ambient turbulence cannot be modelled yet in the software, and that its turbulence model for the downstream wake is not sophisticated enough.
2.2 Turbine performance

The turbine performance can be assessed by its power coefficient, defined by:

\[ C_p = \frac{M_x \Omega}{\frac{1}{2} \rho \pi R^2 U_x^3} \]  \hspace{1cm} (6)

where \( M_x \) denotes the rotor axial moment.

Figure 6 shows the turbine power coefficient evolution function of its TSR. The operating point is reached between TSR = 3 and TSR = 4, with about 40% recovered energy (\( C_p = 0.4 \)). The numerical evolution matches the experimental evolution until TSR = 3. The fact that the numerical \( C_p \) keeps increasing stems from our particle emission scheme, which does not model flow separation on the blades.

Likewise, the thrust coefficient might be considered function of the TSR. This coefficient, denoted by \( C_T \), is defined by:

\[ C_T = \frac{F_x}{\frac{1}{2} \rho \pi R^2 U_x^3} \]  \hspace{1cm} (7)
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where $F_x$ denotes the axial force on the blades.

Figure 7 presents the turbine thrust coefficient function of its TSR. Once again, and for similar reasons, the numerical evolution ceases to match the experimental evolution from TSR = 3.5.

![Figure 7. $C_T$ evolution function of the TSR ($T_{I\infty} = 5\%$ for the experiment).](image)

3. Interactions between two turbines

Our study focuses on the interactions between two turbines located one in the wake of the other. The rotor axes are aligned with the flow, as shows figure 8, which describes the experimental setup. The distance between the turbines is denoted by $a$. Figure 9 shows a picture of this setup.

![Figure 8. Schematic views of the experimental setup.](image)
Figure 10(a) shows the axial velocity map behind the downstream turbine, located 4\(D\) behind the first one. The upstream TI, measured ahead of both turbines, equals 5\%. On the other hand, the TI measured 4\(D\) downstream of a single turbine, in a flow with a 5\% TI, equals 25\%. Consequently, one might expect to observe, behind the second turbine, a wake similar to the one of a single turbine in a flow with a 25\% TI (figure 3(b)). The significant difference between those two maps (10(a) and 3(b)) points out the interaction effect between the turbines. This conclusion is confirmed by the differences between maps 10(b) and 3(b).

Regarding performances, figure 11 shows the turbine \(C_{\text{p,down}}\) function of its \(\text{TSR}_{\text{down}}\), for different \(a/D\) values. The \(\text{TSR}_{\text{down}}\) is computed from expression (1), that is to say still with regard to the upstream flow velocity \(U_{\infty}\). Likewise, the \(C_{\text{p,down}}\) is computed from equation (6), with regard to \(U_{\infty}\). In a way, \(\text{TSR}_{\text{down}}\) and \(C_{\text{p,down}}\) may be considered as incorrect notations. The actual velocity assessment at the downstream turbine location would allow the computation of more physically meaningful downstream TSR and \(C_{\text{p}}\). Nevertheless, our choice is justified by the fact that they represent indicators, only based on the known upstream flow conditions, thus allowing the \textit{a priori} apprehension of a turbine farm implantation, where only the ambient site conditions would be known.
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Figure 11. Downstream turbine $C_p^{\text{down}}$ evolution function of its $\text{TSR}_{\text{down}}$, with the upstream turbine $\text{TSR}_{\text{up}} = 3$ and $\text{TI}_\infty = 5\%$.

The comparison with the single turbine $C_p$ (figure 11) points out that the influence of the upstream turbine on the downstream turbine decreases as the distance $a/D$ increases. Ten diameters downstream of the first turbine ($a/D = 10$), the downstream turbine recovers almost the same behaviour as a single turbine for the considered $\text{TI}_\infty$.

Let the efficiency $\eta$ be defined as the ratio between the maximal downstream turbine power coefficient and the power coefficient of a single turbine with $\text{TSR} = 3$:

$$\eta = \frac{\max(C_p^{\text{down}}(\text{TSR}_{\text{down}}))}{\max(C_p^{\text{up}}(\text{TSR}_{\text{up}}))} = \frac{\max(C_p^{\text{down}}(\text{TSR}_{\text{down}}))}{C_p^{\text{single}}(\text{TSR} = 3)}.$$  \hspace{1cm} (8)

Figure 12 shows the efficiency $\eta$ evolution function of the inter-device spacing. This efficiency increases with the distance to reach only 80% for a ten diameters distance between the turbines.

These results point out that, in a second generation array, a compromise should be made between the upstream turbines individual performance of and the inter-device distance. This distance is directly linked to the number of turbines in a given area.
4. Conclusions and prospects

This studied has pointed out the existence of interaction effects between two marine current turbines, aligned in a uniform flow. More particularly, with a 5% $\text{TI}_{\infty}$, the wake remains pronounced far behind the turbine in terms of axial velocity deficit, which directly impacts the downstream turbine efficiency (only 80% for a ten diameters inter-device spacing). The performance results thus show that a compromise is necessary between individual device performance and inter-device spacing.

Future work will mainly consist in expanding and improving the numerical software to include a more sophisticated turbulence model and so as to model more than one turbine. Figure 13 illustrates an eight turbines farm, modelled with our numerical tool. However, the discretisation is yet not fine enough to provide physical and converged results.

New experimental trials are planned as well, especially on wake characterisation studies behind two turbines in a 25% $\text{TI}_{\infty}$ upstream flow. In fact, a higher turbulence intensity rate should help the destruction of the coherent vortical structures generated by the turbines. Thus, the downstream turbine behaviour would be less influenced by the upstream turbine wake and the two turbines could then be implanted closer to each other.
Figure 13. Farm modelling example with eight turbines by our numerical tool.

5. Acknowledgements
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6. References