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## Enhanced upward heat transport at deep submesoscale ocean fronts

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### Abstract :

The ocean is the largest solar energy collector on Earth. The amount of heat it can store is modulated by its complex circulation, which spans a broad range of spatial scales, from metres to thousands of kilometres. In the classical paradigm, fine oceanic scales, less than 20 km in size, are thought to drive a significant downward heat transport from the surface to the ocean interior, which increases oceanic heat uptake. Here we use a combination of satellite and in situ observations in the Antarctic Circumpolar Current to diagnose oceanic vertical heat transport. The results explicitly demonstrate how deep-reaching submesoscale fronts, with a size smaller than 20 km, are generated by mesoscale eddies of size 50–300 km. In contrast to the classical paradigm, these submesoscale fronts are shown to drive an anomalous upward heat transport from the ocean interior back to the surface that is larger than other contributions to vertical heat transport and of comparable magnitude to air–sea fluxes. This effect can remarkably alter the oceanic heat uptake and will be strongest in eddy-rich regions, such as the Antarctic Circumpolar Current, the Kuroshio Extension and the Gulf Stream, all of which are key players in the climate system.

21 Vertical heat transport is one of the key mechanisms by which the ocean regulates Earth's climate. Munk and Wunsch<sup>1</sup> first  
22 postulated that vertical heat transport is balanced by an upward component due to the large-scale mean flow (>300 km) and  
23 a downward component explained by fine-scale diffusive processes (<20 km). However, recent studies<sup>2,3</sup> highlighted the  
24 importance of mesoscale eddies (50–300 km) for vertical heat transport. Thus, global vertical heat transport by the mean flow  
25 and diffusion are now thought to be both downwards and balanced by an upward eddy heat flux, with the mean and eddy  
26 components generally being the largest contributors<sup>2</sup>.

27  
28 Mesoscale eddies are intensified in energetic areas such as the Antarctic Circumpolar Current (ACC), Kuroshio Extension and  
29 Gulf Stream<sup>4</sup>. They are known to drive the production of submesoscale fronts (<20 km), i.e. regions that separate waters of  
30 different densities<sup>5–9</sup>, ubiquitous on satellite images of ocean color (Fig. 1). To date, submesoscale fronts are mainly thought to  
31 be confined to the ocean surface mixed-layer (~100 m deep)<sup>8,9</sup>. This is because, in the classical paradigm, motions below the  
32 mixed-layer are broadly assumed to be in geostrophic balance (a balance between Coriolis and horizontal pressure forces),  
33 preventing the formation of strong density gradients<sup>10</sup>. As a consequence, fine scales below the mixed-layer are still principally  
34 associated with diffusive processes that drive downward heat transport. However, a handful of studies suggest that submesoscale  
35 fronts associated with upward heat transport may also penetrate below the mixed-layer<sup>11–14</sup>. Yet, these studies do not explain  
36 the formation mechanism of these submesoscale fronts because they are confined to small domains (<50 km). Observational  
37 evidence over domains sufficiently large to capture multiple mesoscale eddies and their associated submesoscale fronts are  
38 needed for the closure of oceanic vertical heat transport. Such measurements are still lacking due to the fact that capturing fine  
39 spatial and temporal scales over extended domains lie at the edge of our observational capabilities.

40  
41 Here, we meet this observational challenge by analyzing a unique dataset collected by an instrumented elephant seal in the ACC.  
42 The seal data reveal the presence of numerous deep-reaching submesoscale fronts that extend well below the mixed-layer and  
43 are principally found on eddies' edges. We then develop a pioneering methodology, combining satellite and seal observations, to  
44 retrieve a 3-D synoptic view of ocean dynamics from meso- to submesoscale. Results explicitly demonstrate that deep-reaching  
45 submesoscale fronts are generated by the strain field associated with co-interacting mesoscale eddies. By invoking properties of  
46 mesoscale turbulence, we explain why deep-reaching fronts, counter-intuitively, drive enhanced vertical heat transport below

47 the surface mixed-layer that is directed upward, which is also supported by a numerical model analysis (see Supplementary  
48 Information). Associated vertical heat transport is larger than the mean flow and eddy contributions<sup>2</sup>, and of similar magnitude  
49 to air-sea fluxes<sup>15</sup>. This effect is argued to crucially limit oceanic heat uptake and therefore to alter the ocean heat storage  
50 capacity.

## 51 Frontal region sampled by elephant seal and satellite

52 Measurements were collected by a southern elephant seal (*Mirounga leonina*) in the Kerguelen area (Indian sector of the  
53 Southern Ocean, Fig. 1) during the austral spring and summer. The dataset has a horizontal resolution of 1 km, a vertical  
54 resolution of 1 m and extends from the surface down to 400 m in the ocean interior. Over a period of more than 3 months and a  
55 distance exceeding 5000 km, the seal continuously recorded temperature, conductivity and pressure, from which buoyancy  $b$   
56 (of opposite sign to density) is derived (see Methods). An example of the buoyancy field is shown in Fig. 2a–c. In addition,  
57 satellite altimeter observations supply daily horizontal fields of Sea Surface Height (SSH), a proxy of surface pressure, with an  
58 effective resolution sufficient to resolve mesoscale eddies with a size of 50 to 100 km.

59  
60 The area sampled by the seal from km 1000 to 2300 (in red in Fig. 1), i.e., from 11/02-24/2014, is rich in eddies and lies within  
61 the energetic ACC<sup>16</sup> as illustrated by the SSH contours in Fig. 1. The seal crossed numerous co-interacting cyclonic (low SSH)  
62 and anti-cyclonic (high SSH) mesoscale eddies. Geostrophic currents derived from SSH reach values of 1 m/s around the eddy  
63 edges (Fig. 2a), similar to those found in the Gulf Stream and the Kuroshio Extension, the two other most energetic ocean  
64 currents<sup>4</sup>. This area is thus representative of the flow field encountered within eddy-rich regions of the world oceans, and will  
65 receive particular emphasis in this study. The other areas crossed by the seal (Fig. 1) are much less energetic (Extended Data  
66 Fig. 1).

67  
68 The comparison between satellite SSH and buoyancy anomalies sampled by the seal in the turbulent area (Figs. 2a–c and  
69 S1,a–c) highlights the expected vertical structure of the mesoscale eddies<sup>10</sup>: buoyancy anomalies are positive and bowl-shaped  
70 in anticyclonic eddies (high SSH) and negative and reversed bowl-shaped in cyclonic eddies (low SSH, Figs. 2a–c and Extended  
71 Data Fig. 1a–c). The combination of satellite observations of SSH and seal measurements of buoyancy provides a synoptic 3-D  
72 view of the flow field encountered by the seal, and in particular of the eddy field, that can extend down to depths of at least 400  
73 m. We refer the reader to the Supplementary Information for a more detailed analysis of the consistency at mesoscale between  
74 these two independent datasets.

75  
76 Frontal structures, or buoyancy fronts, are identified by the along-track derivative of buoyancy and are defined as  $b_s = \partial b / \partial s$ ,  
77 with  $s$  the curvilinear abscissa, i.e. the along-track direction. The fronts, shown in Fig. 2d, have a width between 5 and 20 km  
78 and are thus submesoscale features. Indeed, the Rossby radius of deformation in the Kerguelen area is of  $\sim 15$  km<sup>17</sup>, which  
79 corresponds to an eddy radius of  $\sim 50$  km<sup>17,18</sup>, consistent with the SSH observations (Fig. 2a). These fronts are well resolved  
80 by the seal's 1-km horizontal resolution measurements. They are more numerous below the mixed-layer and extend down to  
81 at least 400 m. Large buoyancy gradients are preferentially found at the edges of the mesoscale eddies and in-between them.  
82 Buoyancy gradient magnitudes reach values larger than  $5 \times 10^{-7} \text{ s}^{-2}$ . The root mean square of the lateral gradient of buoyancy,  
83 used as an indicator of the gradient magnitude, is larger than  $0.5 \times 10^{-7} \text{ s}^{-2}$ , regardless of depth (Extended Data Fig. 2a).  
84 Compared to the few other existing submesoscale-resolving datasets<sup>19–21</sup>, these values are of the same order of magnitude,  
85 highlighting the important frontal activity of the area.

## 86 Frontal dynamics in the ocean interior

87 Fig. 3 illustrates how the production of horizontal gradients of buoyancy is driven by a pure strain field, which corresponds to  
88 the hyperbolic regions in-between co-interacting eddies<sup>5</sup>, as can be seen in Fig. 1. In the schematic Fig. 3a, the strain field  
89 (black arrows) stretches a tracer patch in the  $y$ -direction and compresses it in the  $x$ -direction. This leads to the formation of  
90 strong horizontal gradients of buoyancy, or fronts, at submesoscale that are associated with a growth rate related to the strain  
91 rate  $u_x = \frac{\partial u}{\partial x}$  (Fig. 3b).

92  
93 To assess the relevance of this mechanism in the Kerguelen area, we analyze the background strain field in relation to the  
94 observed buoyancy gradients. We use daily Finite Size Lyapunov Exponents (FSLE)<sup>22</sup> computed from satellite-derived  
95 geostrophic velocities to characterize the strain field properties (see Methods). FSLE indicate both the orientation and time scale  
96 (colorbar in Fig. 4a) of the stretching and compression induced by the strain field (respectively the red and blue curves in Figs.  
97 3a and 4a). As illustrated in Fig. 3a, we expect tracer patch, or equivalently buoyancy anomalies, to be aligned with stretching  
98 FSLE<sup>22</sup>. The spatial distribution of FSLE (Fig. 4a and Extended Data Fig. 3) confirms that regions in-between eddies and on

99 eddy edges are prone to the formation of strong horizontal buoyancy gradients. However, the seal's trajectory is often oblique  
100 rather than perpendicular to the buoyancy fronts, which may lead to an underestimation of the front's magnitude. Therefore, to  
101 correct for the seal's orientation with respect to the FSLE it encounters, buoyancy gradients are first normalized by the angle  
102 between the seal's trajectory and the FSLE direction (see Methods). Note that normalized buoyancy gradients are now referred  
103 to as  $b_x$ , where the subscript  $x$  refers to the direction normal to the stretching FSLE (Fig. 3a). We then compare the along-track  
104 time series of stretching FSLE estimated along the seal's path with the normalized buoyancy gradients at 300 m (comparison  
105 with buoyancy gradients at different depths below the mixed-layer produces similar results). There is good agreement between  
106 FSLE and normalized buoyancy gradients at 300 m (Fig. 4 and Extended Data Fig. 4a), as well as a consistent relationship  
107 linking the two (Fig. 4c). The two time-series are strongly intermittent. Peaks of FSLE and buoyancy gradients are often  
108 co-located (Fig. 4a-b and Extended Data Fig. 4a). Note that similar results are obtained with non-normalized gradients, which  
109 demonstrates that no bias is added via the normalization. Combined together, these two datasets provide observational evidence  
110 of how an eddy strain field, diagnosed at the sea surface, drives strong buoyancy gradients at submesoscale in the ocean interior.

111  
112 Comparison between panels c and d in Fig. 2 further reveals that, whereas mesoscale buoyancy anomalies are slanted on the  
113 vertical, as evidenced by the bowl-shaped structures of buoyancy (panel c), buoyancy fronts at submesoscale are almost vertical  
114 (panel d). This density slope property is related to the dynamical regime that drives these structures and can be quantified  
115 by the non-dimensional Richardson number  $Ri$  (see Methods). The small  $Ri$ -values observed in Fig. 2d suggest an energetic  
116 ageostrophic regime associated with intense vertical currents. The emergence of these vertical currents,  $w$ , counter-balances the  
117 formation of sharp submesoscale fronts generated by the ambient strain field. This mechanism is referred to as frontogenesis<sup>23</sup>  
118 and is sketched in Fig. 3b. It leads to an equilibrium that is captured by the classical omega equation, which involves the vertical  
119 current field  $w$ , the strain field  $u_x$ , and the lateral gradient of buoyancy field  $b_x$ . Here, we diagnose the vertical currents  $w$  by  
120 solving the 2-D ( $x,z$ ) quasi-geostrophic version of the omega equation<sup>23</sup>(see Methods), with  $b_x$  obtained from seal observations  
121 and  $u_x$  estimated from stretching FSLE (Fig. 4). However, compared to the full omega equation, there is a tendency for the  
122 vertical currents diagnosed here to be underestimated by  $\sim 1.4$  (see Methods).

123  
124 The vertical section of  $w$  shown in Fig. 5b reveals positive and negative  $w$ -values with large magnitudes of up to 100 m/day, i.e.  
125 almost an order of magnitude greater than what is attributed to mesoscale eddies alone<sup>24</sup>. Vertical currents have a width of 5 to  
126 10 km. They are intensified in the ocean interior, below the mixed-layer down to at least 400 m, and do not necessarily penetrate  
127 into the mixed-layer. The continuous vertical extent of these vertical currents highlights the crucial role played by deep-reaching  
128 submesoscale fronts in connecting the ocean interior to the surface. The  $w$ -field is characterized by the same intermittency  
129 present in the FSLE and buoyancy gradient fields (Figs. 2d, 4c, 5b and Extended Data Fig. 4b). Large  $w$ -magnitudes are  
130 co-located with strong buoyancy gradients and intense FSLE, and are therefore mostly found on the edges of, and in-between,  
131 eddies.

132  
133 The analysis of the vertical currents presented here is supported by a comparison with a realistic regional numerical model with  
134 a 1.5-km horizontal resolution (see Supplementary Information for more details on the model). The values of  $w$  derived from  
135 the observations are comparable to, although smaller than, what is obtained in the model (Extended Data Fig. 5a). Overall, these  
136 results suggest that the vertical pathway provided by deep ocean fronts in spring and summer is likely a generic mechanism  
137 throughout the ocean. This deep-reaching vertical pathway has important consequences for the vertical transfer of heat between  
138 the ocean interior and the surface mixed-layer, as explored in the next section.

## 139 Vertical heat transport at deep submesoscale fronts

140 Oceanic heat transport is estimated from temperature and vertical velocity anomalies, from the surface down to 400 m depth  
141 (Fig. 5a–b). A vertical section of this transport (see Methods for the calculation) is shown in Fig. 5c, where a positive (negative)  
142 value indicates an upward (downward) heat transport. Positive values result from frontogenesis processes, i.e the production of  
143 fronts, as illustrated in Fig. 3b. On the other hand, negative values arise from frontolysis processes, i.e. the destruction of fronts  
144 (see Supplementary Information). Heat transport is strongly enhanced at the location of submesoscale fronts generated by the  
145 background strain field and has a local amplitude that reaches 2000 W/m<sup>2</sup> below the surface mixed-layer, and extending down  
146 to at least 400 m, consistent with the high-resolution regional model (Extended Data Figs. 5b and 6) and, surprisingly, of the  
147 same order of magnitude as instantaneous air-sea heat fluxes<sup>19</sup>.

148  
149 We now explore the contribution of fine oceanic scales to the domain-averaged vertical heat transport. Averaged vertical heat  
150 transport within the eddy-rich area of the ACC sampled by the seal (km 1000 to 2000, in red in Fig. 1) is directed upward,  
151 i.e. from the ocean interior back to the surface (Fig. 5f). This direction is strikingly opposite to the one induced by the  
152 diffusive processes used in the classical paradigm. However, this result can be understood in terms of the direct cascade

of potential energy, a well-known property of mesoscale eddy turbulence<sup>25</sup>. The direct cascade implies that frontogenesis statistically dominates frontolysis, and thus that the net vertical heat transport associated to submesoscale fronts is positive (see Supplementary Information), which is also striking in the model outputs (Extended Data Fig. 6). Furthermore, the heat transport magnitude reaches an averaged value of  $\sim 100 \text{ W/m}^2$  at 200 m (Fig. 5f). Remarkably, this value is an order of magnitude larger than that associated with mesoscale eddies alone<sup>26</sup>, which is, along with the mean flow, traditionally thought to be the main contributor to vertical heat transport<sup>2</sup>. It is also of comparable magnitude to domain-averaged air-sea heat fluxes<sup>15</sup>, illustrating a potential coherent pathway linking the ocean interior to the atmosphere. Note that the percentage of seal dives decreases with depth (gray line in Fig. 5f), from 100 to 40% between 200 and 400 m. This is likely to account for a part of the RMS decrease (stagnation) of temperature (velocity) anomalies below 200 m, as one would have expected<sup>5</sup> (Fig. 5d,e). As a consequence, the already unexpected strong heat transport (Fig. 5c,f) is likely to be underestimated because of it, in addition to the conservative estimate of the vertical currents discussed in the previous section. Indeed, the domain-integrated heat transport from the high-resolution numerical simulation yields a similar - although stronger - positive vertical heat transport (Extended Data Fig. 7) with, for instance, a value of  $\sim 140 \text{ W/m}^2$  at 200 m. As such, these results strongly contrast with the classical paradigm based on diffusive heat transport, as they emphasize the existence of intense and upward heat transport in the ocean interior well below the ocean surface mixed-layer that are preferentially localized in strain dominated areas (Extended Data Fig. 6).

The data presented here provide the first observational evidence of large and anomalous, i.e. upward, heat transport associated with deep-reaching submesoscale fronts in an eddy-rich area of the world ocean. The observations, supported by a high-resolution regional model (see Supplementary Information), highlight the crucial role played by submesoscale frontal dynamics, in the ocean interior well below the ocean surface mixed-layer, for oceanic heat transport.

In summary, The deep-reaching frontal dynamics and its associated large positive vertical heat transport, observed here in numerous sharp fronts of the ACC, are driven by mesoscale eddies and are likely to occur widely in the ocean, such as in the eddy-rich Gulf Stream and Kuroshio Extension, all of which are key players in the climate system. It potentially plays an important role by, for instance, exacerbating restratification processes as warm (cold) waters become warmer (colder). Furthermore, a first order estimation indicates these deep ocean fronts lead to an additional increase of the sea surface temperature ranging between  $\sim 0.2$  and  $\sim 0.6^\circ\text{C}$  within a month (see Methods for the calculation and caveats), illustrating the potential impact of deep-reaching ocean fronts on air-sea fluxes and how they can substantially limit oceanic heat uptake from the atmosphere.

These observational results suggest revisiting current estimates of the Earth's heat budget and stress the need to account for small-scale physics, not only within, but also below the ocean surface mixed-layer, in the prediction of future climate states. Inaccurate representation of these physics could considerably underestimate the amount of heat transferred from the ocean interior back to the surface and, as a consequence, potentially overestimate the amount of heat the ocean can absorb. Finally, these results may have a far greater scope as the evidence for intense vertical currents associated to the deep-reaching ocean fronts presented here also provide an efficient pathway for the transport of chemical and biological tracers, with potential major implications for biogeochemical systems.

## Methods

### Sea Surface Height and geostrophic currents

The Sea Surface Height (SSH) used to retrieve the mesoscale dynamics of the Kerguelen area ( $67\text{-}91^\circ\text{E}$ ,  $48\text{-}58^\circ\text{S}$ ) is composed of the Mean Dynamic Topography CNES/CLS 2015<sup>27</sup> and the Sea Level Anomaly maps produced by the DUACS processing chain merging the multi-altimeter along-track data. This specific regional dataset was produced in the context of the DUACS-HR project aiming at increasing the resolution of altimetry maps by applying recently developed methods such as dynamic interpolation<sup>28</sup>. The period from October 2014 to January 2015 benefits from an extremely favorable satellite coverage of four altimeters: AltiKa, Jason-2, Cryosat-2 and HY-2, allowing a very good spatial and temporal sampling. The temporal resolution is daily and, as estimated in Ballarotta *et al.* (personal communication), the spatial effective resolution of the gridded anomalies approaches 40 km in wavelength. Using the geostrophic approximation, geostrophic surface currents ( $u$ ,  $v$ ) are derived from SSH following<sup>10</sup>:

$$u = \frac{g}{f} \frac{\partial SSH}{\partial x}, v = -\frac{g}{f} \frac{\partial SSH}{\partial y}, \quad (1)$$

where  $g$  is gravity and  $f$  the Coriolis parameter.

## Finite Size Lyapunov Exponent

Instead of using a direct estimate of the strain rate (i.e.,  $du/dx$  calculated directly from SSH, Fig. 3) that only describes the buoyancy gradient's growth rate, we use Finite Size Lyapunov Exponents (FSLE). Indeed, FSLE have the advantage of exploiting both the spatial and temporal variability of the velocity field deduced from SSH, and consequently provide information about both the growth rate and orientation of elongated buoyancy gradients<sup>29,30</sup>. FSLE is a Lagrangian diagnostic that measures the separation of close initial particles embedded in a given flow field. The separation's growth rate is defined as

$$\lambda(d_0, d_f) = \frac{1}{\tau} \log\left(\frac{d_f}{d_0}\right), \quad (2)$$

where  $d_0$  ( $d_f$ ) is the initial (final) separation distance and  $\tau$  the first time at which a separation  $d_f$  is reached. FSLE has the dimension of  $\text{time}^{-1}$ . FSLE is particularly suited to diagnose the properties of a strain field. Positive (negative) FSLE indicate that patches of particles are being stretched (compressed) in a given direction determined by the background strain field. As such, large positive (negative) FSLE values indicate regions of strong stretching (compression) (see Fig. 3a and Supplementary Information for more details). Here, positive (negative) FSLE are computed backward (forward) in time<sup>22</sup>.

88 daily maps of altimetry-based FSLEs were computed for the Kerguelen area following d'Ovidio *et al.* (2004)<sup>22</sup> and using the geostrophic velocities derived from SSH. Parameters were chosen close to d'Ovidio *et al.* (2004)<sup>22</sup> with  $d_0 = 0.04^\circ$  and  $d_f = 1^\circ$ , i.e. a final separation distances of about 110 km.

An along-track time series of stretching (i.e. positive) FSLE was extracted along the seal's path in order to capture the stretching direction and intensity of the strain field. A subsequent 5-km window moving average was applied to remove the strong intermittency present in the raw data (Fig. 4 and Extended Data Fig. 4a). Stretching FSLEs are then compared to lateral gradients of buoyancy sampled by the seal.

## Southern Elephant Seal measurements

A newly released *in situ* dataset collected in the austral summer by a female southern elephant seal during her three-month post-breeding trip (20 October 2014 to 16 January 2015) east of the Kerguelen Islands (Indian sector of the Southern Ocean, see Fig. 1) is analyzed. Compared to previous tags mounted on elephant seals, this one records every single dive realised by the animal (>80 dives/day) at high-resolution as opposed to 2 to 5 dives/day for previous tags. The seal is localized through the Argos satellite system and is equipped with sensors recording conductivity, temperature and pressure (CTD-Satellite Relay Data Logger) at a continuous frequency of 0.5 Hz. Only the ascending phase of a dive is used because it is more uniform in speed and direction compared to the descent when the seal dives sinusously to forage<sup>31</sup>. The dataset is comprised of 6333 dives, which corresponds to a cumulative length of 5270 km with a median spacing between two dives of 700 m (Extended Data Fig. 8a). Dives, that can be as deep as 500 to 1000 m, last less than 25 minutes and are separated by intervals of a few minutes where the seal breathes but does not transit. More than 80% of the dives reach a depth of at least 200 m, 50% reach 300 m and 35% 400 m or deeper.

To ensure a better accuracy of the temperature and conductivity-derived salinity data, two additional steps are applied: first a thermal cell effect correction is applied to the temperature and conductivity fields. A density inversion removal algorithm, which seeks the minimum adjustment of the salinity profile to achieve neutral stability is subsequently applied to the salinity field. The accuracy of the final post-processed data is of  $\pm 0.02^\circ\text{C}$  for temperature and  $\pm 0.03 \text{ g/kg}$  for salinity. More details on the post-processing method and final data accuracy can be found in Siegelman *et al.* (2019)<sup>31</sup>. Potential density is calculated from corrected conservative temperature and absolute salinity with the TEOS-10 equation<sup>32</sup>.

The animal in this study was handled in accordance with the Institut polaire francais Paul-Emile Victor (IPEV) ethical and Polar Environment Committees guidelines as part of the SNO-MEMO and IPEV program 109 (PI. H. Weimerskirch). The experimental protocols were approved by the Ethics Committee of IPEV and Polar Environment Committees.

## Buoyancy

Along-track time series of buoyancy,  $b = g(1 - \rho/\rho_0)$ , where  $g$  is gravity,  $\rho$  is potential density, and  $\rho_0 = 1025 \text{ kg m}^{-3}$  is a reference density reveals variability covering both meso- and submesoscales. For the analysis, in particular the calculation of lateral buoyancy gradients  $b_s = \partial b / \partial s$  with  $s$  the curvilinear abscissa, buoyancy was first linearly interpolated along the seal's path onto a regular grid of 100 m resolution, corresponding to the shortest along-track distance between two dives (Extended Data Fig. 6). A moving average with a 1 km window was then applied such that the final dataset has a horizontal resolution of 1 km and a vertical resolution of 1 m. Buoyancy anomalies are resolved by multiple vertical profiles, such that the structures are

not related to aliasing of the along-track data. Surface buoyancy anomalies in Fig. 2a,b is defined by the time series of the mean buoyancy from 15 to 50 m minus its mean value calculated from 15 to 50 m along the entire trajectory.

### 239 Mixed layer depth

240 The mixed layer depth (MLD) is defined as the level of a  $0.03 \text{ kg m}^{-3}$  density increase from 15 m depth.

### 241 Normalization of buoyancy gradients

242 Since the seal's trajectory is more often oblique to the stretching FSLE it crosses rather than perpendicular to them (Extended  
243 Data Fig. 8b) and buoyancy fronts are assumed to be aligned with stretching FSLE, buoyancy gradients sampled by the seal  
244 need to be corrected in order to account for the seal's orientation with respect to the FSLE it encounters. To do so, buoyancy  
245 gradients are divided by the sine of the angle  $\theta$  between the seal's trajectory and the FSLE direction. More precisely,  $\theta$  is the  
246 angle between the FSLE eigenvector and the seal's path. To focus on the regions prone to the formation of submesoscales,  
247 only  $b_y$  associated with large FSLE ( $>0.15 \text{ day}^{-1}$ ) have been normalized and are then referred to as  $b_x$ . However, a sensitivity  
248 analysis (ranging from 0.1 to  $0.3 \text{ day}^{-1}$ , not shown here) to this threshold value leads to similar results.

### 249 Link between strain, frontogenesis and vertical heat transport (Fig. 3)

250 The ambient strain field in Fig. 3a acts to elongate the tracer patch in the stretching direction (y-direction) and to compress it  
251 in the x-direction since the area of the tracer patch is conserved to leading order<sup>10</sup>. This increases the tracer gradient in the  
252 x-direction. The orientation and time scale of the strain field can be captured by the Finite Size Lyapunov Exponents (FSLE,  
253 see main text and Methods). Red (blue) FSLE lines identify the horizontal stretching (compressing) direction. This mechanism  
254 is particularly relevant for the formation of submesoscale fronts, that are thus aligned with the stretching FSLE (red line). Fig.  
255 3b shows a schematic illustration of the frontogenesis process. The Fig. corresponds to a 3-D slice through a submesoscale  
256 front generated by a background mesoscale strain field (curved black arrows) like the one in a). Thin black lines are isotherms.  
257 Straight black arrows correspond to the vertical velocities that develops in response to the front intensification. Warmer (or  
258 equivalently lighter) fluid (light red) is on the right of the Fig. and colder (or equivalently heavier) fluid (light blue) is on the left.  
259 As a consequence, the vertical heat transport associated to frontogenesis is directed upward because of the positive correlation  
260 between temperature and vertical velocity anomalies.

### 261 Richardson number

262 The non-dimensional Richardson number  $Ri$ , estimated from the seal measurements, is defined as  $Ri \equiv f^2 N^2 / b_x^2$ , with  $N^2 =$   
263  $\partial b / \partial z$  the Brunt-Väissälä frequency and  $b_x = \partial b / \partial x$  the along-track lateral gradient of buoyancy.  $Ri$  characterizes the dynamical  
264 regime and can be interpreted as the steepness of the isopycnal slopes relatively to  $N/f$ , since  $Ri = \frac{f^2}{N^2} \left( \frac{\partial b / \partial z}{\partial b / \partial x} \right)^2 = \frac{f^2}{N^2} \left( \frac{\partial x}{\partial z} \right)^2$ .  
265 Thus, for  $Ri \gg 1$ , which corresponds to the quasi-geostrophic regime<sup>33,34</sup>, the steepness of the isopycnal slope,  $\frac{\partial b / \partial x}{\partial b / \partial z}$ , is small.  
266 For  $Ri$  close to one (i.e.  $Ri \leq 4$ ), which corresponds to the ageostrophic regime<sup>33,34</sup>, the steepness of the isopycnal slope,  $\frac{\partial b / \partial x}{\partial b / \partial z}$ ,  
267 is large. Seal observations suggest a strong ageostrophic regime since instances of strong  $b_x$ ,  $|b_x| \geq 2.5 \times 10^{-7} \text{ s}^{-2}$ , coincide  
268 with  $Ri < 2$  (Extended Data Fig. 2b). Small  $Ri$ -values ( $Ri < 2$ ) indicate an ageostrophic regime where vertical currents are  
269 large<sup>33,34</sup>. Instances of strong  $b_x$ ,  $|b_x| \geq 2.5 \times 10^{-7} \text{ s}^{-2}$ , coincide with  $Ri < 2$  (Fig. 2 and Extended Data Fig. 2b).

### 270 Vertical velocities

271 Classical methods to diagnose vertical velocities are based on the Q-vector version of the omega equation<sup>23,35</sup>. In this study,  
272 we use the quasi-geostrophic (QG) version of the omega equation (see the Supplementary Information section for a discussion  
273 about this choice). Buoyancy fronts are assumed to be elongated along a stretching direction (red FSLE in Fig. 3a) such that the  
274 along-front gradient of buoyancy in the y-direction is negligible with respect to the cross-front one (x-direction). Thus, we  
275 consider the 2-D version (x,z) of the QG omega equation. This equation assumes that the trajectory is normal to the front, i.e.  
276 that the front is embedded in a pure strain field, which is achieved through the buoyancy gradients normalization mentioned  
277 above. This equation reads :

$$N^2 w_{xx} + f^2 w_{zz} = -2 (u_x b_x)_x, \quad (3)$$

278 where subscripts indicate derivatives.  $u_x$  is estimated from stretching FSLE derived from satellite altimetry and  $b_x$ ,  $N^2$  and  $f^2$   
279 from the seal's measurements.

281 Equation (3) is solved using the flexible framework for spectrally solving differential equations provided by dedalus<sup>36</sup>.

283 Note that when the Richardson number is close to one, equation (3) underestimates vertical velocities. When  $Ri \sim 2$ , the  
284 magnitude of this underestimation is of  $\sim 0.7$ , implying that the vertical velocities  $w$  diagnosed at sharp fronts should be closer  
285 to  $1.4 \times w$  (see Supplementary Information for more details).

286  
287 Note also that this study focuses on strain dominated regions. However, in other regions, for instance, within mesoscale eddies,  
288 the strain rate is weaker and its impact on the formation of horizontal gradients is counterbalanced by the impact of the relative  
289 vorticity, which leads to the formation of weaker gradients of buoyancy. In such regions, even though the 2-D version of the  
290 omega equation is no longer appropriate and a 3-D version needs to be used, the resulting vertical velocities are 7.5 times  
291 weaker than the ones associated to submesoscale fronts in strain dominated regions<sup>5</sup>, like the ones considered in the present  
292 study.

### 293 Vertical heat transport

294 The vertical heat transport is defined as  $\rho C_p w' T'$ , where  $C_p = 3985 \text{ J kg}^{-1} \text{ K}^{-1}$  is the specific heat capacity of seawater,  $\rho =$   
295  $1025 \text{ kg m}^{-3}$  is the density of the fluid,  $w'$  and  $T'$  the vertical velocity and temperature anomalies, respectively.

### 296 Impact of deep-reaching ocean fronts on the mixed-layer temperature

Impact of deep-reaching ocean fronts on the mixed-layer temperature, and therefore the sea surface temperature, is derived  
from a thermodynamic equation that captures the evolution of the mixed-layer temperature  $T$ . This approach has already been  
used and validated at leading order<sup>26</sup>. The equation, integrated over the mixed-layer depth, reads:

$$C \frac{dT}{dt} = S - \lambda T, \quad (4)$$

297 where  $C = \rho C_p H$  is the total heat capacity of the mixed-layer.  $H$  is the mixed-layer depth,  $S$  is the heat transport at the base of  
298 the mixed-layer due to deep-reaching fronts, and  $-\lambda T$  is the negative feedback from air-sea heat fluxes. From equation (4),  
299 positive  $S$  causes a higher temperature  $T$ , and hence a larger upward air-sea heat exchange  $\lambda T$ .

300  
301 A sensitivity analysis is carried out to assess the range of the mean mixed-layer temperature change due to submesoscales  
302 over a period of one month, which corresponds to the time spent by the seal in the turbulent region and the time span of the  
303 high-resolution model. We set  $S$  to vary between 50 and 100  $\text{W/m}^2$ , as obtained from both the observational (Fig. 5f) and model  
304 (Extended Data Fig. 7) results,  $\lambda$  to vary between 15 and 25  $\text{W m}^{-2} \text{ K}^{-1}$ , according to Vallis (2012)<sup>37</sup>, and the mixed-layer  
305  $H$  to vary between 100 and 200 m, implying that  $C$  varies between  $\sim 4 \times 10^8$  and  $\sim 8 \times 10^8 \text{ J m}^{-2} \text{ K}^{-1}$ . As a consequence,  
306 equation (4) integrated over one month indicates that the mean mixed-layer temperature increase ranges between  $\sim 0.2$  and  
307  $\sim 0.6^\circ\text{C}$ .

308  
309 Note this is a first order estimation that includes several caveats. In particular, this estimation does not take into account any  
310 subsequent atmospheric feedback on the ocean that may arise in response to these surface heat fluxes ( $\lambda T$ ). For instance, such  
311 feedback may include interactions between the windstress and SST anomalies at submesoscales<sup>38</sup>, which may limit the mean  
312 temperature increase.

### 313 Data availability

314 The marine mammal data were collected and made freely available by the International MEOP Consortium and the national  
315 programs that contribute to it, and is available at [http://www.meop.net/database/meop-databases/  
316 meop-sms-database-submesosc.html](http://www.meop.net/database/meop-databases/meop-sms-database-submesosc.html). The Ssalto/Duacs altimeter products were produced and distributed by the  
317 Copernicus Marine and Environment Monitoring Service with support from CNES, and is available at [http://marine.  
318 copernicus.eu/services-portfolio/access-to-products/](http://marine.copernicus.eu/services-portfolio/access-to-products/).

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## 402 **Author contributions statement**

403 L.S. and P.K. conceived the experiments, analysed the results and wrote the manuscript. D.M. and H.S.T. ran the numerical  
404 simulations. H.S.T helped with analyzing the regional simulation. L.S., P.K., P.R., A.F.T., H.S.T. and M.F. reviewed the  
405 manuscript.

## 406 **Competing interests**

407 The authors declare no competing interests.

## 408 **Figure captions**

409 **Fig. 1 Study region.** Three-month seal’s trajectory (black line) superimposed with a snapshot of chlorophyll a (colorscale)  
410 and SSH (white contours). Three regions are highlighted: the highly turbulent area (red), the weakly turbulent area (grey) and  
411 the southern eddy edge (orange). Cyclones (C) and anti-cyclones (A) are identified from elliptic SSH contours. Hyperbolic  
412 SSH contours located in-between eddies identify the strain field (see main text and Fig. 3a). Red arrows indicate the direction  
413 of the seal. Bathymetry contours of 0.5, 2 and 3 km (thin black lines) from NOAA ETOPO5 outline the Kerguelen plateau. The  
414 inset shows the Kerguelen region (red polygon).

415

416 **Fig. 2 Characteristics of the strongly turbulent area** (in red in Fig. 1). a) Snapshot of SSH (colorbar) and geostrophic  
417 currents (black arrows) superimposed with surface buoyancy anomaly measured by the seal from 11/02/2014 to 11/24/2014. b)  
418 Along-seal-track time series of SSH (black line), seal-measured buoyancy anomaly (blue line) and steric height (green line, see  
419 Supplementary Information). c) Seal's vertical section of buoyancy. Thin black lines are isopycnals. d) Seal's vertical section  
420 of lateral buoyancy gradients,  $b_s$ . e) Seal's vertical section of the Richardson number. The mixed layer depth is shown in bold  
421 black on panels c)–e).

422

423 **Fig. 3 Strain field, frontogenesis and vertical heat transport.** a) Horizontal slice (x,y) of tracer patch (light blue) in a  
424 strain field (black arrows). The strain elongates (compresses) the tracer in the y(x)-direction<sup>10</sup>. Red (blue) Finite Size Lyapunov  
425 Exponents (FSLE, proxy of strain) identify horizontal stretching (compressing) directions. Fronts are aligned with stretching  
426 FSLE. b) 3-D slice of strain-induced submesoscale front. Thin black lines are isotherms. Vertical velocities (w, straight  
427 black arrows) develop in response to the front intensification. Since temperature and w anomalies are positively correlated,  
428 frontogenesis-induced vertical heat transport is upward (see Methods for a full description).

429

430 **Fig. 4 FSLE and horizontal buoyancy gradients ( $|b_x|$ ).** a) Snapshot of FSLE (colorscale) and SSH contours (dashed  
431 gray) for 11/13/2014 in the strongly turbulent region (red in Fig. 1), with surface  $|b_x|$  from 11/02/2014 to 11/24/2014. b)  
432 Scatterplot of along-seal-track stretching FSLE and  $|b_x|$  at 300 m, over the entire trajectory, after a 30km-moving average and  
433 averaging the y-axis over 100 bins (black dots), unaveraged data in gray. Relationship obtained between FSLE and  $|b_x|$  in red.  
434 c) Along-seal-track time series of stretching FSLE (blue) and  $|b_x|$  at 300 m (black) after a 5km-moving average, from km 1600  
435 to 2100.

436

437 **Fig. 5 Temperature anomaly, vertical velocity and vertical heat transport (VHT).** Vertical section of a) seal-sampled  
438 temperature anomaly, b) vertical velocity derived from seal and satellite data with equation 3, c) VHT, as defined in the Methods.  
439 In a)–c), the mixed layer depth is in bold black. RMS(z) from km 1000 to 2000 of d) temperature anomaly, e) vertical velocity.  
440 f) averaged VHT ( $\langle \text{VHT} \rangle$ ).  $\langle \text{VHT} \rangle$  reaches  $\sim +110 \text{ W/m}^2$  at 200 m. The percentage of profiles (in gray) goes from 100 % at  
441 200 m to 40% at 400 m.

442

443 **Extended Data Fig. 1 Weakly turbulent and southern eddy edge areas** Same as Fig. 2 but for i) 2014/11/24 to 2014/12/20  
444 with the SSH snapshot in a) taken on 2014/12/07. The seal crosses a large anti-cyclonic region (grey trajectory in Fig. 1)  
445 characterized by weaker currents (smaller SSH anomalies) and referred to as the weakly turbulent area. ii) 2014/12/22–29 with  
446 the SSH snapshot in a) taken on 2014/12/26. The seal follows the edges of mesoscale eddies over a distance of  $\sim 600$  km. This  
447 region is referred to as the southern eddy (in orange in Fig. 1). Bold black arrows indicate the direction of the seal.

448

449 **Extended Data Fig. 2 Lateral gradient of buoyancy and Richardson number in the strongly turbulent area.** a) RMS  
450 of lateral gradients of buoyancy,  $|b_x|$ , as a function of depth in the strongly turbulent area. b) Scatter plot between lateral  
451 gradients of buoyancy,  $|b_x|$ , and Richardson number,  $Ri$ , in the strongly turbulent area.  $Ri < 2$  coincide with strong buoyancy  
452 gradients ( $|b_x| > 2.5 \times 10^{-7} \text{ s}^{-2}$ ), highlighting the ageostrophic character of the dynamical regime encountered by the seal and  
453 the expected strong frontogenesis processes at play.

454

455 **Extended Data Fig. 3 Map of finite size Lyapunov exponents** Map of FSLE over the entire domain on 13 November 2014.  
456 FSLE are greatly enhanced in the strongly turbulent region (black rectangle and in red in Fig. 1) compared to the rest of the  
457 domain.

458

459 **Extended Data Fig. 4 Finite size Lyapunov exponents and horizontal gradient of buoyancy, vertical velocities and  
460 vertical heat transport at 300 m.** Times series of a) Horizontal gradients of buoyancy at 300 m sampled by the seal (in black)  
461 and FSLE derived from satellite altimetry along the seal's track (in blue). b) Vertical velocities at 300 m derived from the seal  
462 and satellite data by solving the omega equation (see main text and Methods). c) Vertical heat transport (see Methods). The  
463 areas described in the main text and in Fig. 1 are highlighted by the colored rectangles.

464

465 **Extended Data Fig. 5 Daily averaged vertical velocities and vertical heat transport from the high-resolution numerical simulation.** Daily averaged vertical section from the high-resolution numerical simulation for November 22, 2011 at 52°S of a) Vertical velocities b) Vertical heat transport. Isopycnals are shown by the black lines. Enhanced vertical velocities and heat transport with a width of 5–10 km are found in the ocean interior and, in particular, below the mixed layer, similar to the observation presented in the main text.

470

471 **Extended Data Fig. 6 Averaged vertical heat transport from the high-resolution numerical simulation.** 2-D (x,y) view of 10-day averaged vertical heat transport (VHT) at a) 50 m and b) 200 m. Isotherms are shown in black. Domain averaged values are respectively 92 and 197 W/m<sup>2</sup>. VHT is enhanced at depth and follows the isotherms on the eddy edges, and its averaged value is directed upward (positive value), all of which is consistent with the observational results presented in the main text.

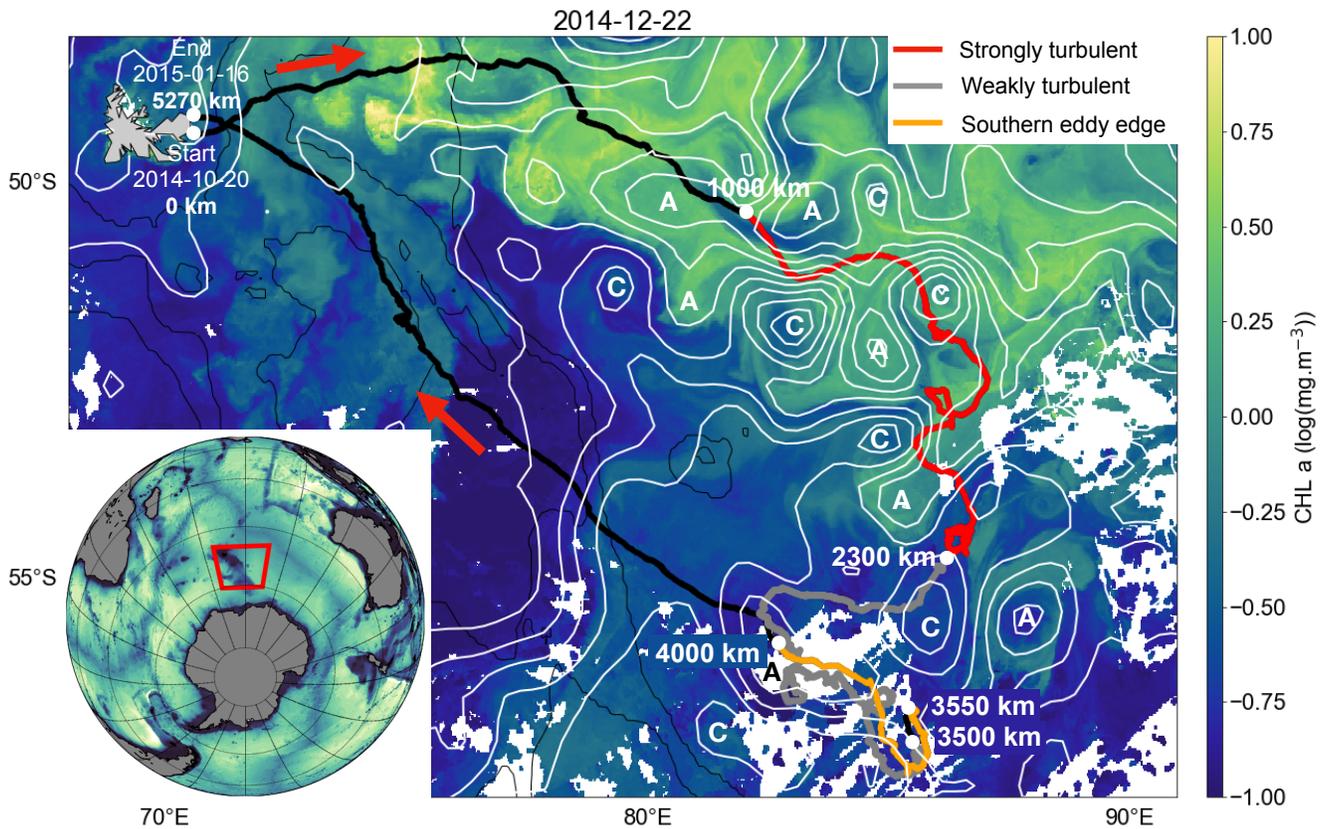
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477 **Extended Data Fig. 7 Domain averaged vertical heat transport from the high-resolution numerical simulation.** Monthly averaged vertical heat transport (<VHT>) as a function of depth over the entire domain from the high-resolution numerical simulation. VHT is directed upwards (positive values) and its magnitude is similar - although even higher - than what is derived from the observational data presented in the main text.

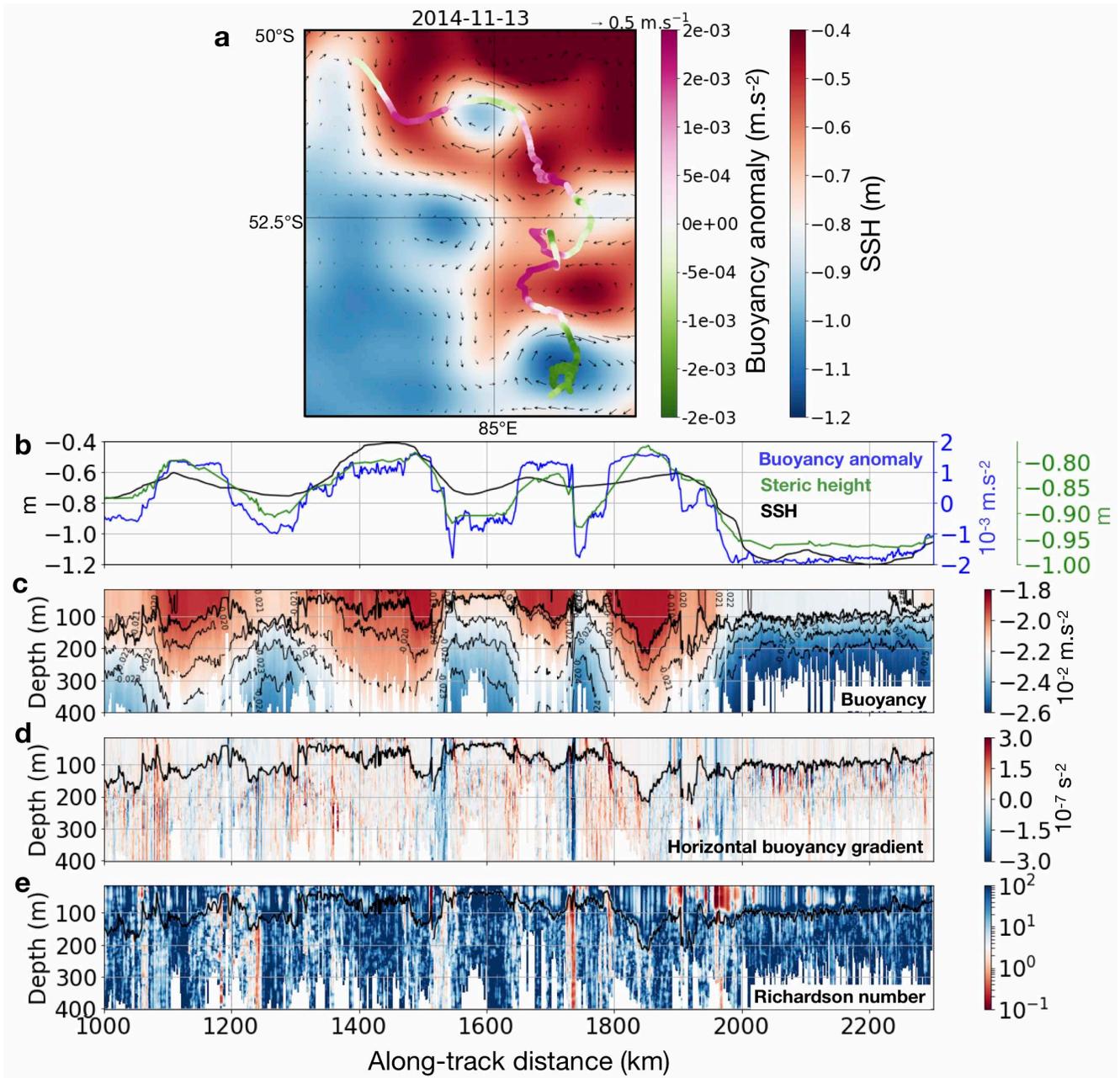
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482 **Extended Data Fig. 8 Distance between two dives and angle between the seal's trajectory and the fronts.** a) Histogram of the distance between two dives. Median distance between two dives is 700 m (dotted line) and the shortest distance is 100 m. b) Histogram of the angle between the seal's trajectory and the stretching FSLE it encounters for FSLE > 0.15 day<sup>-1</sup>. Oblique crossings are most frequent and a normalization is implemented to correct for it (see Methods).

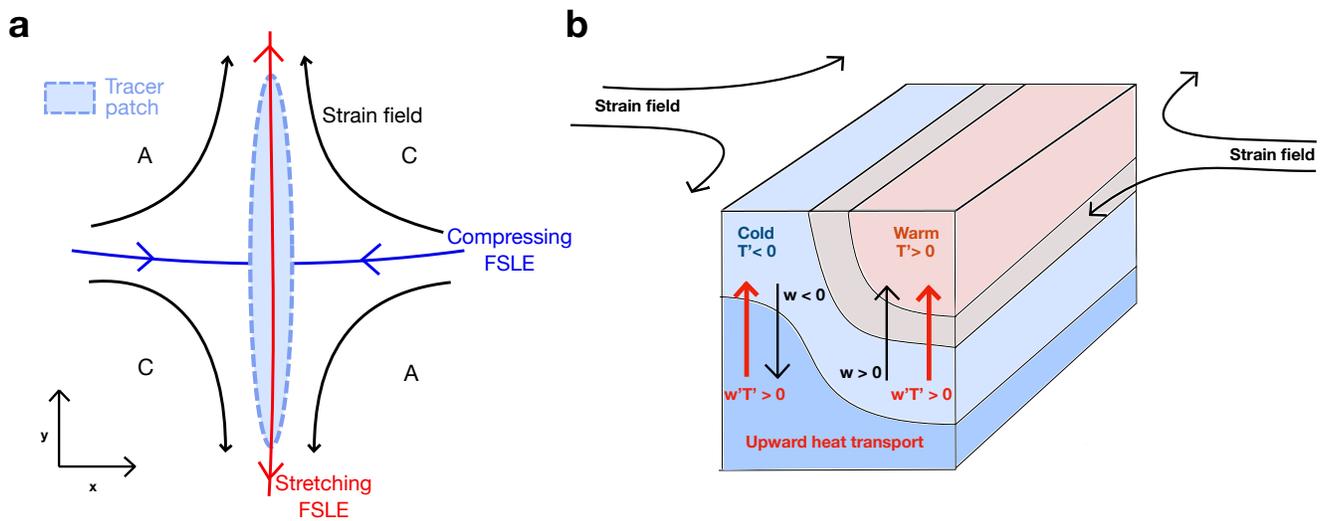
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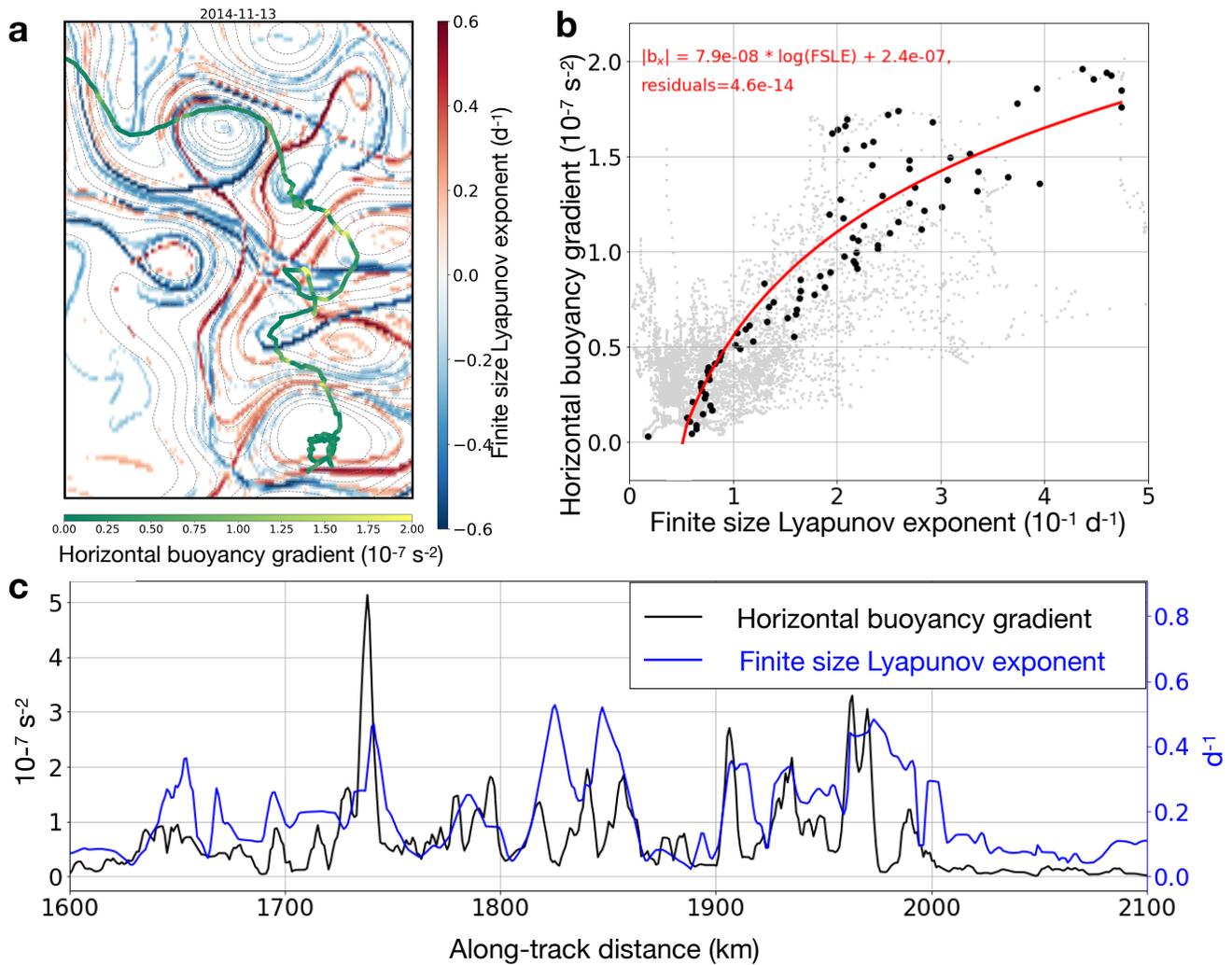
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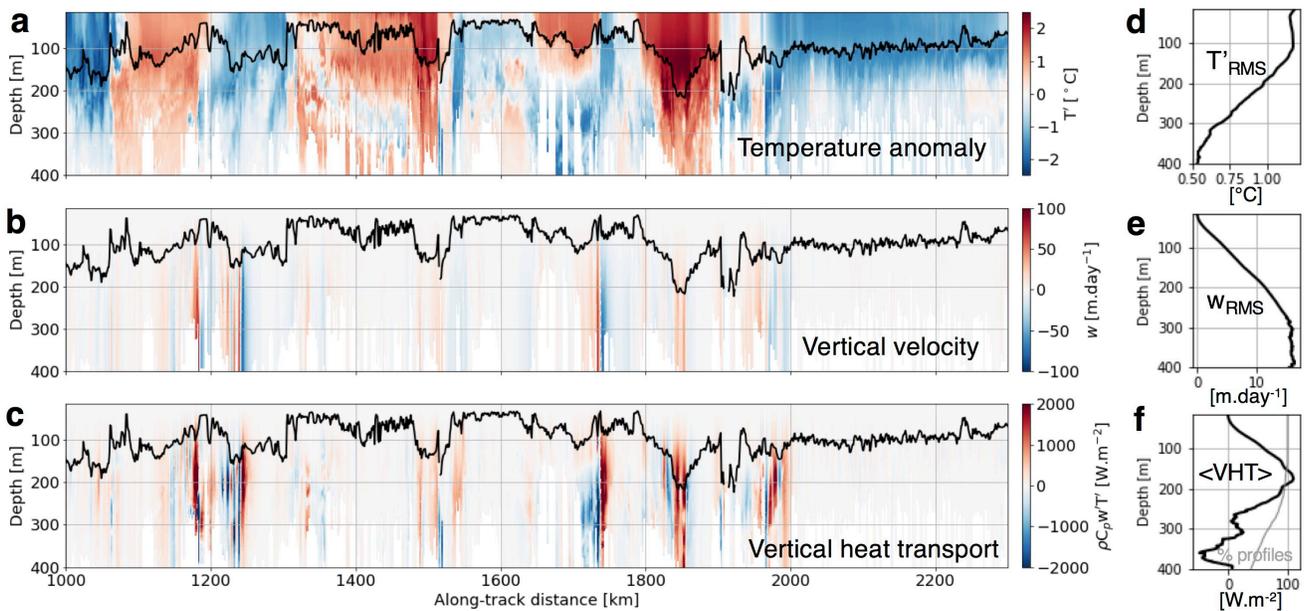
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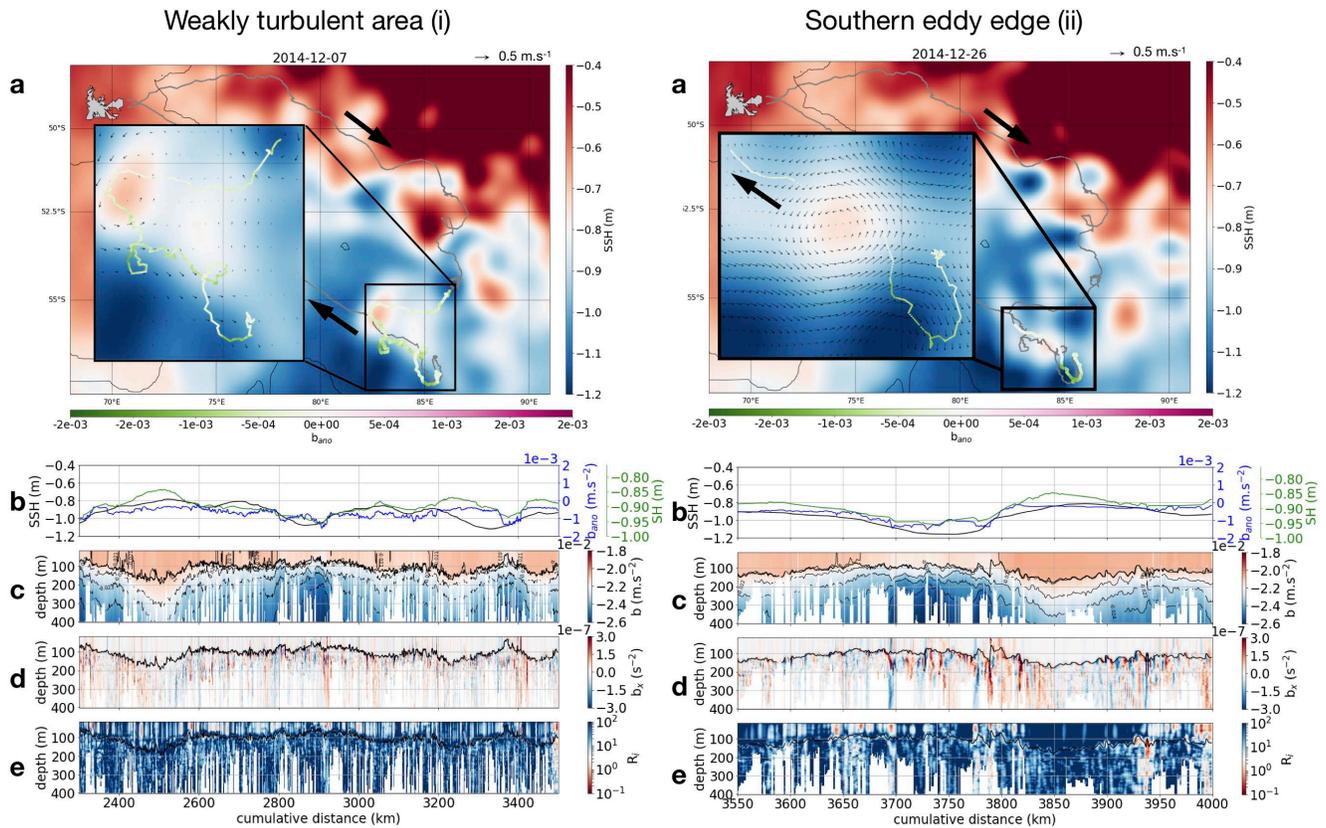
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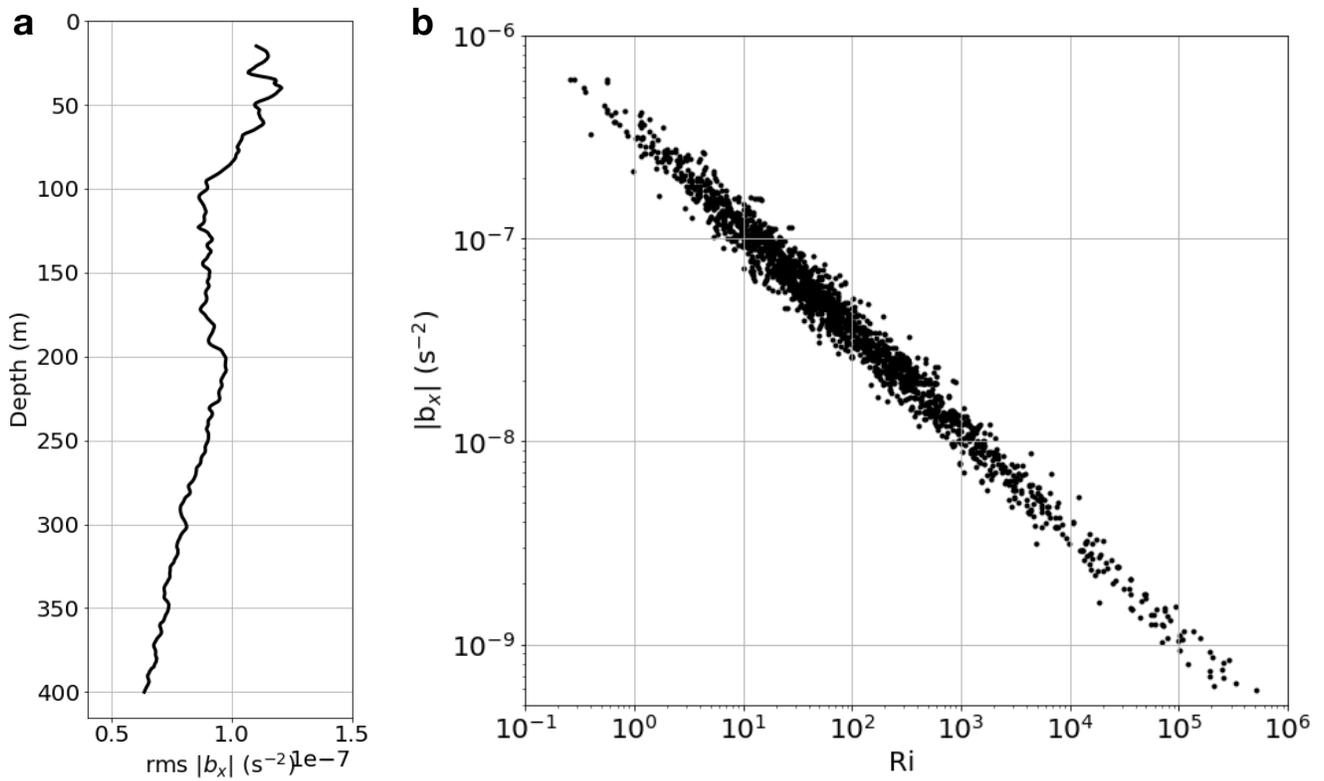
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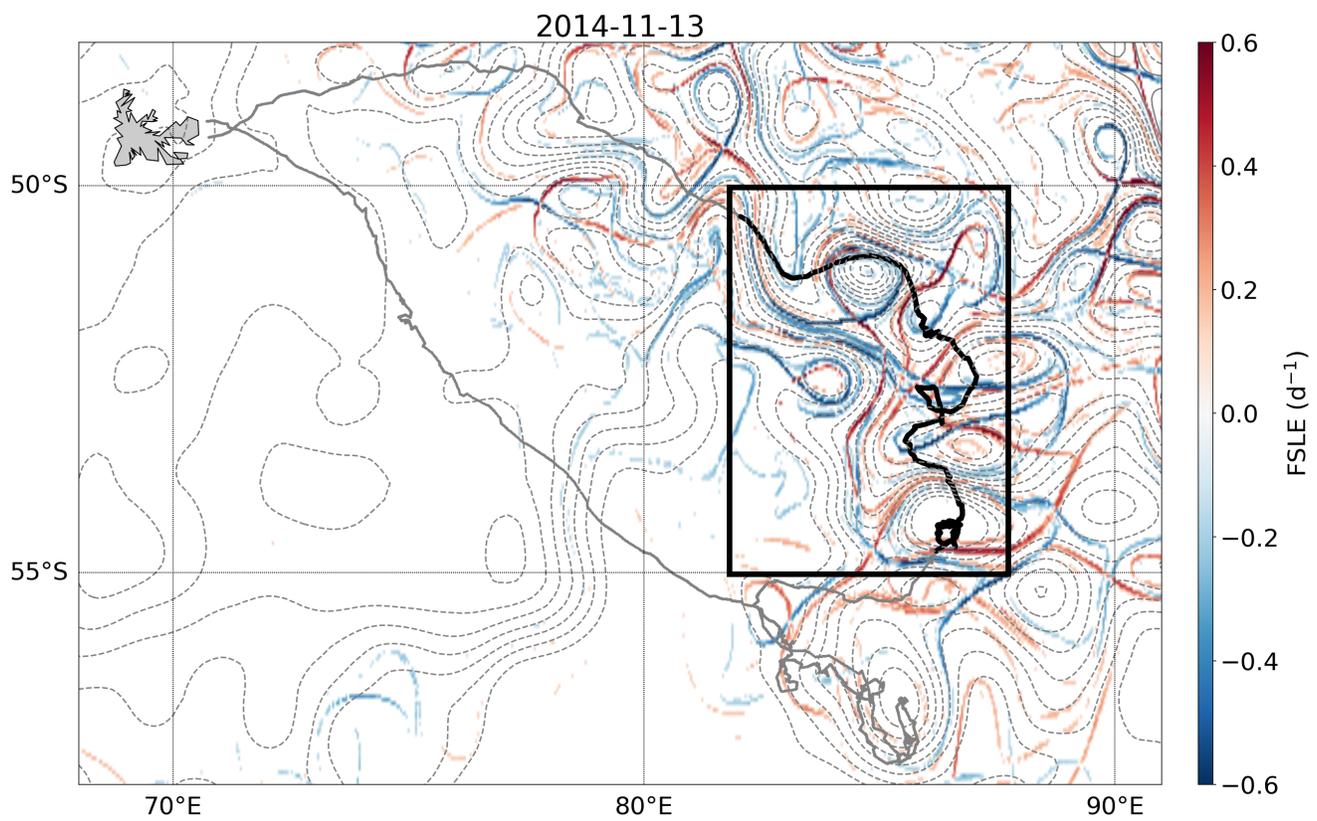
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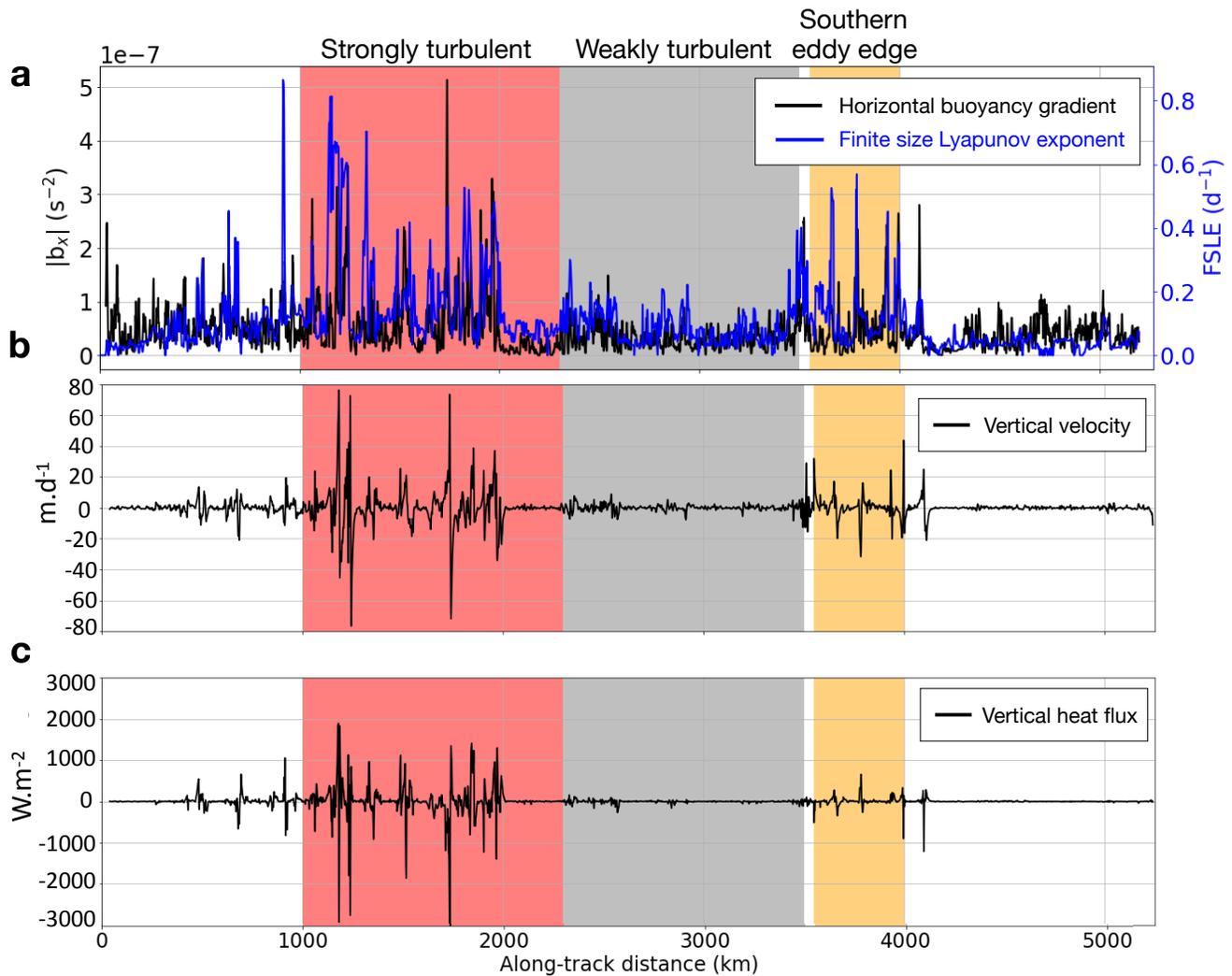
**Extended Data Fig. 1. Weakly turbulent and southern eddy edge areas** Same as Fig. 2 but for i) 2014/11/24 to 2014/12/20 with the SSH snapshot in a) taken on 2014/12/07. The seal crosses a large anti-cyclonic region (grey trajectory in Fig. 1) characterized by weaker currents (smaller SSH anomalies) and referred to as the weakly turbulent area. ii) 2014/12/22-29 with the SSH snapshot in a) taken on 2014/12/26. The seal follows the edges of mesoscale eddies over a distance of  $\sim 600$  km. This region is referred to as the southern eddy (in orange in Fig. 1). Bold black arrows indicate the direction of the seal.



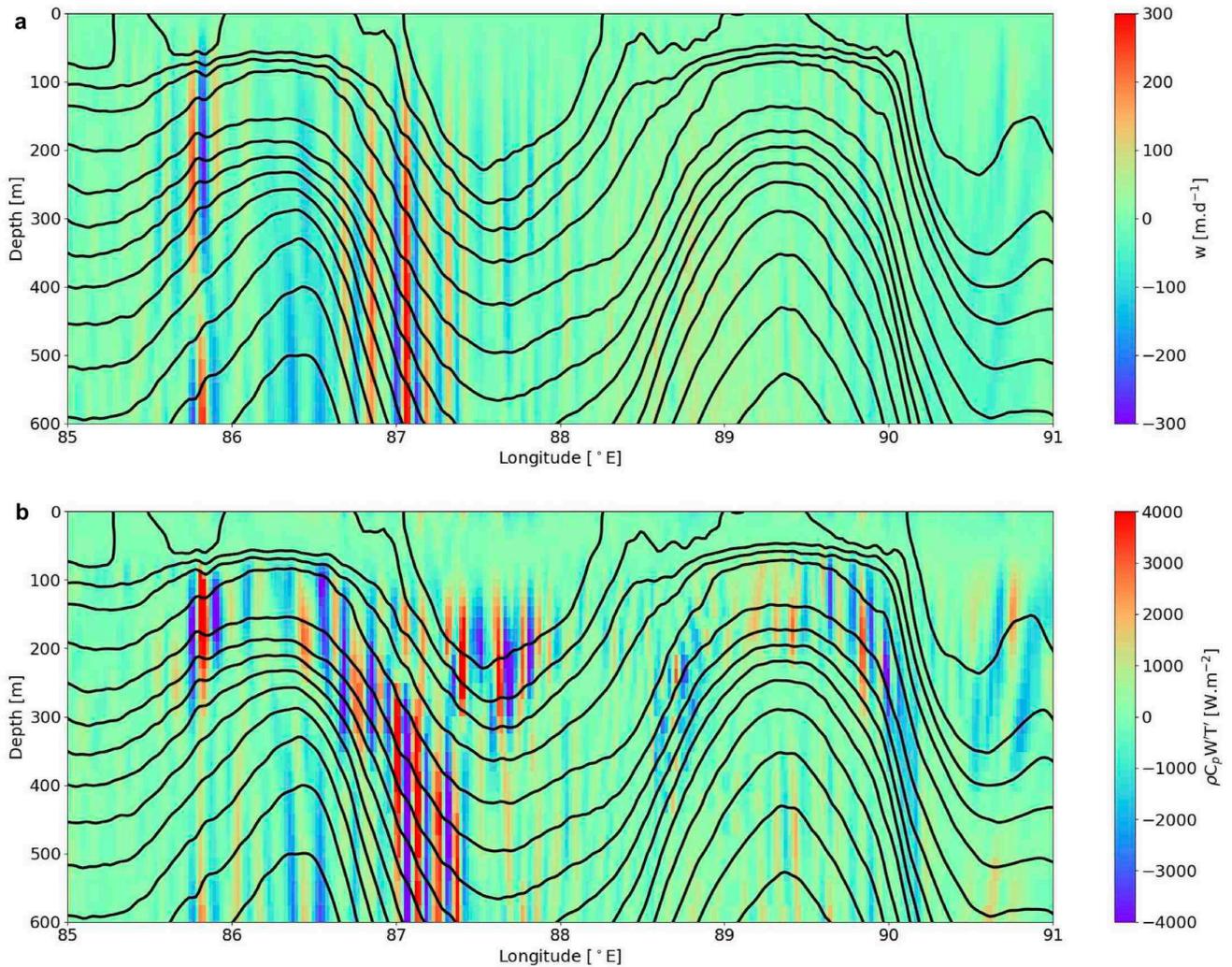
**Extended Data Fig. 2. Lateral gradient of buoyancy and Richardson number in the strongly turbulent area.** a) RMS of lateral gradients of buoyancy,  $|b_x|$ , as a function of depth in the strongly turbulent area. b) Scatter plot between lateral gradients of buoyancy,  $|b_x|$ , and Richardson number,  $Ri$ , in the strongly turbulent area.  $Ri < 2$  coincide with strong buoyancy gradients ( $|b_x| > 2.5 \times 10^{-7} \text{ s}^{-2}$ ), highlighting the ageostrophic character of the dynamical regime encountered by the seal and the expected strong frontogenesis processes at play.



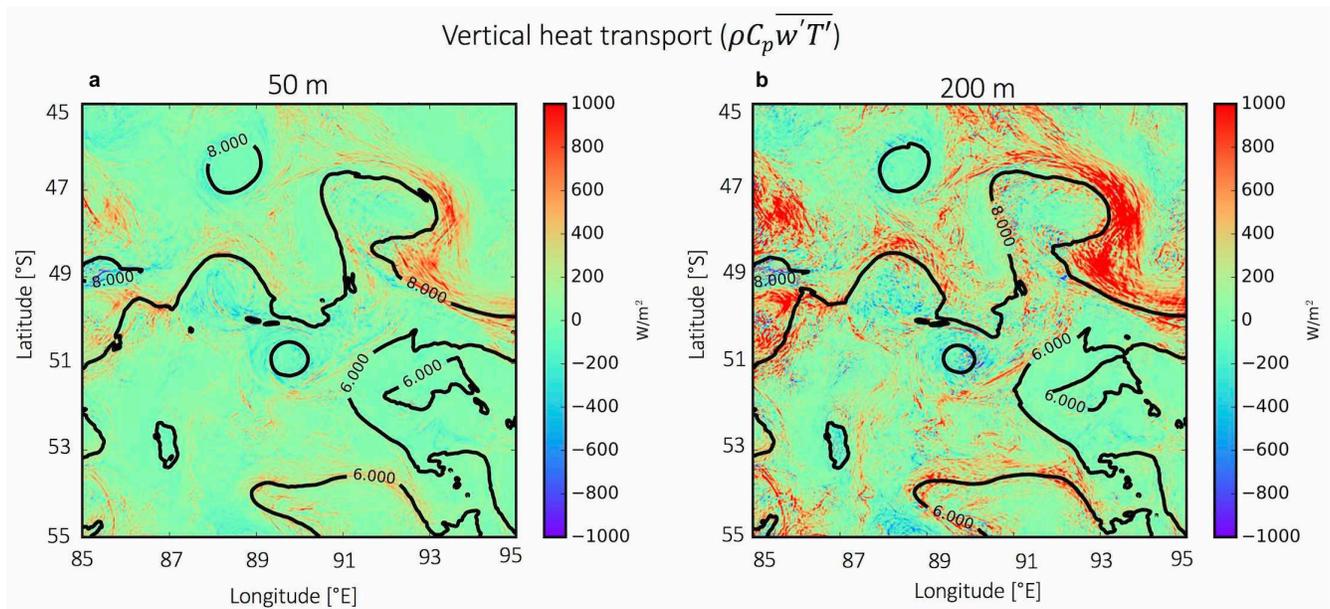
**Extended Data Fig. 3. Map of finite size Lyapunov exponents** Map of FSLE over the entire domain on 13 November 2014. FSLE are greatly enhanced in the strongly turbulent region (black rectangle and in red in Fig. 1) compared to the rest of the domain.



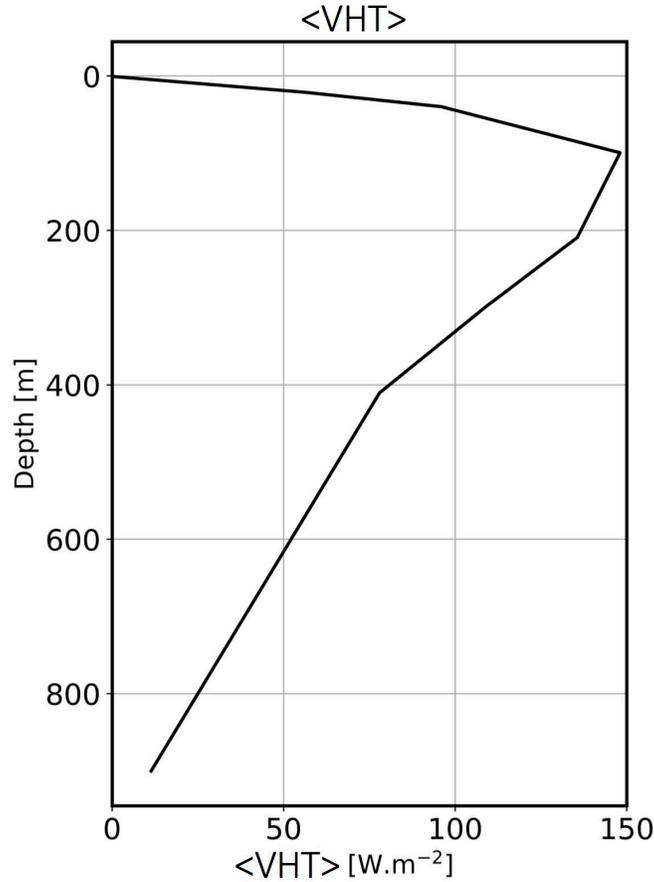
**Extended Data Fig. 4. Finite size Lyapunov exponents and horizontal gradient of buoyancy, vertical velocities and vertical heat transport at 300 m.** Times series of a) Horizontal gradients of buoyancy at 300 m sampled by the seal (in black) and FSLE derived from satellite altimetry along the seal's track (in blue). b) Vertical velocities at 300 m derived from the seal and satellite data by solving the omega equation (see main text and Methods). c) Vertical heat transport (see Methods). The areas described in the main text and in Fig. 1 are highlighted by the colored rectangles.



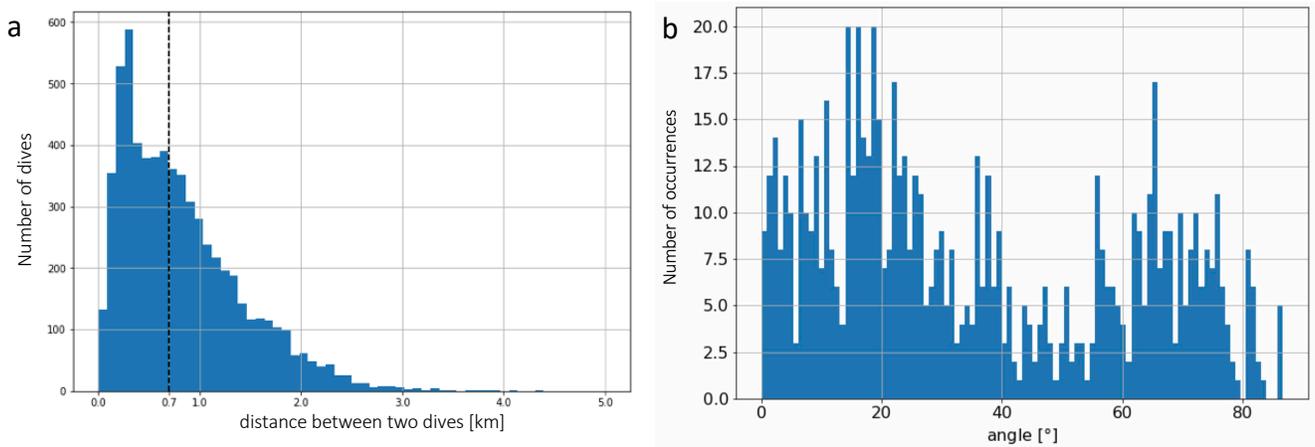
**Extended Data Fig. 5. Daily averaged vertical velocities and vertical heat transport from the high-resolution numerical simulation.** Daily averaged vertical section from the high-resolution numerical simulation for November 22, 2011 at 52°S of a) Vertical velocities b) Vertical heat transport. Isopycnals are shown by the black lines. Enhanced vertical velocities and heat transport with a width of 5–10 km are found in the ocean interior and, in particular, below the mixed layer, similar to the observation presented in the main text.



**Extended Data Fig. 6. Averaged vertical heat transport from the high-resolution numerical simulation.** 2-D (x,y) view of 10-day averaged vertical heat transport (VHT) at a) 50 m and b) 200 m. Isotherms are shown in black. Domain averaged values are respectively 92 and 197 W/m<sup>2</sup>. VHT is enhanced at depth and follows the isotherms on the eddy edges, and its averaged value is directed upward (positive value), all of which is consistent with the observational results presented in the main text.



**Extended Data Fig. 7. Domain averaged vertical heat transport from the high-resolution numerical simulation.** Monthly averaged vertical heat transport ( $\langle \text{VHT} \rangle$ ) as a function of depth over the entire domain from the high-resolution numerical simulation. VHT is directed upwards (positive values) and its magnitude is similar - although even higher - than what is derived from the observational data presented in the main text.



**Extended Data Fig. 8. Distance between two dives and angle between the seal's trajectory and the fronts.** a) Histogram of the distance between two dives. Median distance between two dives is 700 m (dotted line) and the shortest distance is 100 m. b) Histogram of the angle between the seal's trajectory and the stretching FSLE it encounters for  $\text{FSLE} > 0.15 \text{ day}^{-1}$ . Oblique crossings are most frequent and a normalization is implemented to correct for it (see Methods).

# Enhanced upward heat transport at deep submesoscale ocean fronts - Supplementary Information

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## Consistency between seal and satellite observations at meso- and submesoscale

The contribution of the vertical stratification to the SSH can be estimated by integrating the hydrostatic equation  $dp/dz = -\rho g$ . The SSH ( $\eta$ ) referenced from  $z = 0$  is then given by<sup>1</sup>

$$\eta = \frac{p'_b}{\rho_0 g} - \frac{p_a}{\rho_0 g} - \int_{-H}^0 \frac{\rho'}{\rho_0} dz, \quad (1)$$

where  $p$  is the pressure,  $\rho$  the potential density,  $\rho_0$  the reference potential density ( $1025 \text{ kg m}^{-3}$ ),  $\rho'$  the potential density anomaly ( $\rho = \rho_0 + \rho'$ ),  $g$  the gravity of Earth,  $p_a$  the atmospheric surface pressure,  $H$  the depth of the ocean and  $p'_b = p_b - \rho_0 g H$  the bottom pressure anomaly with  $p_b$  the ocean bottom pressure. The term  $\int_0^\eta \rho'/\rho_0 dz$  has been neglected because  $\eta \ll H$ . The three terms on the right hand side of equation (1) represent respectively the contributions from the bottom pressure, the atmospheric pressure loading, and the steric height. The steric height ( $\zeta$ ) is computed with the seal dataset from the surface down to  $H = 400$  m for dives reaching at least 400 m (3100 dives) as  $\zeta_{400} = \int_{-400}^0 \rho'/\rho_0 dz$ .  $\zeta_{400}$  is then compared to the SSH observed by altimetry.

SSH obtained from satellite data and mixed layer depth (MLD) and buoyancy anomalies, sampled by the seal, have a larger magnitude in the strongly turbulent region (Fig. 2) than in the weakly turbulent one (Extended Data Fig. 1i). Anticyclonic structures, or positive SSH anomalies, are associated with an increase in MLD and bowl-shaped positive buoyancy anomalies from the surface down to 400 m depth (Fig. 2 and Extended Data Fig. 1). Shallow MLD and negative buoyancy anomalies are associated with cyclonic structures, or negative SSH anomalies, confirming the fact that buoyancy anomalies compensate SSH anomalies. To further quantify this compensation over the water column, we have compared SSH with the depth-integrated buoyancy also called steric height. Since seal observations mostly sample the upper ocean, the steric height contribution has been estimated from surface down to 400 m (which concerns at least 35% of the dives) as  $\zeta_{400} = \int_{-400}^0 b dz$  with  $b$  the buoyancy (see Methods). As emphasized by the time-series in Fig. S1a (SSH in black and  $\zeta_{400}$  in blue), SSH and steric height fluctuations correlate well over the entire trajectory, but only for scales smaller than 100 km. SSH reveals a large-scale signal ( $\sim 1000$  km) not present for  $\zeta_{400}$ . This indicates that SSH at larger scales is likely compensated by the buoyancy field below 400 m and/or by bottom pressure. The contribution of  $\zeta_{400}$  to SSH is no more than 30% as revealed by the linear regression coefficient of 3.58 linking the two-time series (not shown).

To remove this large-scale contribution and focus only on the meso/sub-mesoscale band, time-series of the horizontal gradients of SSH and  $\zeta_{400}$  are computed (a gradient operator overemphasizes contribution of smaller scales). This is the equivalent of comparing horizontal currents from SSH using the geostrophic approximation, with those explained by the buoyancy field contribution in the water column using the thermal wind balance<sup>1</sup>. The two time-series are now closer in terms of amplitude differences (Fig. S1b).  $\zeta_{400}$  gradients statistically explain almost 75% of the SSH gradients as revealed by the linear regression coefficient of 1.35 linking the two time-series (not shown). This further emphasizes the consistency between the two independent datasets at meso/sub-mesoscale despite their different spatial resolution. The main differences concern the extrema of SSH gradients (mostly located on the eddy edges) that overcome those of  $\zeta_{400}$  gradients by a factor of two to three. This suggests the steric height is not integrated deep enough to capture SSH in the upper mesoscale band and therefore that dynamics of this band affects at least the first 400 m below the surface.

## Link between the strain field, Finite Size Lyapunov Exponents and lateral gradients of buoyancy

As illustrated in Fig. 3a, buoyancy anomalies embedded in a strain field are elongated in one direction and compressed in the perpendicular direction. This mechanism can be understood in terms of particle dispersion, and thus in terms of Finite Size Lyapunov Exponents (FSLE); two particles, initially close and embedded in a strain field, become quickly separated in one particular direction (the stretching direction, in red in Figs 3a and 4a). As such, the time scale of their separation can be characterized by  $\lambda^{-1}$  (see equation 2 in Methods), with large  $\lambda$  being indicative of an intense strain field. More precisely, FSLE characterize both the time scale (via the largest FSLE eigenvalue  $\lambda$ ) and the direction (via the FSLE eigenvector associated to  $\lambda$ ) of the elongation of buoyancy anomalies.

Thus, the time scale  $\lambda$  (shown in the colorbar of Fig. 4a for instance) can be used to characterize the production of buoyancy gradient expressed in the RHS of the omega equation (equation 3 in Methods). In particular, the intersection of intense compressing and stretching FSLE lines, respectively in blue and red in Figs 3a and 4a, identify Lagrangian hyperbolic points, where particles (or tracers) are simultaneously being stretched along one direction and compressed along the other one. Areas surrounding hyperbolic points are particularly prone to frontogenesis.

## Vertical velocities underestimation

At steeply tilted isopycnals' fronts, the vertical velocity field is more accurately captured by the full omega equation, known as the Sawyer-Eliassen (SE) equation, than by its QG version<sup>2,3</sup>. The 2-D (x,z) SE equation, assuming the front is embedded in a pure strain field and diffusive processes are negligible, reads<sup>2</sup>:

$$N^2 \frac{\partial^2 \psi}{\partial x^2} + F^2 \frac{\partial^2 \psi}{\partial z^2} + 2S^2 \frac{\partial^2 \psi}{\partial z \partial x} = 2u_x b_x, \quad (2)$$

with  $\psi$  a meridional streamfunction related to the ageostrophic circulation (i.e. defined as  $v_a = -\frac{\partial \psi}{\partial z}$ ,  $w = \frac{\partial \psi}{\partial x}$ , with  $v_a$  the ageostrophic component of the meridional component of the horizontal velocity field.  $N^2 = N^2(x, z)$ ,  $S^2 = -b_x$  and  $F^2 = f(f + \frac{\partial v}{\partial x})$ , where  $\frac{\partial v}{\partial x}$  is the relative vorticity associated with the front<sup>3</sup>.

Compared with the QG version (equation 3 in Methods) rewritten in the form of the ageostrophic stream function, equation (2) involves  $F^2 = f(f + \frac{\partial v}{\partial x})$  instead of  $f^2$  as well as  $N^2(x, z)$  instead of  $N^2(z)$ . In addition, equation (2) involves the extra term  $2S^2 \frac{\partial^2 \psi}{\partial z \partial x}$ . A dimensional analysis, using  $L$  and  $D$  as respectively the horizontal and depth scales of the front, indicates that this extra term is of the order of  $Ri^{-1}$ , with  $Ri$  the Richardson number, compared to the other two terms on the LHS<sup>2,3</sup>. Since  $Ri^{-1}$  is not small but close to one at locations of sharp fronts, this term should not be ignored. Nevertheless, a real solution for equation (2) exists if and only if  $F^2 N^2 - S^4 > 0$ . This condition can be written as  $f^2 N^2 (1 + Ro - Ri^{-1}) > 0$ , with  $Ro$  the Rossby number. As such, it places a strong constraint on  $Ri^{-1}$ , which is positive and has to be smaller than  $1 + Ro$ . This leads to a limitation of the steepness of the front and also to a limitation of the importance of the  $S^2$  term relatively to others.

However, we do not have access to  $F^2$  and in particular to  $\frac{\partial v}{\partial x}$ , the along-front relative vorticity, that can be of order  $f$ . SSH observations have a spatial resolution too low to resolve  $\frac{\partial v}{\partial x}$  at these scales. This is why we use the QG version (equation 3 in Methods). Nevertheless, many studies, starting with Hoskins (1982)<sup>4</sup> and more recently confirmed by Hakim and Keyser (2001)<sup>2</sup>, emphasize that the SE and QG solutions are qualitatively similar when the condition  $F^2 N^2 - S^4 > 0$  is met. In particular, the SE and QG ageostrophic circulation, and therefore the w-field, have the same sign. What differs is the amplitude of the w-field, which is larger in the SE solution, as well as the shape of the ageostrophic circulation, which is more tilted and oriented parallel to the isopycnals in the SE solution. Thus, the QG omega solution gives the correct sign for w but the magnitude may be underestimated at low  $Ri$ .

This underestimation can however be quantified using the analytical solutions for the QG and SE versions of the omega equation derived in Hakim and Keyser (2001)<sup>2</sup>. These authors show that  $w_{SA} \sim w_{QG} [\frac{PV_{QG}}{PV_{PE}}]^{1/2}$  with  $w_{SA}$  and  $w_{QG}$  respectively the solution of the QG and SA equations and  $PV_{QG}$  and  $PV_{PE}$  respectively the QG potential vorticity and the Ertel potential vorticity. Using the approximations  $PV_{QG} \sim fN^2$  and  $PV_{PE} \sim fN^2[1 - Ri^{-1}]$ , as detailed by Thomas et al. 2008<sup>3</sup>, leads to  $[\frac{PV_{QG}}{PV_{PE}}]^{1/2} = [\frac{1}{1 - Ri^{-1}}]^{1/2}$ . When  $Ri = 2$ , which corresponds to the strongest fronts in the seal measurements (see main text), we get  $w_{SA} \sim 1.4 \times w_{QG}$ . In other words, the maximum w-values found in our study should be closer to 140 m/day than to 100 m/day.

## Dominance of frontogenesis versus frontolysis understood via the direct cascade of potential energy

The classical frontogenesis process<sup>5</sup> emphasizes that the increase tendency of a buoyancy gradient embedded in a strong strain field is balanced by a vertical velocity field that tends to decrease this buoyancy gradient (black arrows in Fig. 3b). The reason is that a buoyancy gradient increase destroys the thermal wind balance and this balance is restored by the emergence of the vertical velocity field. These mechanisms lead to the omega equation (see Methods section “Vertical velocities”). As illustrated in Fig. 3b, the frontogenesis process leads to an upward vertical heat flux (red arrows in Fig. 3b) because of the positive correlation between temperature and vertical velocities anomalies.

On the other hand, the frontolysis process, or the destruction of front, occurs when the strain rate decreases and/or changes its direction. As a consequence, the buoyancy gradient relaxes, which is then balanced by a vertical velocity field (and therefore a vertical heat flux) in the opposite direction for the same reason as before (thermal wind balance). The frontolysis process is also captured by the omega equation and is associated with a downward vertical heat flux because of the negative correlation between temperature and vertical velocities anomalies (Fig. 5c). Frontogenesis (frontolysis) processes explain occurrences of positive (negative) vertical heat fluxes displayed in Fig. 5c and Extended Data Fig. 5b.

However, a well-known property of mesoscale eddy turbulence is the direct cascade of potential energy driven by the background strain field. The direct cascade refers to the creation of buoyancy anomalies at smaller and smaller scales and thus to the continuous production of submesoscale fronts<sup>6</sup>. This is why frontogenesis processes statistically dominate frontolysis ones, as can be seen in Fig. S2c where positive buoyancy fluxes are more numerous and of greater magnitude than negative ones. As a consequence, we propose that the dominance of positive vertical heat fluxes at submesoscale as demonstrated in the main text is consistent with the strong background eddy field (Fig. 5f).

## Numerical simulation comparison

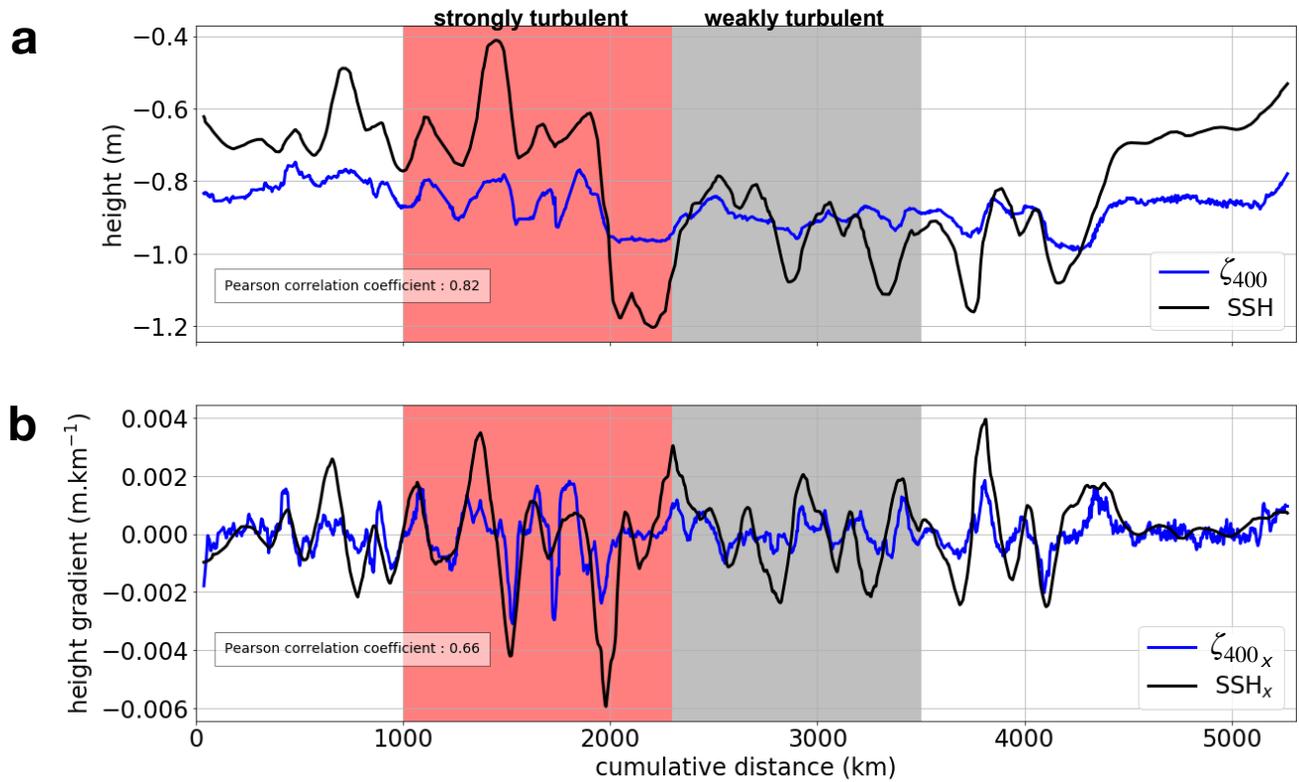
The vertical velocity field and vertical heat transport (VHT) calculated from the observations are compared to the same fields obtained from a high-resolution numerical simulation in the Kerguelen area in late spring-early summer (November 2011) performed with the Massachusetts Institute of Technology general circulation model (MITgcm). This high-resolution simulation has a horizontal resolution of  $1/48^\circ$ , 90 vertical levels and 10 minute outputs and is described in many papers (see for example Su *et al.* (2018)<sup>7</sup>). The model domain is  $45^\circ\text{S}$ – $55^\circ\text{S}$ /  $85^\circ\text{E}$ – $95^\circ\text{E}$  (or  $\sim 1000 \times 1000$  km). This domain is embedded in the MITgcm LLC 4320 global numerical simulation performed at the same resolution but with hourly outputs<sup>7</sup>. Boundary conditions and forcings are supplied by the global simulation.

Vertical sections of daily averaged vertical velocities and vertical heat transport obtained from this simulation are presented in Extended Data Fig. 5. At depths of 100–600 m, intense vertical velocities with a width of 5–10 km are present below the mixed layer and reach 300 m/day. Similar features are observed for vertical heat transport with values locally reaching  $4000 \text{ W/m}^2$ . Two-dimensional slices (x,y) of vertical heat transport averaged over 10 days are shown in Extended Data Fig. 6 at 50 and 200 m. This Fig. clearly highlights that the organization of VHT is driven by the background mesoscale strain field, intensified on the eddy edges. This Fig. also shows the dominance of positive VHT in the domain as well as its intensification at depth. Finally, Extended Data Fig. 7 presents the domain-averaged VHT over one month, which reveals similar - although larger - values than the ones derived from the observational data. Overall, the similar shape, distribution within the water column, and magnitude of both quantities in the model and in the observations strengthen the results presented in this study, and further highlight the impact of deep reaching ocean fronts on oceanic heat transport.

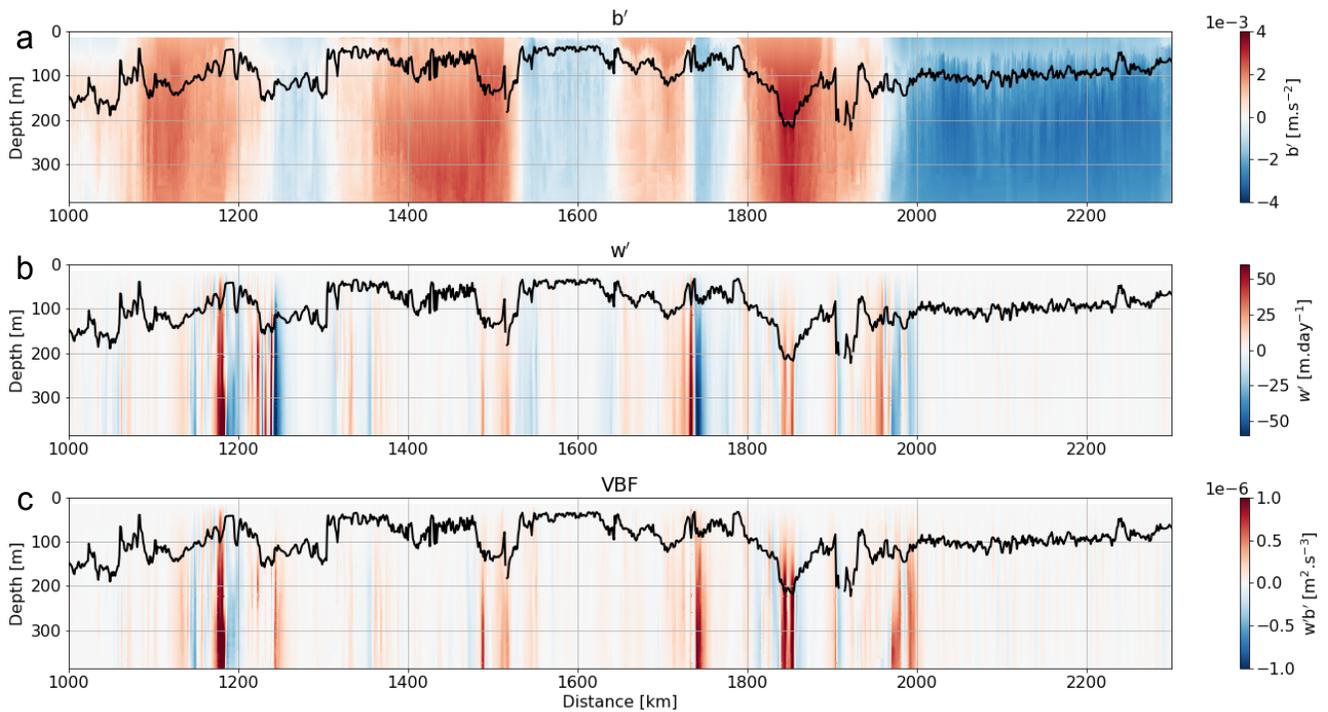
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**Supplementary Fig. S1. SSH and steric height ( $\zeta_{400}$ ).** a) Time series of satellite SSH (black line) along the seal’s path and steric height ( $\zeta_{400}$ , blue line) calculated from the SES dataset down to 400 m. b) Time series of the lateral gradients of SSH ( $SSH_x$ , black line) and steric height ( $\zeta_{400,x}$ , blue line). On both panels, the red (grey) zone corresponds to the strongly (weakly) turbulent area of Fig. 2(S1i).



**Supplementary Fig. S2. Buoyancy and temperature anomalies and vertical buoyancy fluxes from seal and satellite data** Same as Fig. 5 but for buoyancy. a) Vertical section of buoyancy anomaly sampled by the seal. b) Vertical section of vertical velocity anomaly derived from the seal and satellite data by solving the omega equation (see main text and Methods). c) Vertical section of vertical buoyancy flux (or transport, VBF) defined as  $w'b'$ , with  $w'$  and  $b'$  are the anomalies of vertical velocity and buoyancy, respectively. The mixed layer depth is shown in bold black. From panel c) it is clear that frontogenesis (positive VBF, in red) dominates frontolysis (negative VBF, in blue).