Impacts of surface gravity waves on a tidal front: A coupled model perspective

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Abstract :

A set of realistic coastal coupled ocean-wave numerical simulations is used to study the impact of surface gravity waves on a tidal temperature front and surface currents. The processes at play are elucidated through analyses of the budgets of the horizontal momentum, the temperature, and the turbulence closure equations. The numerical system consists of a 3D coastal hydrodynamic circulation model (Model for Applications at Regional Scale, MARS3D) and the third generation wave model WAVEWATCH III (WW3) coupled with OASIS-MCT at horizontal resolutions of 500 and 1500 m, respectively. The models were run for a period of low to moderate southwesterly winds as observed during the Front de Marée Variable (FroMVar) field campaign in the Iroise Sea where a seasonal small-scale tidal sea surface temperature front is present. Over the 2 day period considered, long fetch waves grow gradually propagating north east and east.

Contrasting a stand-alone ocean run with a coupled ocean-wave run shows that waves move the Ushant front offshore by up to 4 kilometres and cool the offshore stratified side of the front by up to 1.5°C. The analysis of the temperature budget shows that the change in advection is the dominant factor contributing to the frontal shift while the contribution of wave enhanced vertical temperature diffusion is secondary. Temperature, considered to be a tracer, is advected in the coupled run by the Lagrangian current resulting from the guasi-Eulerian and Stokes drift. Although the Stokes drift is directed shorewards, changes in the quasi-Eulerian current lead to a more offshore advection in the coupled than the stand-alone run. The quasi-Eulerian current is reduced (enhanced) during the ebb (flood) flow which correspond to periods of wave-following (-opposing) currents. This is due to wave breaking enhanced vertical mixing acting on the positive vertical gradient present in the quasi-Eulerian current during both ebb and flood tides. Partially coupled runs reveal that it is the surface flux of TKE associated to wave breaking that is key rather than the changes in the surface stress. They further elucidate the role of other modelled wave related processes. Although the contribution of the Stokes-Coriolis force and the wave breaking induced enhancement in vertical mixing to the quasi-Eulerian current are of similar magnitude and sign, it does not contribute significantly to the frontal shift. This is because it partially counters the Stokes drift advection which pushes the front shorewards. All Stokes drift related processes combined thus only lead to a very slight displacement of the front.

Highlights

► A novel ocean-wave coupled modelling and analysis framework was developed. ► Realistic high resolution numerical simulations reveal wave-current interactions. ► Wave enhanced mixing reduces or enhances surface currents when following or opposing. ► Waves alter the position of the surface temperature tidal front in the Iroise Sea. ► Wave-ocean dynamics and kinematics in a tidally driven coastal ocean are described.

Keywords : Ocean-wave coupling, Coastal coupled modelling, Current-wave interactions, Tidal front, Iroise Sea

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1 1. Introduction

In recent years much effort has been dedicated to understanding and quantifying the impacts of surface gravity waves on upper ocean currents and mixing as these can have significant physical and biogeochemical consequences (see *Sullivan and McWilliams*, 2010; *Cavaleri et al.*, 2012; *Villas Boâs et al.*, 2019, and references therein). The impacts in coastal seas are particularly relevant to a wide range of scientific questions and applications (*Cavaleri et al.*, 2018). Modeling wave-current interactions in coastal environments presents many challenges since they are governed by the interplay of multiple phenomena spanning a wide range of spatio-temporal scales.

Waves alter the momentum and energy input to the upper ocean. They take up a portion of the wind 9 input as they grow and release some to the ocean as they break. They generate a mean Lagrangian current 10 in the direction of wave propagation known as the Stokes drift. On the rotating earth, the Stokes drift is 11 affected by the Coriolis force inducing a current perpendicular to wave propagation and a transport that 12 compensates the Stokes drift over an inertial period (Hasselmann, 1970; Xu and Bowen, 1994). Interaction 13 between the Stokes drift velocity and the mean-flow vorticity results in the Stokes vortex force (Craik 14 and Leibovich, 1976; Lane et al., 2007). The persistent vertical shear of the Stokes drift tilts the vertical 15 component of the vorticity that is perpendicular to the wind into the wind direction. This promotes the 16 generation of rolls aligned with the wind known as Langmuir circulations (Langmuir, 1938). A thorough 17 overview of the effects of the Stokes drift on currents can be found in Suzuki and Fox-Kemper (2016). 18 Wave breaking, Langmuir circulations, Stokes drift interaction with the Coriolis force, and stirring by 19 non-breaking waves all contribute to upper-ocean mixing and turbulence (Wu et al., 2015) as shown from 20 measurements of the dissipation of the turbulent kinetic energy (Agrawal et al., 1992; Terray et al., 1996). 21

A common and highly predictable feature of coastal oceans are tidal fronts. These surface temperature 22 fronts separate cold shallow waters nearshore where tidal friction produces enough turbulence to constantly 23 mix the entire water column and warm waters offshore over depths where tidal mixing is not sufficient to 24 erode the seasonal thermocline. They appear in the spring and erode at the end of autumn. Such fronts 25 present convergence zones associated with wave steepening and breaking (Baschek et al., 2006). How in 26 turn waves alter ocean currents, temperatures, and mixing around tidal fronts has not been studied in 27 great detail because wave forcing is secondary to tidal forcing. The wave adjustement of geostrophic fronts 28 was studied by McWilliams and Fox-Kemper (2013) and Suzuki et al. (2016) showed the importance of 29 the Stokes shear in frontogenesis as they found it to energise the ageostrophic secondary circulations. 30 In these studies, the Stokes drift is of the same order of magnitude as the frontal circulation and both 31

³² are of the order or larger than the background flow. This is not the case around tidal fronts where the ³³ background tidal flow can be an order of magnitude larger than the frontal circulation and the Stokes ³⁴ drift. The set up of tidal fronts depends on the competing stratifying effect of solar radiation and tide ³⁵ driven mixing. Their location is largely determined by the magnitude of the tidal current and the water ³⁶ depth (*Simpson*, 1981). However, wave driven currents and mixing could alter the frontal position as this ³⁷ paper aims to elucidate.

Distinguishing wave effects in current measurements is not a straightforward exercise (*Polton et al.*, 38 2005; Rascle and Ardhuin, 2009; Ardhuin et al., 2009) and often does not allow for much more than 39 qualitative inferences. Laboratory experiments (Kemp and Simons, 1982, 1983; Klopman, 1993, 1994) 40 provided insights on how surface waves alter currents. The dynamics they imply have yet to be verified 41 in the field which may be in a different parameter regime and their existence in the real or modeled 42 ocean needs to be assessed. Theoretical frameworks provide insights into key physical processes but the 43 high complexity of the system does not allow to go much beyond asymptotic behaviour (McWilliams 44 et al., 2004) and specific equilibria (McWilliams and Fox-Kemper, 2013; Song, 2009). Numerical methods 45 allow to better understand the processes at play. However, asymptotic approaches and parameterisations 46 remain necessary in models. One dimensional (vertical) models have been used to study wave modification 47 to the Ekman current trying to reproduce in situ current shear measurements (Rascle et al., 2006; Rascle 48 and Ardhuin, 2009). Large eddy simulations (Polton et al., 2005; McWilliams and Fox-Kemper, 2013; 49 Sullivan et al., 2007; Suzuki et al., 2016) and direct numerical simulations (Sullivan et al., 2004) remain 50 idealistic and only represent a subset of wave related processes. 51

To investigate the multitude and complexity of processes at play in the coastal oceans, realistic fully-52 coupled ocean-wave simulations are needed. In coupled modeling, the inclusion of wave processes heavily 53 relies on parameterizations. Also, the representation of wave-current interactions is simpler than in the 54 above mentioned theoretical work. They are, however, largely based on assumptions supported by those 55 'idealised' approaches and coupled simulations can provide a broader view of the processes at play. To 56 date, several coupled model frameworks have been developed and exploited to study the impact of waves 57 on currents in coastal seas (Osuna and Wolf, 2005; Bolaños et al., 2014; Ràfols et al., 2019). While 58 Bolaños et al. (2014) concluded that waves do not significantly alter the tidally dominated component of 59 the current but improved the transverse current component, Osuna and Wolf (2005) showed large effects 60 of waves on currents especially where the currents are strong and sheared. Ràfols et al. (2019) reported 61 no substantial differences in the water current field between coupled and uncoupled simulations. 62

It is important to note here that to date the majority of studies, be it theoretical, numerical, or

experimental, have focused on cases where the Stokes drift is comparable or stronger than the background 64 flow. Filling this gap, a new set of coupled model experiments were undertaken focusing on the Iroise 65 Sea which provides an excellent natural laboratory to study interactions between the waves, the ocean, 66 and the atmosphere in strongly tidally forced conditions. Located in the North Atlantic, off the coast of 67 Brittany, France, the Iroise Sea is subject to long fetch waves and features an intense seasonal surface 68 thermal front: the Ushant tidal front (Fig. 1). It is characterized by a strong surface temperature gradient 69 separating the homogeneous waters of moderate temperatures $(<14^{\circ}C)$ close to the coast and the warm 70 surface $(>16^{\circ}C)$ stratified waters offshore. A second temperature front exists at the bottom separating 71 the waters of the cold "tongue" which covers the continental shelf and the homogeneous waters close to 72 the coast. Le Boyer et al. (2009) noted that the two fronts are governed by different dynamics meaning 73 that the two fronts are not always co-located. The position of the surface front varies with the tidal 74 current. It is pushed towards the coast during the flood tide and towards the open sea by the ebb tide. 75

This paper provides a detailed study of the wave-ocean coupling in the Iroise Sea with a focus on the impacts on the currents and surface temperatures around the Ushant front based on a set of realistic forced and coupled coastal model runs. These are described in Section 2 along with an outline of the coupling framework. Key results are presented in Section 3 and discussed in Section 4. The conclusion section summarises the results and processes at play. Finally, it highlights the interest of the proposed model and analysis framework.

82 2. Model Experiments

In this section, the equations at the heart of the stand-alone ocean model are presented first followed 83 by those used in the coupled configuration. Relevant aspects of the coupling between the ocean and the 84 wave models are detailed exposing how wave related processes are taken into account. These include 85 Stokes drift advection of tracers, Stokes-Coriolis and Stokes vortex forces on the horizontal currents, wave 86 altered surface stress, wave breaking induced turbulence, and wave orbital velocity driven bottom stress. 87 Configurations used for the ocean and wave models are then summarized along with the description of 88 the simulations' setup. The equations of the wave model with currents are not recalled herein, as the 89 focus of the paper is on the ocean response to waves. These can be found in Ardhuin et al. (2017). 90

91 2.1. Uncoupled Ocean Model

The ocean model used in this study is the 3D coastal hydrodynamic circulation model MARS3D (Model for Applications at Regional Scale, *Lazure and Dumas* (2008); *Lazure et al.* (2009)). MARS3D resolves the primitive equations for an in-compressible, hydrostatic fluid under the Boussinesq hypothesis. The temporal evolution of a horizontal current ($\mathbf{u} = u + iv$ in $\mathbf{x} = x + iy$) is modeled as:

$$\frac{\partial \mathbf{u}}{\partial t} = -\mathcal{L}(\mathbf{u}) - if\mathbf{u} + \frac{\partial}{\partial z} \left(K_u \frac{\partial \mathbf{u}}{\partial z} \right) + \frac{d}{d\mathbf{x}} \left(K_\mathbf{x} \frac{d\mathbf{u}}{d\mathbf{x}} \right) + \frac{1}{\rho_0} \frac{dP_i}{d\mathbf{x}} - g \frac{d\zeta}{d\mathbf{x}} - \frac{1}{\rho_0} \frac{dP_a}{d\mathbf{x}}$$
(1)

with the operator $\mathcal{L} = \left(u\frac{\partial}{\partial x} + v\frac{\partial}{\partial y} + w\frac{\partial}{\partial z}\right)$ and the complex derivative: $\frac{d}{d\mathbf{x}} = \frac{\partial}{\partial x} + i\frac{\partial}{\partial y}$. $\mathcal{L}(\mathbf{u})$ represents 96 the non-linear advection terms, g the acceleration due to gravity, $\rho_0 = 1027.34$ kg m⁻³ the reference water 97 density, f the Coriolis parameter, K_u the vertical eddy viscosity and K_x the horizontal ones, ζ the sea 98 surface height, and P_a and P_i the surface atmospheric and internal pressures, respectively. Since the 99 model assumes the ocean to be hydrostatic, P_i is derived from $\frac{\partial p}{\partial z} = \rho_0 b$ with the buoyancy given by: 100 $b = -g(\rho - \rho_0)/\rho_0$ and ρ the water density. The vertical velocity follows from continuity. The surface 101 boundary conditions are given by the zonal and meridional wind stress $\tau_{\mathbf{a}}$ computed from the 10-m wind 102 $(\mathbf{u_{10}})$ forcing using: 103

$$\tau_{\mathbf{a}} = \rho_a C_D \mathbf{u}_{10}^2 \tag{2}$$

where C_D is the drag coefficient based on *Charnock* (1955) and ρ_a the surface air density.

The evolution of a tracer C is given by the advection-diffusion equation:

$$\frac{\partial C}{\partial t} = -\left(\frac{\partial}{\partial x}\left[uC\right] + \frac{\partial}{\partial y}\left[vC\right] + \frac{\partial}{\partial z}\left[wC\right]\right) + \frac{\partial}{\partial z}\left(K_C\frac{\partial C}{\partial z}\right) + F$$
(3)

where K_C is the vertical diffusivity (the horizontal ones are set to 0). The source term F consists of the solar irradiance and long-wave radiation for temperature. The salinity evolves with water fluxes induced by precipitation minus evaporation as well as river outflows. The surface boundary condition for temperature diffusion is the latent and sensible turbulent fluxes.

The eddy viscosity $(K_u = c_\mu \frac{k^2}{\varepsilon})$ and vertical diffusivity for temperature $(K_C = c'_\mu \frac{k^2}{\varepsilon})$ are obtained from the two-equation $k - \varepsilon$ model (*Burchard*, 1998; *Burchard and Bolding*, 2001) which were chosen in this study for turbulence closure. The *Canuto et al.* (2001) version A (CA) stability functions c_μ and c'_μ based on the non-dimensional shear and buoyancy numbers as described in *Umlauf and Burchard* (2005) are used to damp (enhance) turbulence in stably (unstably) stratified conditions. The turbulent kinetic energy (TKE, k) is modeled as:

$$\frac{\partial k}{\partial t} = -\mathcal{L}(k) + \frac{\partial}{\partial z} \left(\nu_k \frac{\partial k}{\partial z} \right) + P + D - \varepsilon$$
(4)

where the shear P and the buoyancy D contributions are functions of the vertical shear and the Brunt-Väisäla frequency, respectively. In the configuration used here, the advection term $\mathcal{L}(k)$ is neglected. The equation of the TKE dissipation rate (ε) is given by:

$$\frac{\partial \varepsilon}{\partial t} = \frac{\varepsilon}{k} \left(c_{\varepsilon 1} P + c_{\varepsilon 3} D - c_{\varepsilon 2} \varepsilon \right) + \frac{\partial}{\partial z} \left(\nu_{\varepsilon} \frac{\partial \varepsilon}{\partial z} \right) \tag{5}$$

The empirical constants $c_{\varepsilon i}(=1.44, 1.92, -0.63 \text{ or } 1)$ are taken from *Burchard and Bolding* (2001) and *Umlauf* (2003). A positive (negative) $c_{\varepsilon 3}$ is taken for unstable (stable) stratified flows (*Canuto et al.*, 2001). The eddy viscosities ν_k and ν_{ε} are computed through constant Schmidt numbers as: $\nu_{k,\varepsilon} = \frac{K_u}{\sigma_{k,\varepsilon}}$ with $\sigma_k = 1$ and $\sigma_{\varepsilon} = 1.3$.

A constant flux condition is used at the sea surface for Eq. (4):

$$\frac{\partial k}{\partial z} = 0 \tag{6}$$

¹²⁴ For Eq. (5), the Neuman-type surface boundary condition is:

$$\frac{\partial \varepsilon}{\partial z} = \left(c^0_\mu\right)^{\frac{3}{4}} \frac{k^{\frac{3}{2}}}{\kappa \left(z_0 + z'\right)^2} \tag{7}$$

where $c_{\mu}^{0} = 0.077$ (CA), z_{0} is the surface roughness length, z' the distance to the surface boundary, and $\kappa = 0.4$ the von Karman constant.

127 2.2. Coupled Wave-Ocean Model Framework

The MARS3D has been coupled with the 3rd generation wave model WAVEWATCHIII (WW3, Tolman 128 (2014)), through OASIS-MCT (Voldoire et al., 2017). As listed on the diagram Figure 2, MARS3D sends 129 3 fields to WW3 and receives 17 fields from WW3. The framework was developed in a way to minimize 130 the parameterizations of wave dependent variables within the ocean model. Thus coupling as many fields 131 directly computed from the source function of WW3 and the model wave spectra as possible rather than 132 relying on say wave height dependent parameterizations. The coupling between WW3 and MARS3D 133 occurs every 100 s. The coupling module performs distance weighted nearest neighbour interpolations 134 from one regular model grid to the other based on 4 points using the Los Alamos National Laboratory 135 SCRIP1.4 library (Jones, 1999). 136

The impact of waves on the ocean is modeled following the quasi-Eulerien framework (*Ardhuin et al.*, 2008; *Bennis et al.*, 2011) based on wave-averaged primitive equation limited to second order wave theory. In the coupled ocean-wave configuration Eq. (1) becomes:

$$\frac{\partial \hat{\mathbf{u}}}{\partial t} = -\hat{\mathcal{L}}(\hat{\mathbf{u}}) - if\hat{\mathbf{u}} + \frac{\partial}{\partial z} \left(K_u \frac{\partial \hat{\mathbf{u}}}{\partial z} \right) + \frac{d}{d\mathbf{x}} \left(K_\mathbf{x} \frac{d\hat{\mathbf{u}}}{d\mathbf{x}} \right) + \frac{1}{\rho_0} \frac{dP_i}{d\mathbf{x}} - g \frac{d\zeta}{d\mathbf{x}} - \frac{1}{\rho_0} \frac{dP_a}{d\mathbf{x}} - if\mathbf{u}_\mathbf{s} - i \left(\frac{\partial \hat{v}}{\partial x} - \frac{\partial \hat{u}}{\partial y} \right) \mathbf{u}_\mathbf{s} - \frac{\partial \hat{\mathbf{u}}}{\partial z} w_s - \frac{\partial J}{\partial \mathbf{x}}$$
(8)

where $\hat{\mathbf{u}}$ is the quasi-Eulerien velocity defined as the difference between the Lagrangian velocity $(\mathbf{u}_{\mathbf{L}})$ and the horizontal Stokes drift $(\mathbf{u}_{\mathbf{s}})$:

$$\hat{\mathbf{u}} = \mathbf{u}_{\mathbf{L}} - \mathbf{u}_{\mathbf{s}} \tag{9}$$

Both $\hat{\mathbf{u}}$ and $\mathbf{u_s}$ satisfy continuity. In Eq. (8) $\hat{\mathcal{L}} = \left(\hat{u}\frac{\partial}{\partial x} + \hat{v}\frac{\partial}{\partial y} + \hat{w}\frac{\partial}{\partial z}\right)$ and w_s is the vertical component 142 of the Stokes drift. New wave dependent terms appear on the right hand side terms of Eq. (8): the 143 Stokes-Coriolis force $(if\mathbf{u}_{\mathbf{s}})$, the Stokes vortex force $\left(-i\left(\frac{\partial \hat{u}}{\partial x}-\frac{\partial \hat{u}}{\partial y}\right)\mathbf{u}_{\mathbf{s}}-\frac{\partial \hat{\mathbf{u}}}{\partial z}w_s\right)$, and the wave-induced 144 Bernoulli head pressure (J, Smith (2006)). In this configuration, the model remains hydrostatic and the 145 impact of the Stokes shear on the pressure gradient (see Suzuki and Fox-Kemper, 2016) is not taken into 146 account. Note that only surface Stokes drift fields are sent by the wave model to the ocean model along 147 with the Stokes transport. These are then used to approximate vertical Stokes profiles based on *Breivik* 148 $et \ al. \ (2014).$ 149

In addition to these modifications in current equations, the boundary conditions are changed. The surface stress felt by the ocean is no longer $\tau_{\mathbf{a}}$ but:

$$\tau_{\text{surf}} = \tau_{\mathbf{a}} - \tau_{\mathbf{aw}} + \tau_{\mathbf{wo}} \tag{10}$$

where τ_{aw} corresponds to the amount of momentum used by wave formation and τ_{wo} to the breaking wave induced stress transferred to the ocean. These fields, provided by WW3, are derived from the input and dissipation source functions (*Tolman*, 2014). At the bottom boundary, the stress due to the waves is added to the bottom friction. It is computed from the bottom orbital velocities \mathbf{u}_{bw} and a wave friction factor following *Soulsby et al.* (1993). For the wave friction factor the parameterisation of *Soulsby* (1997) (their Eq. 62a) is used.

¹⁵⁸ Waves impact the advection of tracers which is done by the Lagrangian velocity. Thus, with waves ¹⁵⁹ Eq. (3) becomes:

$$\frac{\partial C}{\partial t} = -\left(\frac{\partial}{\partial x}\left[\left(\hat{u} + u_s\right)C\right] + \frac{\partial}{\partial y}\left[\left(\hat{v} + v_s\right)C\right] + \frac{\partial}{\partial z}\left[\left(\hat{w} + w_s\right)C\right]\right) + \frac{\partial}{\partial z}\left(K_C\frac{\partial C}{\partial z}\right)$$
(11)

Waves effects have also to be considered as impacting eddy viscosity and diffusion terms in Eqs. (8) and (11). This is achieved by modifying the surface boundary conditions of the turbulent closure equations and adding a new source terms within the bottom boundary layer. The TKE production term added to the right hand sides of Eqs. (4) and (5) is taken from *Walstra et al.* (2000). For k, it stands as:

$$P_w^{bot}(z) = \frac{2\Phi_{bbl}}{\delta} \left(1 - \frac{d+\zeta-z}{\delta} \right) \quad \text{for } d+\zeta-z \le \delta$$
(12)

where Φ_{bbl} is the wave energy dissipation due to bottom friction sent by WW3 to MARS3D and d the topography. The bottom wave boundary layer thickness δ is derived following *Grant and Madsen* (1982) (their Eqs. 5 and 6) based on the wave friction factor. These depend on the bottom orbital velocities $\mathbf{u_{bw}}$ and the mean wave period T_{m1} provided by WW3.

168 Thus Eqs. (4) and (5) become:

$$\frac{\partial k}{\partial t} = -\mathcal{L}(k) + \frac{\partial}{\partial z} \left(\nu_k \frac{\partial k}{\partial z} \right) + P + D - \varepsilon + P_w^{bot}$$
(13)

$$\frac{\partial \varepsilon}{\partial t} = \frac{\varepsilon}{k} \left(c_{\varepsilon 1} P + c_{\varepsilon 3} D - c_{\varepsilon 2} \varepsilon \right) + \frac{\partial}{\partial z} \left(\nu_{\varepsilon} \frac{\partial \varepsilon}{\partial z} \right) \\ + \frac{\varepsilon}{k} c_{\varepsilon 1} P_w^{bot}$$
(14)

For these two equations, the Neuman-type boundary conditions taking the waves into account at the sea surface are given by:

$$\frac{\partial k}{\partial z} = \Phi_{oc} \tag{15}$$

$$\frac{\partial \varepsilon}{\partial z} = \left(c_{\mu}^{0}\right)^{\frac{3}{4}} \left[\frac{k^{\frac{3}{2}}}{\kappa \left(z'+z_{0}\right)^{2}} + \left(c_{\mu}^{0}\right)^{\frac{3}{4}} \frac{\frac{3}{2}\sigma_{k}\Phi_{oc}}{c_{\mu}\kappa^{2} \left(z'+z_{0}\right)^{2}}\right]$$
(16)

with $c_{\mu}=0.09$ (Burchard, 2001) and Φ_{oc} the wave to ocean energy flux provided by WW3 accounting for the injection of TKE from breaking waves. Similarly to τ_{wo} , Φ_{oc} is derived from the parameterisation chosen for the dissipation source function in WW3. Note that Φ_{oc} replaces $c_w u_*^3$ from the Craig and Banner (1994) model for the wave enhanced layer in the boundary conditions reported in Burchard (2002). Rather than considering the surface wave TKE contribution as a flux, it could be inputted as a vertically distributed (at the scale of the heights of breaking waves) production term similar to P_w^{bot} . Given the very high mixing there is very little difference between these approaches Rascle et al. (2013).

179 2.3. Case Study

A realistic case study was devised to evaluate the impact of waves on the Ushant tidal front under low to 180 moderate winds. Given the relatively short period over which consistent wind and wave conditions prevail, 181 the simulations were run only for a couple of days. This does not allow for a full tidal decomposition 182 of the results. However, choosing a period in which waves propagate consistently in one direction allows 183 straight forward contrasting of different wave-tide alignments. Models (MARS3D, WW3) were set-up to 184 best represent the conditions measured during the FROMVAR (Front de Marée Variable) field campaign 185 between the 02 and 04 September 2011. An anticyclonic circulation was present at the beginning of the 186 campaign with very weak winds and calm seas. With the arrival of an atmospheric front around 1700 187 UTC on 02 September, southwesterly winds gradually intensified to reach a local maximum of 14 m s^{-1} on 188

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03 September around 1600 UTC. The coupled simulations were started on 02 September at 0600 UTC but
in the following analysis, model outputs are only considered starting at 1200 UTC, allowing for adequate
wave spin up from calm conditions.

192 2.4. Model Configurations

The models were run at high horizontal resolution (500 m for MARS3D and 1500 m for WW3) over a 193 domain spanning about 160 by 160 km^2 (Fig. 1) with hourly outputs. The model configurations chosen 194 are those used for operational purposes as part of the "Modelling and Analysis for Coastal Research" 195 (MARC) project (https://marc.ifremer.fr). A stand-alone MARS3D run (version V11.0 OAW01) was 196 spun up starting January 2011 using a Bay of Biscay configuration with a horizontal resolution of 2.5 km 197 similar to that used operationally for Prévimer (Lazure et al., 2009) (precursor to the MARC project). 198 A fine resolution zoom (500 m) over the Iroise Sea was embedded into the regional grid and integrated 199 through 2-way AGRIF nesting (*Debreu et al.*, 2008). This zoom provided the initial and lateral boundary 200 conditions for the MARS3D simulations used in the present study. Run from 0600 UTC on 02 September 201 2011 to 0000 UTC on 04 September 2011, the stand-alone MARS3D simulation analysed herein gives 202 almost identical outputs to the zoom. The chosen model configuration and forcing were shown to best 203 reproduce the front. Choice of the turbulence scheme was motivated by previous model development 204 (Bennis et al., 2011). 205

MARS3D was forced with tidal components taken from the global Finite Element Solution tide model 206 FES2004 (Lyard et al., 2006) and atmospheric forcing fields consistent with those used to force the Bay of 207 Biscay run. These atmospheric forcing fields come from the operational French forecast model AROME 208 with a temporal resolution of 1 hour and a spatial resolution of $0.025^{\circ}(\sim 2.5 \text{ km})$. AROME provides the 209 following variables to MARS3D: 2-meter air temperature, atmospheric pressure, relative humidity, 10-m 210 zonal and meridional wind components, and cloud cover. Heat fluxes are internally computed based on 211 the NOMADS-2 parameterisation for solar fluxes proposed by Gill (1982), the "EDF" parameterisation 212 for thermal fluxes described in Dumas and Langlois (2009), and COARE 3.0 (Fairall et al., 2003) for 213 the turbulent fluxes. MARS3D operates on an Arakawa C grid with topographically conformal vertical 214 coordinate (σ) system. The vertical resolution was set to 40 σ levels. Figure 3 shows the mean surface 215 (0-30 m) vertical resolution over a tidal cycle. The top sigma level is about 15 cm below the sea surface. 216 Each subsequent sigma level is about 30 cm deep over the top 2.4 m of the water column, then gradually 217 increase in thickness to be around 0.5 m at 5 m below the water line. Surface diagnostics of the current 218 and temperature equations shown in the results section are from the top sigma level while near surface 219

 $k-\varepsilon$ diagnostics are from the top mid-level. The model automatically controls the timestep starting 220 from a maximum timestep of 20 s and a critical Courant-Friedrichs-Lewy (CFL) condition set to 0.6. The 221 QUICK (Kowalik and Murty, 1993) numerical scheme is used for the advection of currents. For tracer 222 (temperature and salinity) a fifth order upwind scheme is used for horizontal advection and an upwind 223 compact and conservative scheme is used for vertical advection (Debreu and Duhaut, 2011). These are 224 employed in a three dimensional two-step MACHO method (*Leonard et al.*, 1996). An implicit scheme is 225 used for vertical diffusion of currents and tracers. The forcing, parameterisations, and numerical schemes 226 chosen correspond to those used in the bay of Biscay configuration which combined with the AGRIF 227 downscaling method allow for the best representation of the Ushant front. 228

In WW3 (adapted from v5.16), the spectral space was discretized using 32 frequencies ranging from 229 0.0373 to 0.7159 Hz in 10% steps $(f_{i+1} = 1.1f_i)$, where i is a discrete grid counter and f the frequency 230 with 24 directions ($\Delta \theta = 15^{\circ}$). The overall timestep was set to 100 s, the spatial (CFL without currents) 231 and spectral (refraction) propagation timesteps to 25 s, and the integration of the source function to 10 s. 232 The physics package used is ST3 which prescribes an f^{-5} spectral tail outside the model frequency range 233 (Bidlot et al., 2005; Tolman et al., 2014). This set of source function parameterizations was chosen for 234 their ability to reproduce the variability in the drag coefficient. For a review of the performances of the 235 different physics packages available see Stopa et al. (2016). The model was started from calm conditions 236 $(H_s=0)$ and forced at the boundaries by 3 hourly energy spectra produced by the HOMERE reanalysis 237 (Boudière et al., 2013) at the open boundaries. The atmospheric forcing for WW3 (zonal and meridional 238 components of the 10m wind) are taken from the AROME fields used to force MARS3D. 239

240 3. Results

The wave impact onto the ocean is analysed by contrasting results of the coupled MARS3D-WW3 run with those of the stand-alone MARS3D run. The following paragraphs focus on the northern extension of the front around a longitudinal transect at 48.8°N as well as the two nearly homogeneous areas Z1 and Z2 located on each side of the Ushant front (see Fig. 1) where the water depth is 116.2 ± 0.97 m and 98 ± 2.2 m, respectively.

246 3.1. Environmental Conditions Simulated

Figure 4 shows time series of the key variables describing the environmental conditions over the simulated period. Average conditions are plotted for the whole domain (black curves) as well as for two equal sized zones, one on either side of the front: Z1 (stratified, red curve) and Z2 (well mixed, blue curve); c.f. Figure 1. As shown below, the tidal signal of the current (rather than the sea level) is central to understand the impact of waves on the front. Throughout the paper, particular attention will be drawn to the relative alignment between current and wave propagation directions. Therefore, periods when waves propagate with (against) the tide roughly corresponding to flood (ebb) or northeastwards (southwestwards) flow are highlighted with coral (blue) shadings on the figures.

The mean winds grow gradually from ~ 3 to $\sim 8 \text{ m s}^{-1}$ between 1200 UTC on 02 September and 1800 UTC on 03 September before decreasing shortly until 2100 UTC and increasing again up to $\sim 9 \text{ m s}^{-1}$ at the end of the simulation (Fig. 4c). A similar pattern is observed in Z1 and Z2, though winds reach a maximum on 03 September of 9.6 m s⁻¹ at 1300 UTC in Z1 and of 8.4 m s⁻¹ at 1800 UTC in Z2. Also, unlike in Z1 or when averaged over the whole domain, winds in Z2 do not increase again after 2100 UTC on 03 September. They blow to the north-northeast throughout the majority of the simulation but for the first and last few hours when average directions display more variability (Fig. 4d).

The tidal cycle as described by the sea level (Fig. 4a), current intensity (Fig. 4e), and direction (Fig. 4f) is semi-diurnal. Three tidal cycles with a tidal range of about 6 m are resolved over the study period starting at low water. The magnitude of the tidal current (Fig. 4e) varies between ~0.4 and ~0.8 m s⁻¹ on average over the whole domain and Z1. This range is intensified near the coast as shown by the temporal averages in Z2 that vary between ~0.2 and ~1.2 m s⁻¹. Currents are the strongest around times of high and low water as is the case for progressive tidal waves.

From 2000 UTC on 02 September, the significant wave height increases from <1 m to ~2 m (Fig. 4b) 268 and its temporal evolution follows that of the wind (Fig. 4c). The main spectral wave peak corresponds to 269 a swell system (see wave periods in Fig. 4b). Waves propagate to the northeast (Fig. 4h) and are roughly 270 aligned with the wind (Fig. 4d). The intensity of the Stokes drift (Fig. 4g) increases as the wind and the 271 waves grow. The wave period is seen to decrease smoothly over time. It does not appear to be influenced 272 by the tide. However, the Stokes drift presents two maxima 0.053-0.076 m s⁻¹ and 0.073-0.1 m s⁻¹ around 273 0200 and 1300 UTC on 03 September, respectively. The Stokes drift appears to be intensified during 274 ebb flow when waves roughly oppose the tidal current (blue shaded periods). The significant wave height 275 also displays local maxima around these times. A decrease in the Stokes drift and in the significant wave 276 height is observed during the two last flood tides of the study period. This aligns with the concept that a 277 wave-opposing current steepens (decrease in mean wavelength, increase in amplitude). A wave-opposing 278 current compresses the wave field while a wave-following current stretches, thus flattens it (Ardhuin et al., 279 2017; *Phillips*, 1984). As the Stokes drift is proportional to the square of the steepness of the waves it 280

282 3.2. Frontal Displacement and the Temperature Equation

The sea surface temperature (SST) front is well represented in both MARS3D runs. It is characterized 283 by a strong SST gradient between 4.9° W and 5.1° W with warm (SST > 15.5 °C) stratified waters offshore 284 and cold (SST < 14 °C) well mixed waters close to the coast (Fig. 1a). The mixed layer whose depth is 285 computed based on a temperature criterion of 0.2° C absolute difference from surface, is around 10-20 m 286 deep on the stratified side and reaches the sea floor on the mixed side (Fig. 1b). Note that computing 287 the mixed layer depth based on a density criterion does not significantly alter the results. Looking 288 at longitude-time Hovmöller diagrams of the SST along the transect at 48.8°N clearly shows the zonal 289 displacement of the Ushant front with the tidal flow (Fig. 5b). As expected, it is seen to advance towards 290 the shore with the flood and retreat offshore with the ebb flow in both the stand-alone and coupled 291 simulations as illustrated in Figure 5b. The zonal displacement at 48.8° N is not in phase with the mean 292 sea level (MSL, Fig. 5a) but rather with the zonal surface current (Fig. 5d) showing how tidal advection 293 drives the front's position. 294

A surface negative temperature anomaly of up to $\sim 1.5^{\circ}$ C in the stratified side (Fig. 5c) is visible in 295 the coupled run compared to the stand-alone run. This cooling is pronounced $(>1^{\circ}C)$ within 2 to 4 km 296 west of the front location in the stand-alone MARS3D run between 0100 and 1800 UTC on 03 September 297 but extends over 10 kilometers further. The differences in temperature and displacement intensify during 298 the simulated period as the waves grow. No clear link is observed between the intensity of the SST 299 response and the tidal cycle. A wave induced cooling can be expected due to wave surface breaking 300 induced mixing (Eqs. 15, 16) which would only have visible impacts on the temperature on the stratified 301 part. However, the analysis of the location of the maximum SST gradient along 48.8°N reveals that this 302 cooling is associated with a westward displacement of the Ushant front. Differences in the surface tracer 303 advecting velocities between the coupled and stand-alone runs are mostly negative around the position of 304 the front (Fig. 5e). This indicates a reduction of the eastward advection and an increase of the westward 305 advection. On the mixed side of the front, the differences are positive indicating an increased advection 306 to the east in line with the Stokes' drift and regardless of tidal phase. On the stratified side of the 307 front, changes in tracer advection are more variable with both positive and negative regions and periods 308 without a clear relation to the tidal phase. The mixed layer depth is seen to reach the sea bottom within 309 a few kilometers west of the SST front as detected in the uncoupled run further hinting at the westward 310 displacement of the front due to waves (Fig. 5f). A deepening of the mixed layer of 5-10 m is also seen 311

throughout the stratified side outside of the frontal region. It intensifies over time and with proximity to the front.

The location of the SST front is obtained based on the maximum values of the SST gradient or mixed 314 layer depth (MLD) obtained by a Sobel filter (*Pringle*, 1969). Its temporal evolution at 48.8°N is shown 315 in Figure 6a. Both types of estimation are consistent between them. The one based on the MLD gives 316 a more regular forehead position that clearly follows the tidal flows. The SST based one appears noisier. 317 When wave-current interactions (coupled run) are modeled, the position deduced from the SST gradient is 318 up to 4 km further west than in the stand-alone run (Fig. 6b). Tracking a specific isotherm such as 14.7°C 319 gives comparable results (not shown). The offset of the position deduced from the maximum gradient 320 of MLD deduced from the coupled and stand-alone runs reaches 3.5 km at the end of the simulation, 321 tracking the SST offset (Fig. 6b). Although results are shown for a specific latitude, the impact of waves 322 is clearly visible all along the Ushant front. As illustrated in Figure 7, the front has similar meanders 323 in the stand-alone (panel a) and coupled (panel b) runs. Mapping the difference in SST between the 324 coupled and the stand-alone run (Fig. 7c) clearly reveals cooling on the stratified side of the front. Some 325 positive differences in SST are visible in the southern extension of the front where meanders are stronger, 326 particularly near the Ushant Island. Presence of the island and shallow bathymetry there complicates the 327 dynamics and wave interactions. 328

Positive salinity and density anomalies accompany the negative surface temperature anomaly on the 329 west side of the front (Fig. 8). The anomalies extend to the MLD on the stratified side of the front 330 without any clear variation of magnitude with depth. Up to ~ 5 m beneath the MLD of the stand-alone 331 run, the anomalies are of opposite sign as can be expected from enhanced mixing. This is accompanied 332 with a deepening of the MLD of $\sim 2-3$ m. No significant differences in temperature and salinity, hence 333 neither in density, are found at depth between the run with or without waves (a full depth version of 334 Figure 8 can be found in Supplementary Materials, c.f. S1). This suggests that only the surface front is 335 impacted by waves under the forcing considered here. The waves impact on the tracer fields is however 336 clearly seen several meters below the mixed layer. 337

Three physical processes could explain the SST cooling and the westward shift of the SST front in the coupled MARS3D-WW3 compared to the stand-alone MARS3D run:

horizontal advection of SST gradient to the west replacing warm stratified waters by cold waters
 from the mixed side of the front;

2. increase of the vertical mixing through additional injection of TKE in ocean due to the presence of
waves;

344 3. changes in vertical entrainment at the MLD bottom bringing cold water up due to wave induced 345 changes in mean vertical velocities.

Changes of vertical entrainment as computed from the vertical velocity using the continuity equation 346 are not significant. The leading order processes driving the temperature evolution are advection and 347 vertical diffusion. Contrasting the budget of the temperature equation of the coupled and stand-alone 348 runs (Eqs. 3 and 11, respectively) allows to determine which of these two processes changes more in 349 response to wave coupling. Figure 9 shows Hovmöller plots at 48.8°N of the different terms of the 350 temperature equation for the stand-alone MARS3D run (panels a and b) and the difference between the 351 coupled wave-ocean and the stand-alone MARS3D runs (panels c to e). The temporal trend term of the 352 stand-alone run is not shown because it is very closed to the total advection term as expected in a tidally 353 dominated environment. Note also that budget terms are hourly averaged rather than instantaneous as 354 in previous figures. The semi diurnal tidal signal is clearly visible in the total advection (Fig. 9a) but not 355 in the vertical diffusion term (Fig. 9b) which is negative on the well mixed side of the front and positive 356 on the stratified side. The plots of differences reveal that the changes in the advective terms (Fig. 9d) 357 are larger around the front than the changes in the vertical diffusion (Fig. 9e). Indeed, the difference 358 in the temperature trend (Fig. 9c) follows that of the total advection revealing cooling near the front, 359 particularly during flood tide. Figure 9e does however clearly show an increase in vertical diffusion on 360 the warm side of the front at times. 361

362 3.3. Current and $k - \varepsilon$ Equations

To further explore the dynamics and energetics responsible for the wave induced changes described 363 above, current and $k - \varepsilon$ equation budgets computed from the coupled and stand-alone runs are compared. 364 Figures 10a,b,d, and e show vertical profiles of the horizontal components of the Eulerian and quasi-365 Eulerian velocities averaged in Z1 (red) and Z2 (blue) for two instants: one when waves and currents 366 are opposed (1200 UTC on 03 September, top row) and one when they follow each other (1800 UTC on 367 03 September, bottom row). The general behaviour on both the stratified (Z1) and mixed (Z2) sides of 368 the front is similar. Currents opposing (following) to wave propagation are found to increase (decrease). 369 The vertical profiles all clearly feature a near surface gradient, although the mean flow is driven largely 370 by barotropic tides. The impact of waves on currents is clearly enhanced near surface but reaches below 371 the MLD which is around 15.3 m and 15.8 m at 1200 UTC and 13.8 m and 14.1 m at 1800 UTC in Z1 372 in the stand-alone and coupled run, respectively. The vertical eddy viscosities (Fig. 10c and f) are seen 373 to increase within the top ~ 10 -15 m of the water column in both cases on either side of the front. The 374

increased mixing leading to reduced vertical gradients can explain the increased (decreased) quasi-Eulerian
velocities in condition of wave-opposing (-following) currents. A positive vertical gradient (shear), likely
due to Ekman dynamics, exists at all times in both the zonal and the meridional velocity components.
The resulting down-gradient turbulent diffusion leads to an increase in magnitude of the upper ocean
velocity when negative and a decrease in the magnitude when positive.

The impact of waves on the magnitude of the near-surface tidal current is further analysed through 380 time series of differences between the magnitude of the quasi-Eulerian current in the coupled run and 381 that of the Eulerian current in the stand-alone run (Fig. 11a). The differences of the current magnitudes 382 averaged over Z1 reach 0.080 ± 0.007 m s⁻¹ during the ebb flow on 03 September at 1200 UTC and -383 0.073 ± 0.010 m s⁻¹ during the rising tide at 1800 UTC on 03 September. This equates to changes in the 384 (quasi-)Eulerian surface current magnitude of up to $\pm 17.5\%$ relative to the Eulerian current magnitude of 385 the stand-alone run in Z1. Changes on the mixed side of the front (Z2) are relatively smaller, amounting 386 to +11% and -16.7%. The differences in the zonal (meridional) (quasi-)Eulerian current components 387 (see Supplementary Material S2 and S3) are for the most part negative indicating that east(north)ward 388 flows are reduced and west(south) ward flows are enhanced. Note that the magnitude of the differences in 389 (quasi-)Eulerian currents is for the most part smaller than the magnitude of the Stokes drift (see Fig. 4g). 390 Indeed, comparing the Lagrangian velocity of the coupled run to the Eulerian velocity of the stand-alone 391 run suggests the Stokes drift tends to compensate the changes in (quasi-)Eulerian currents. It increases 392 (decreases) the wave-following (-opposing) currents by <3% outside of the frontal region, accounting for 393 the positive $\Delta |\mathbf{u}_{\mathbf{L}}|$ on the well mixed side in Figure 5e. However, as shown in Figure 5e, this is not the case 394 in close proximity of the temperature front where the Lagrangian velocity in the coupled run is smaller 395 than the Eulerian velocity of the stand-alone run during flood tides and larger during ebb flow. 396

The analysis of the current equation budget allows to evaluate the main physical balances at play. Given the budget of zonal and meridional currents, it is easy to derive that of the current magnitude. The evolution of the horizontal current follows from Eqs. (1) and (8):

$$\frac{\partial\sqrt{u^2 + v^2}}{\partial t} = \frac{1}{\sqrt{u^2 + v^2}} \left(u\frac{\partial u}{\partial t} + v\frac{\partial v}{\partial t} \right) \tag{17}$$

Note that doing so eliminates the (quasi-)Eulerian Coriolis terms, meaning that the temporal evolution of the current magnitude follows the pressure gradient term at first order (Fig. 11b). Plotting the terms of the equations for the zonal and meridional components (see Supplementary Material S2 and S3) rather than the module clearly shows that the main evolution of the currents is driven from a balance between the pressure gradient and the Coriolis force, i.e. tides. Figure 11b shows the time series of the domain

averaged terms contributing to the evolution of current magnitude. Starting around 2000 UTC on 02 405 September a separation is visible between the terms of the stand-alone (solid curves) and the coupled 406 (dashed curves) MARS3D outputs in both the temporal trend (black curves), the pressure terms (purple 407 curves), and the vertical diffusion term (light blue curves). Note that the addition of the wave induced 408 pressure (J) does not significantly alter the pressure gradient terms. The observed offset between the 409 solid and dashed purple curves reflects differences between the Eulerian current of the stand-alone run 410 and the quasi-Eulerian current of the coupled run. When looking at the zonal and meridional components 411 (Supplementary Material S2 and S3), the change in (quasi-)Eulerian currents is reflected in the (quasi-412) Eulerian Coriolis terms $(if \mathbf{u})$. Time series of the difference between the coupled and the stand-alone 413 MARS3D fields (Fig. 11c) clearly show that as the waves start to grow the Stokes-Coriolis term grows. 414 The difference in trend of the quasi-Eulerian velocity in the coupled run and the Eulerian velocity in the 415 stand-alone run arises from changes in the vertical diffusion term and the Coriolis terms which evolve 416 in opposite phase. The balance described above was verified to hold in average not only over the whole 417 domain, but also in Z1 and Z2. 418

Changes in the vertical diffusion term arise from changes in the surface stress, the vertical shear, and 419 the eddy viscosity (see Eqs. 1 and 8). The surface stress acting upon the ocean (Eq. 10 vs. Eq. 2) is 420 reduced when waves and currents are aligned, but enhanced when opposed, with changes of the order of 421 $\pm 10\%$ relative to τ_a . The near surface shear is reduced regardless of wave-current alignment. The near 422 surface eddy viscosity is enhanced on average by a factor of $\mathcal{O}(10)$ in the coupled run compared to the 423 stand-alone run due to changes in the $k - \varepsilon$ equations (Eqs. 12-16 vs. Eqs. 4-7). As discussed in Section 424 2.2, the surface boundary conditions are modified when wave effects as derived from WW3 model are 425 taken in account. Consequently, the near surface TKE (Fig. 12a) and the dissipation ε (not shown) are 426 seen to increase as the waves grow displaying two maxima similar to the Stokes drift magnitude and H_s . 427

As variations of the TKE dissipation rate largely reflect those of TKE, more insights may be gained by looking at the evolution of the dissipation length scale L derived via the *Taylor* (1935) scaling:

$$L = C_L \frac{k^{3/2}}{\varepsilon} \tag{18}$$

where the proportionality constant $C_L = (c_{\mu}^0)^{\frac{3}{4}} \simeq 0.146$ is derived from the stability function c_{μ} for D =o and $P = \varepsilon$ (see *Burchard*, 2002). While the near surface L in the stand-alone run is nearly constant and equal to 0.24 ± 0.031 m, it increases from 0.23 to 0.48 m when averaged over the whole domain in the coupled run (Fig. 12b), mimicking the evolution of the H_s and the Stokes drift. Note that L in the stand-alone run is directly proportional to z_0 which was set to 0.4 m. This is equivalent to conditions with H_s equal to 0.67 m ($z_0 = 0.6H_s$, following the scaling law proposed by *Terray et al.* (1996) with the

proportionality coefficient of Soloviev and Lukas (2003)) which roughly corresponds to the wave heights 436 at the beginning of the coupled simulation. Note that other scalings of z_0 as a function of H_s can be 437 found in the literature (Rascle et al., 2006), particularly $z_0 = 1.6H_s$ (Terray et al., 2000) which unlike 438 the scaling proposed by Soloviev and Lukas (2003) includes the contribution of swell. Taking $z_0 = 1.6H_s$ 439 increases mixing in the coupled run leading to an unrealistically flat temperature front at the end of the 440 2.5 days simulation. It does however have no substantial impact on the stand-alone run. As z_0 appear 441 in the denominator of the surface boundary condition for ε (Eq. 16), increasing it leads to a reduction 442 in ε and thus an increase in k and L. This in turn further increases the diffusivities, leading to a further 443 deepening of the mixed layer and cooling of the surface. 444

The leading order terms of the near surface TKE budget in both the stand-alone and coupled runs 445 are the vertical diffusion and the TKE dissipation rate (Fig. 13b). These are substantially enhanced 446 in the coupled run. The vertical diffusion term displays a clear tidal variation in the stand-alone run 447 (not shown), varying with current magnitude, being minimum (maximum) an hour before the current 448 maximum (minimum). The tidal signature in the vertical diffusion term is no longer visible in the 449 coupled run. Rather, like the TKE dissipation rate, it increases as the waves growth and the two periods 450 of enhancement are clearly seen in the domain mean time series. The shear production term is seen to be 451 dampened by waves in the near surface k equation (Fig. 13a) as expected from the increased mixing. 452

453 3.4. Analysis of Partially Coupled Runs

In order to better identify the different processes at play, a series of partially coupled model experiments 454 were run. Four partially coupled runs are considered in this section: a run in which all Stokes drift related 455 processes are included in the current and tracer equations (STOKESALLonly), a run where only the Stokes 456 advection terms are included in the tracer equations (STOKESADVonly), a run where only the Stokes-457 Coriolis terms are included in the current equations (STOKESCORonly), and a run where waves are 458 only taken into account in the turbulence closure model (WAVETURBonly). For the first three partially 459 coupled runs, the turbulence equations and surface boundary conditions remain unchanged, i.e. there is 460 no increase in K_u or K_c and the vertical diffusion terms are the same as in the stand-alone MARS3D 461 run. In all the above mentioned runs the vertical boundary condition of the current equations is that 462 of the stand-alone run, i.e. the impact of the waves on the surface stress is ignored. Partially coupled 463 runs where only the stress was changed (not shown) revealed that it does not alter the front position 464 significantly. 465

⁴⁶⁶ Figure 14b shows the cross-front SST at 48.8°N for the partially coupled runs as well as the stand-alone

and the fully coupled runs. The SST curves are centered on the position of the 14.7°C isotherm in the 467 stand-alone run. This snapshot illustrates the relative frontal displacement between the runs once the wave 468 impact is visible. As expected, including only the Stokes advection terms (STOKESADVonly) leads to an 469 eastward shift of the front, in the direction of the wave propagation. Only including the Stokes-Coriolis 470 terms (STOKESCORonly) can have the opposite effect displacing the front westwards as shown for the 471 considered instant. The front remains however to the east of that in the fully coupled run. As mentioned 472 in the previous section, the Stokes-Vortex force has minimal impact: the run STOKESALLonly shows the 473 combined effect of the Stokes-Coriolis force on the current and of the Stokes advection on tracers. It leads 474 to a slight eastward displacement of the front relative to the stand-alone position. The Stokes-Coriolis 475 force can act to increase the eastward displacement along with the Stokes drift, depending on the relative 476 alignment between the currents and wave propagation. These partially coupled experiments suggest that 477 the wave induced mixing is largely responsible for the frontal displacement. Indeed, the frontal position 478 of the WAVETURBonly run follows that of the fully coupled run very closely and is at times even further 479 to the west than in the fully coupled run. Although results in Section 3.1 suggest that for temperature 480 wave induced changes in mixing are less important than wave induced changes in advection, this is not 481 the case for currents. Thus, it is the impact of wave mixing on currents rather than on temperature that 482 is the key process explaining the main difference between stand-alone and coupled runs. 483

Vertical profiles of the (quasi-)Eulerian and Lagrangian velocities along the front (Fig. 14) clearly 484 show strong baroclinicity on the stratified side of the front. Profiles of the zonal and meridional current 485 components display a positive vertical gradient which is more pronounced on the stratified side of the 486 front. Thus, when the flow is positive (negative)/north-eastwards (south-westwards) the flow is stronger 487 (weaker) on the stratified side of the front than on the mixed side. Consequentially, once the front is 488 displaced westwards due to mixing, the surface velocities within several kilometers of the front as identified 489 by the 14.7°C isotherm are homogenised: their intensities have increased when negative and decreased 490 when positive. This shift of regime induced by wave mixing within the frontal area has a greater impact 491 than the changes related to the Stokes drift. 492

493 4. Discussion

The realistic model simulations described above reveal the role of gravity waves in modifying the position of a surface thermal tidal front. Waves propagating shore-ward roughly perpendicularly to the front result in a displacement of the front in the opposite direction of the wave propagation and Stokes drift. This is due to an increase (decrease) of the quasi-Eulerian currents when waves oppose (follow) them which is more important than the Stokes drift around the front. The following paragraphs draw parallels between these results and previous work before exposing avenues for future development and discussing broader implications.

501 4.1. Comparison to Laboratory Experiments

The simulated quasi-Eulerian current response to waves is in line with early laboratory measurements 502 (Bakker and Van Doorn, 1978; Kemp and Simons, 1982, 1983; Klopman, 1994, 1993; Umeyama, 2005). 503 Full depth Eulerian-mean current records show an increase (reduction) in surface currents when opposed 504 (following) to waves compared to the classic logarithmic law of the wall current profiles without waves. 505 These flume experiments were geared mainly towards analysing how waves alter currents in the bottom 506 boundary for different bed roughness. Neertheless, they show systematic changes in the surface currents. 507 They are regularly considered as the "truth" for wave-current interaction model developments although 508 being based on paddle generated non-breaking wave trains which do not have the three dimensionality 509 and spectral spread comparable to real wave fields. It had been argued that the observed wave impact was 510 due to the presence of lateral boundaries which induce Langmuir circulations (*Dingemans et al.*, 1996). 511 However, transverse circulations due to sidewalls were shown to only weakly impact velocity profiles 512 (Groeneweg and Battjes, 2003). 513

The mean velocity shear was also observed to be altered by waves in the aforementioned laboratory 514 records: it increased when waves propagated against the current and decreased or even changed sign when 515 waves and currents propagated in the same direction. Turbulent intensity measurements from Umeyama 516 (2005) suggest that changes in shear were due to the wave-current Reynolds stresses which arise from the 517 phase averaged correlation between the horizontal and vertical particle motion. The sign of the wave-518 current Reynolds stress always opposes that of wave propagation. Thus, for wave-following (-opposing) 519 the current, it is of the opposite (same) sign to the current shear leading to a reduced (enhanced) shear. 520 Wave-current Reynolds stresses are not directly included. As it stands, the coupled framework presented 521 here leads to a reduction of the vertical velocity shear in the surface layer due to the increased wave 522 mixing regardless of the relative alignment between currents and waves. Yet the expected enhancement 523 of the quasi-Eulerian current is reproduced during wave-opposing periods. This is only because mixing 524 homogenises the positive background surface current gradient which exists regardless of waves under the 525 simulated wind conditions. 526

527 4.2. Comparison to Wave-Current Models and Boundary Layer Theories

Several analytical 1D wave-current models and boundary layer theories have been proposed to repro-528 duce the quasi-Eulerian current response observed in the laboratory experiments detailed above. Relying 529 on either the surface distortion of the depth dependent eddy-viscosities (Huang and Mei, 2003), parame-530 terization of wave induced second order stresses (You, 1996), or a mixing length hypothesis (Yang et al., 531 2006) they are capable of roughly replicating measured vertical velocity profiles. More recently, Olabarri-532 eta et al. (2010) proposed a 3D non hydrostatic Eulerian wave-current model using a one equation eddy 533 viscosity turbulence closure able to mimic the current response to waves from the laboratory experiments. 534 They used it to study different wave-current alignments for shallow to deep water waves. Teles et al. 535 (2013) used 3D Reynolds Averaged Navier-Stokes to evaluate how well three turbulent closure schemes 536 could reproduce the conditions measured in laboratory by Umeyama (2005) and Klopman (1994). They 537 concluded that the two first order models $(k - \varepsilon \text{ and } k - w)$ which rely on the eddy viscosity hypothesis do not 538 reproduce laboratory results as well as the Reynolds Stress transport Model (RSM). Teles et al. (2013) 539 however imposed a surface boundary condition to their first order models which forces the eddy viscosity 540 to decrease towards the surface. This is contrary to what is imposed in the realistic simulations presented 541 here where wave coupling leads to a surface enhancement of the eddy viscosity due to the input of wave 542 induced TKE. 543

A fundamental discrepancy between the current work and the laboratory experiments, the theoretical 544 work, and numerical studies discussed so far is in the relative magnitude of the currents and Stokes drift. 545 While in the present study the tidal currents are much faster than the waves, they are of the same order of 546 magnitude in the aforementioned studies. Furthermore, the current work focuses on deep water waves. By 547 contrast, the laboratory experiments, which the previous studies aim to reproduce, featured intermediate 548 depth waves with a ratio of wave height over depth of 0.24 and 0.1 respectively for Klopman (1994) and 549 Umeyama (2005). Consequently only limited comparisons to previous laboratory and analytical works are 550 possible. Numerical development may be necessary to improve the dynamics and kinematics of surface 551 wave-current interactions but dedicated in situ surface current and turbulence profile measurements are 552 also needed for validation. 553

554 4.3. Comparison to Regional Coupled Modelling Studies

Previous realistic coupled modelling studies, which do not include an RSM, reported no substantial impact of waves on currents. Closer inspection of published figures, however, reveals a wave induced change in currents of about 10% in two of them which is of the same order as those reported herein.

These studies were conducted under much stronger wind conditions and weaker currents than those 558 simulated here: one during wind-jet events with wind induced currents (*Ràfols et al.*, 2019), the other in 559 a tidal estuary (Osuna and Wolf, 2005). Using the COAWST modelling system for the north Ebro shelf, 560 $R\dot{a}$ fols et al. (2019) showed that the main impact of waves was on the water column stratification as waves 561 inject turbulent kinetic energy and enhance surface stress thus deepening the mixed layer. Their results 562 indicate differences in surface currents of up to 20 cm s⁻¹ for currents ranging between 20 to less than 80 563 cm s⁻¹ under winds from 10 to 20 m s⁻¹. Osuna and Wolf (2005) reported a daily mean differences of 564 up to 10 cm s⁻¹ during a strong west-southwesterly wave event under winds of 15-20 m s⁻¹ in the shallow 565 coastal areas (with depth around 50 m) of the eastern Irish Sea where the current magnitude is around 566 1 m s⁻¹. This is based on output from the coupled Proudman Oceanographic Laboratory Coastal-Ocean 567 Modelling System-ProWAM framework. It is not possible to determine from the article how the observed 568 enhancement relates to the relative alignment between the tidal currents and the waves. 569

The wave related processes found to be important in the Iroise Sea numerical experiments presented 570 here are: the Stokes-Coriolis force which along with changes in vertical diffusion due to wave injection 571 of TKE and surface stress alter surface currents. In the Irish Sea estuary, only the wave induced surface 572 stress was reported to be key (Osuna and Wolf, 2005). Analysis of the cross-shelf momentum equation in 573 the Ebro simulations revealed a main balance between the pressure gradient and the Coriolis term before 574 wind events, although with wind speeds of 10 m s⁻¹, with all other terms being an order of magnitude 575 smaller ($R\dot{a}$ fols et al., 2019). During wind-jet events in the Ebro region, the vortex force, pressure gradient, 576 surface stress, and horizontal advection were found to be of the same order 4 km offshore, where the water 577 is about 50 m deep. Further offshore, up to tens of kilometers, the vortex force and surface stress were 578 shown to mostly balance the pressure gradient. In the macro tidal regime simulated in the Iroise Sea the 579 wave effect on the horizontal advection and pressure gradient are negligible and under low wind conditions, 580 the vortex force is found to be secondary to other wave processes. Its role in altering the currents and 581 front position under stronger winds has yet to be investigated. 582

583 4.4. Comparison to Remotely Sensed Measurements

The partially coupled simulations reveal that advecting the temperature with the Lagrangian velocity without allowing feedbacks of wave mixing and the Stokes-Coriolis force leads to an eastward bias of the frontal position. The erosion of the temperature front associated with the wave mixing is also shown to be key and explains the westward shift of the front. Joint analysis of hourly satellite derived SST and HF radar derived currents at 48.75°N suggested that the Ushant front is not advected by the Stokes drift

(*Chevallier et al.*, 2014). Estimating the front position from advection based on HF radar derived currents 589 during a period of moderate easterly winds $(5-10 \text{ m s}^{-1})$ led to a westward bias of tens of kilometers after a 590 couple of days. A closer to real estimate of the temporal evolution of the front position by advection was 591 only possible after removal of the Stokes bias (Ardhuin et al., 2009) from the current measurements. A 592 small westward bias is still visible after the Stokes drift correction which may hint to the fact that it does 593 not take into account the impact of surface gravity waves on the quasi-Eulerian currents. The present 594 study suggests that for a more complete correction of the Stokes drift effect in HF radar measurements, 595 the knowledge of the vertical gradients of the horizontal velocity is necessary as well as an estimate 596 of the wave induced mixing. While the finding of *Chevallier et al.* (2014) may suggest that the surface 597 temperature should be advected by the quasi-Eulerian velocity only, the authors ignore the impact of local 598 tidally induced adiabatic mixing which maintains the frontal dynamics. As the tidal residual current in 599 the region is to the north-east, pure advection would lead to an eastward drift of the front which overtime 600 would end up on the coast. This is clearly not observed. The HF radar measurements give the currents 601 within the top tens of centimeters of the water column while the surface frontal signature results from 602 the dynamics of the top tens of meters. Advecting the front by Lagrangian HF radar observations thus 603 overestimates the relative importance of the Stokes drift compared to other wave impacts (mixing) and 604 leads to a front displacement disconnected from mixed layer dynamics. 605

606 4.5. Limitations and Avenues to Improve the Coupled Framework

The impacts of TKE production by Stokes drift and Langmuir turbulence were not included in the 607 present study nor the previously mentioned coastal coupled modeling efforts. As the current horizontal 608 resolution is too coarse to resolve Langmuir circulations (100 m - 1 km) a parameterization would need 609 to be included in the energy equations to take them into account. Several approaches can be envisioned 610 based on previous studies (e.g. Kantha and Clayson, 2004; Harcourt, 2013). Langmuir turbulence has the 611 potential to impact the water column deeper than wave breaking. Thus including it could lead to erosion 612 of the temperature stratification on the offshore side of the front, further contribution to a offshore 613 shift in its location. Another avenue for improving the current framework is to lift the hydrostatic 614 constraint or to include the effects of the Stokes shear force on the pressure term (see Suzuki and Fox-615 *Kemper*, 2016). A higher vertical resolution would also be needed to properly resolve the Stokes shear. 616 As it stands, using the *Breivik et al.* (2014) parameterization for the vertical Stokes drift profiles, the 617 surface Stokes shear is underestimated. In the current framework, the surface current fed to the wave 618 model is that of the top vertical mode. In situations of strong surface current shear it may be more 619 appropriate to consider a vertically integrated current (Suzuki, 2019). The integration depth considered 620

could further be wavelength dependent. This however would add considerable computations. Improving this parameterization, increasing the resolution, and applying the quasi-hydrostatic approach (*Suzuki and Fox-Kemper*, 2016) would increase the impact of the Stokes vortex force. Many uncertainties still surround the other parameterizations on which the framework relies. These include the source functions of the wave model which are used to derive the surface stress felt by the ocean (τ_{surf}) and wave to ocean energy flux (Φ_{oc}) as well as the boundary conditions of the turbulence closure scheme.

627 4.6. Broader Implications

The frontal displacement reaches up to 4 km within 1.5 days as waves propagating into the region 628 grow. Under steady wave forcing one can expect the front to shift until a new equilibrium is reached 629 and wave breaking induced mixing has eroded the surface velocity and temperature gradients. Frontal 630 displacements can be observed repeatedly over periods of a couple of days in a 14 day run with realistic 631 forcing. Note that for the conditions simulated in the present study, low wind and tidal dominated 632 dynamics, the two-way coupling between ocean and waves does not give significantly different results 633 than when forcing the ocean by wave model fields as long as tidal currents were used to produce the wave 634 fields. This was tested by running the coupled framework allowing only wave fields from a stand-alone 635 WW3 run to be sent to the ocean model hourly. Indeed, in the studied situation, the described changes in 636 the (quasi-)Eulerian currents are too small to significantly alter the properties of the swell. Thus, in this 637 particular case coupling is not necessary for either the wave or the ocean components. This may however 638 not be the case in non tidally dominated environments where currents are weaker or under stronger winds 639 or under short fetches as wind-seas are more sensitive to currents. 640

641 5. Conclusions

The current study shows how surface gravity waves alter the location of a surface tidal temperature 642 front. In accordance to previous theoretical and laboratory works, the coupled modelling framework 643 reproduces a reduction (increase) of the surface quasi-Eulerian currents when they follow (oppose) waves. 644 In a situation of mainly eastward propagating waves as in the present case study, the front is advected 645 westwards by up to 4 km due to a reduction in the flooding tide and an increase in the ebb flow. This 646 counter-intuitive impact opposes and over compensates the advection effect of Stokes drift around the 647 front. Note that the situation studied here is not strongly forced by winds and tidal currents are much 648 stronger than the wave induced drift. Yet the impact of waves is clearly detectable. The processes at play 649

are summarized in the diagram in Figure 15. Here horizontal ocean and wave variability on either side of 650 the front are neglected as the resolution is not vet sufficient to properly reproduce them. In the current 651 coupled framework, the main wave dynamics behind the changes in currents are the vertical mixing and 652 the Stokes-Coriolis force which leads to a transport that opposes the Stokes drift. Including wave physics 653 is seen to increase the vertical mixing at the sea surface due to the TKE injection related to wave breaking. 654 This increase in vertical mixing results in a reduction of the surface vertical gradient of the current which 655 is positive for both flood and ebb tides leading to the observed changes in quasi-Eulerian currents. Within 656 the studied environmental setting (strong tidal currents, moderate waves and winds) it appears that only 657 forcing the turbulence closure with a surface wave breaking energy flux is sufficient to reproduce the wave 658 impact produced by the fully coupled framework. In environments which are much more sensitive to 659 the local wind conditions such as upwelling systems or under extreme conditions feedback between the 660 ocean and the waves will have to be taken into account. Before a definite conclusion can be reached on 661 which coupling aspects are necessary for operational use in coastal seas, the coupled model framework 662 will have to be improved further. Both the horizontal and vertical resolutions need to be increased and 663 further development is needed to improve the representation of the Stokes shear and Stokes vortex force 664 and include Langmuir turbulence. Nevertheless, the present study highlights the importance of taking 665 wave-current interactions into account even in environments where the background flow is an order of 666 magnitude stronger than the Stokes drift. Thus, waves should be considered in dispersion studies even in 667 tidally forced coastal seas. The enhanced surface mixing resulting of injection of TKE from wave breaking 668 can significantly vertically homogenize surface tidal currents even under moderate winds. In altering the 669 surface advection, waves can lead to displacements of fronts. Valid in a tidally forced environment, the 670 processes described herein are likely more important where surface currents are weaker. Susceptible to 671 influence the position of any surface temperature front, wave-current interactions could be important in 672 dictating the offshore extent of upwelling systems. The coupled model framework exploited herein would 673 allow studying coupling dynamics and energetics in a wide variety of coastal settings through analysis not 674 only of state variables but also of the terms of the temperature, current, and energy equations. 675

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- waves developed by A.-C. Bennis from which an idealistic test case can be found in *Bennis et al.* (2011).
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Figure 1: Maps of (a) the sea surface temperature (SST) and (b) the mixed layer depth (MLD) from the stand-alone MARS3D ocean model run for 02 September at 1200 UTC. The map in (c) shows the location of the study region denoted by a red box off the coast of Brittany, France. Also shown in (a) and (b) are the model domains and the regions of interest considered in this study.



Figure 2: Diagram showing the variables exchanged between the ocean (MARS3D) and wave (WAVEWATCHIII) models during coupling.



Figure 3: Time series over a tidal cycle of the vertical levels resolved in MARS3D (a) from the sea surface to 5 m and (b) from 5 to 30 m below the sea surface. The solid lines represent levels at which the velocities, temperature, and salinity are evaluated, the dashed lines represent the mid-levels at which the $k - \varepsilon$ equations are evaluated.



Figure 4: Time series of (a) the mean sea level, (b) the significant wave height and period of waves at the spectral peak, (c) the 10-m wind speed, (d) the direction of the 10-m wind in trigonometric convention, (e) the surface current speed from the stand-alone MARD3D run, (f) the direction of the surface current from the stand-alone MARD3D run in trigonometric convention, (g) the intensity of the surface Stokes drift, and (h) the direction of the surface Stokes drift in trigonometric convention. The black line represents an average over the whole domain while the blue and red lines are the averages in Z1 (warm, stratified side of front) and Z2 (cold, mixed side of front), respectively. Shadings around the mean curves correspond to \pm one standard deviation. The light blue and coral shadings demarcate periods of wave-opposing and wave-following currents, respectively.



Figure 5: (a) Time series of the mean sea level along the transect at 48.8°N, between 5.2 and 4.8°W (see Fig. 1), and Hovmöller plots at 48.8°N of (b) the SST from the stand-alone MARS3D run, (c) the SST difference between the coupled MARS3D-WW3 and stand-alone MARS3D runs, (d) the zonal surface velocities from the stand-alone MARS3D run, (e) the difference in zonal surface tracer advecting velocities between the coupled MARS3D-WW3 and stand-alone MARS3D runs, and (f) the difference in mixed layer depths between the coupled MARS3D-WW3 and stand-alone MARS3D runs. The black lines indicate the position of the surface SST front in the stand-alone (solid) and coupled (dashed) runs. The light blue and coral shadings in (a) demarcate periods of wave-opposing and wave-following currents, respectively.



Figure 6: Time series at 48.8°N of (a) the position of the Ushant front based on the maximum gradient in SST (black) and MLD (purple) and (b) the displacement of the front in km based on maximum gradient in SST (black) and MLD (purple). In (a) solid lines correspond to the stand-alone MARS3D run and dashed ones to the coupled MARS3D-WW3 run. The light blue and coral shadings demarcate periods of wave-opposing and wave-following currents, respectively.



Figure 7: Maps of the sea surface temperature from (a) the stand-alone MARS3D run and (b) coupled MARS3D-WW3 run as well as (c) difference between the coupled and the stand-alone runs for 03 September 2011 at 1300 UTC.



Figure 8: Depth vs. longitude transects at 48.8°N of (a) the potential temperature, (b) the salinity, and (c) the density from the stand-alone MARS3D ocean model run. Transects of the difference at 48.8°N in (d) potential temperature, (e) salinity, and (f) density between the coupled MARS3D-WW3 run and the stand-alone MARS3D run. The light grey contours in (b) through (f) are of the potential temperature of the stand-alone run. In pink the mixed layer depth of the stand-alone (solid) and coupled (dashed) runs.



Figure 9: Hovmöller plots at 48.8°N of (a) the advection and (b) the vertical diffusion of the surface temperature diagnosed from the stand-alone MARS3D run, as well as of the differences (coupled - stand-alone) of (c) the temporal trend, (d) the advection, and (e) the vertical diffusion of the surface temperature. The black lines indicate the position of the SST front in the stand-alone (solid) and coupled (dashed) runs.



Figure 10: Vertical profiles of (a, d) the zonal and (b, e) the meridional components of the (quasi-)Eulerian and Lagrangian (dot dashed lines) velocities, as well as (c,f) the tidal eddy viscosities for two periods: 2011-09-03 12:00 (top row) corresponds to a period when waves oppose the tidal flow and 2011-09-03 18:00 (bottom row) to a period where wave and tidal currents are aligned. The red and blue lines correspond to averages within Z1 (warm, stratified side of front) and Z2 (cold, mixed side of front), respectively. Solid lines are from the stand-alone MARS3D run and dashed lines from the coupled MARS3D-WW3 run.



Figure 11: Time series of (a) the differences in the (quasi-)Eulerian surface current magnitude, (b) the terms of the equation for the surface current magnitude (Eqs. 1 and 8 transformed using Eq. 17) averaged over the whole domain, and (c) the differences (coupled - stand-alone) of the terms shown in (b). Note that the horizontal diffusion terms and the wave Bernoulli pressure head are omitted as negligible. In (a) the black line represents an average over the whole domain while the blue and red lines are the averages in Z1 (warm, stratified side of front) and Z2 (cold, mixed side of front), respectively. Shadings around the mean curves in (a) correspond to \pm one standard deviation. In (b) solid lines correspond to the output of the stand-alone run and dashed lines to the coupled run. Wave related terms are represented by the dot-dashed lines. The light blue and coral shadings demarcate periods of wave-opposing and wave-following currents, respectively.



Figure 12: Time series of the near surface (a) turbulent kinetic energy and (b) turbulent length scale averaged over the whole domain (black), Z1 (red), and Z2 (blue) for the stand-alone (solid) and coupled (dashed) MARS3D runs. Shading around the curves represent \pm one stansdard deviation. The light blue and coral shadings demarcate periods of wave-opposing and wave-following currents, respectively.



Figure 13: Time series of near-surface terms of the turbulent kinetic energy equation for the stand-alone (solid lines) and coupled (dashed lines) MARS3D runs averaged over the whole domain. Shown in (a) the trend (black), the shear production (orange), the buoyancy production (light blue), (b) the vertical diffusion (purple), the turbulent kinetic energy dissipation rate (red). The light blue and coral shadings demarcate periods of wave-opposing and wave-following currents, respectively.



Figure 14: (a) Time series of the mean sea level putting the chosen snapshot (2011-09-03 2000 UTC, red dot) into the tidal context. (b) Across front SST transects on 2011-09-03 2000 UTC centered around grid point nearest to the 14.7°C isotherm (grey dashed line) in the stand-alone run. Vertical profiles on 2011-09-03 2000 UTC at several location (0 ± 1 , 3, and 6 km from the grid point nearest to the 14.7°C isotherm in the stand-alone run) within the frontal region of (c) the zonal, and (d) the meridional components of the (quasi-)Eulerian (solid) and Lagrangian (dashed) currents as well as (e) their module. The light blue and coral shadings in (a) demarcate periods of wave-opposing and wave-following currents, respectively.



Figure 15: Diagram illustrating the impacts of shore-wards propagating surface gravity waves on a tidal front and currents. Solid lines represents wave free conditions and dashed lines show the wave induced changes for wave-following/flood (black) and wave-opposing/ebb (blue) currents.

686 5.1. Supplementary material

⁶⁸⁷ Supplementary Figure S1 is the full depth version of Figure 8.

Supplementary Figures S2 and S3 show the terms of the current equation for the zonal and meridional components, respectively, similar to Figure 11.



S 1: Depth vs. longitude transects at 48.8°N of (a) the potential temperature, (b) the salinity, and (c) the density from the stand-alone MARS3D ocean model run. Transects of the difference in (d) potential temperature, (e) salinity, and (f) density between the coupled MARS3D-WW3 run and the stand-alone MARS3D run. The light grey contours in (b) through (f) are of the potential temperature from the stand-alone run. In pink the mixed layer depth of the stand-alone MARS3D run. Also shown are the location of the profiles plotted in Fig. 14 indicated by the purple ticks at the top of each panel. The number indicates the distance from the 14.7isotherm in the stand-alone run.



S 2: Time series of (a) the differences in the (quasi-)Eulerian zonal surface current, (b) the terms of the equation for the surface zonal current averaged over the whole domain, and (c) the differences (coupled - stand-alone) of the terms shown in (b). Note that the horizontal diffusion terms and the wave Bernoulli pressure head are omitted as negligible. In (a) the black line represents an average over the whole domain while the blue and red lines are the averages in Z1 (warm, stratified side of front) and Z2 (cold, mixed side of front), respectively. Shadings around the mean curves in (a) correspond to \pm one standard deviation. In (b) the solid lines correspond to the output of the stand-alone run and the dashed lines to the coupled run. Wave related terms are represented by the dot-dashed lines. The light blue and coral shadings demarcate periods of wave-opposing and wave-following currents, respectively.



S 3: Time series of (a) the differences in the (quasi-)Eulerian meridional surface current, (b) the terms of the equation for the surface meridional current averaged over the whole domain, and (c) the differences (coupled - stand-alone) of the terms shown in (b). Note that the horizontal diffusion terms and the wave Bernoulli pressure head are omitted as negligible. In (a) the black line represents an average over the whole domain while the blue and red lines are the averages in Z1 (warm, stratified side of front) and Z2 (cold, mixed side of front), respectively. Shadings around the mean curves in (a) correspond to \pm one standard deviation. In (b) the solid lines correspond to the output of the stand-alone run and the dashed lines to the coupled run. Wave related terms are represented by the dot-dashed lines. The light blue and coral shadings demarcate periods of wave-opposing and wave-following currents, respectively.

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