
A note on radar signatures of hydrometeors in the melting layer as inferred from Sentinel-1 SAR data acquired over the ocean

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Abstract :

Synthetic aperture radar (SAR) images acquired over the ocean often show radar signatures of rain, which are not easy to interpret. The scattering mechanisms causing radar signatures are usually attributed to surface scattering due to sea surface roughness variations caused by raindrops impinging onto the sea surface and/or by up- and downdraft winds. In this paper, we address another radar signature of rain, which is often observed in C-band (and also in X-band) SAR images, but whose origin has been a matter of debate in the ocean remote sensing community since long time and has not been solved yet. This radar signature consists of areas of very high radar backscatter (bright patches) at co- as well as well as at cross-polarization. This paper aims at providing evidence that it is not caused by surface scattering, but by volume scattering from wobbling, non-spherical, oblate hydrometeors within the melting layer. To this end, we first review the theory of radar backscattering from the melting layer as developed by D'Amico et al. (1998) and then present historic radar backscatter data from the melting layer carried out by ground-based and airborne radars, which validate this theory. Then we show four representative Sentinel-1 SAR images acquired over the sea area close to Hong Kong and a SIR-C/X-SAR image acquired over the Gulf of Mexico, which show pronounced radar signatures of rain (bright patches) at co-polarization (VV) and cross-polarization (VH). The analysis of the SAR images yields the result that within the bright patches the ratio of the radar backscatter at cross-polarization to the one at co-polarization shows the same characteristics as the linear depolarization ratio (LDR) measured by radar meteorologist in radar backscattering from the melting layer. Furthermore, we show that radar signatures of rain due to volume scattering may interfere with co-polarization radar signatures of rain due to surface scattering. Thus, cross-polarization SAR images are better suited to detect radar backscattering from the melting layer than co-polarization SAR images, This investigation is of relevance for ocean surface wind retrieval using C-band SARs, since scattering at hydrometeors in the melting layer can cause significant errors in ocean wind retrieval. Areas with simultaneously high co- and cross-polarization NRCS values of around -10 dB and -20 dB, respectively, have to be flagged as areas where the conventional wind retrieval algorithm cannot be applied.

Highlights

► C-band Sentinel-1 SAR images showing radar signatures of rain cells are analyzed. ► Very strong radar backscattering is observed at co- and cross-polarization. ► They result from scattering at tilted, oblate hydrometeors in the melting layer. ► Sentinel-1 SAR data are compared with data from ground-based and airborne radars. ► Sentinel-1 SAR data are compared with weather radar data from Hong Kong.

Keywords : Rain cells, C-band radar backscatter, Melting layer, Weather radar, Sentinel-1, Cross-polarization, SAR

46 **1. Introduction**

47 SAR images acquired over the ocean, in particular over coastal areas, often show large
48 variability of the backscattered radar power or the normalized radar cross section (NRCS). This
49 variability can have many reasons: It can be due, among others, to variable sea surface winds,
50 variable the air-sea interface stability, variable ocean surface currents, slick coverage, or rain.
51 Identifying and explaining rain signatures in C-band synthetic aperture radar (SAR) imagery
52 acquired over the ocean is a challenging task, since rain can lead to an increase or a decrease of
53 the NRCS (Braun and Gade, 2006; Alpers et al., 2016). The reason is that several physical

54 mechanisms contribute to the rain signature in SAR imagery over the ocean. They are: 1)
55 scattering of the radar pulse from the sea surface, whose roughness is changed by raindrops
56 impinging onto the sea surface, 2) scattering and attenuation from hydrometeors in the
57 atmosphere (volume scattering and attenuation), and 3) scattering from the sea surface whose
58 roughness is modified by rain-related winds, like downdraft or updraft. The first scattering
59 mechanism process is very intriguing since raindrops impinging onto the sea surface can
60 increase the NRCS due to scattering from rain-generated ring waves and from splash products,
61 like stalks, craters, and raindrops emitted from the sea surface. On the other hand, they also can
62 decrease the NRCS roughness due to generation of turbulence, which attenuates the short-scale
63 waves (Bragg waves) responsible for the radar backscattering (Bliven et al., 1993, 1997;
64 Contreras and Plant, 2006; Alpers et al., 2016; Zhang et al., 2016).

65 One outstanding phenomenon often observed in Sentinel-1 SAR images acquired over the
66 ocean are areas of very high radar backscatter, often referred to as bright patches, which are
67 observed when rain is present. The scattering mechanism causing the bright patches has been a
68 matter of debate in the ocean remote sensing community since long time and has not been
69 solved yet. In the past, several scattering mechanisms have been proposed to explain this
70 phenomenon: 1) Scattering at splash products generated by raindrops impinging onto the sea
71 surface (Atlas, 1994a, 1994b), 2) radar pulse reflection from the sea surface followed by
72 scattering at raindrops above the sea surface (Jameson et al., 1997), 3) scattering at low-salinity
73 "puddles" in the upper ocean layer generated by intense rainfall (Wijesekera and Gregg, 1996),
74 and 4) scattering at steep slopes on the rim of the craters produced by impinging raindrops
75 (Braun, 2003).

76 In this paper, we compare Sentinel-1 co-and cross-polarization SAR data with data from
77 radar backscattering measurements carried out by ground-based and airborne radars, and we
78 refer to the theory of radar backscattering from the melting layer as developed by d'Amico et

79 al. (1998). Since the bright patches in the SAR images show similar characteristics as radar
80 backscattering from the melting layer carried out with ground-based and airborne radars, we
81 conclude that the underlying scattering mechanism is the same, i.e., volume scattering from
82 wobbling, non-spherical, oblate hydrometeors within the melting layer.

83 The results obtained in this paper are of relevance for ocean surface wind retrieval using C-
84 band SAR data, since scattering at hydrometeors in the melting layer can cause errors in wind
85 retrieval. When inverting NRCS values in SAR images into wind speed, it is assumed that the
86 backscattered radar power is solely due to surface scattering and receives no contribution from
87 volume scattering. Thus, areas with simultaneously high co- and cross-polarization backscatter
88 values due to volume scattering from the melting layer have to be flagged as areas of corrupted
89 winds. We expect that wind retrieval in tropical storms is especially prone to be affected by
90 volume scattering from the melting layer.

91 The rest of the paper is organized as follows: In Section 2, we review theories and
92 experimental data on radar backscattering from the melting layer. . In Section 3, we present 4
93 representative examples of co- and cross-polarization Sentinel-1 SAR images on which
94 pronounced radar signatures of rain cells are visible and relate them to quasi-simultaneously
95 acquired weather radar images from the Hong Kong Observatory (HKO). In Section 4, we first
96 present a SIR-C/X-SAR image showing the diversity of radar signatures of rain cells and then
97 show how rain-induced surface scattering can interfere with volume scattering from the melting
98 layer. In Section 5, we interpret the data in terms of a theory on radar backscattering from
99 hydrometeors in the melting layer, and in Section 6, we summarize the results and draw
100 conclusions.

101 **2. Radar backscattering from the melting layer**

102 2.1 Basics

103 The melting layer is the layer in the atmosphere, where the irregularly falling ice particles
104 undergo a phase transition from solid to liquid and where the ice particles are coated with liquid
105 water due to meltin (Szyrmer and Zawadzki, 1999). Here, the radar backscatter or reflectivity
106 (Z) is strongly enhanced, which is the result of complex interactions of dynamics and
107 microphysics as described, *e.g.*, by D’Amico et al. (1998) and Szyrmer and Zawadzki (1999).
108 These authors have shown that, due to the horizontal gradients of the buoyancy in the melting
109 layer, the hydrometeors experience tilting (canting) in the melting layer. Scattering of the radar
110 pulse at randomly oriented (wobbling) melting particles causes the large radar signatures at
111 both, co- and cross-polarization. These theoretical results have been validated by radar
112 backscatter measurements carried out with ground-based radars. Although most ground-based
113 radar backscatter mmeasurements aimed at investigating the melting layer have been carried
114 out at co-polarization (see, *e.g.*, Brandes and Ikeda, 2004; Boodoo et al., 2010; Kumjian, 2013),
115 some measurements were also carried out at cross-polarization.

116 As early as 1952, Browne and Robinson (1952) performed cross-polarization measurement
117 with a ground-based radar having a wavelength of 3.2 cm. They found that, at cross-
118 polarization, the backscattered radar power from the “melting layer” was larger than the one
119 from raindrops below and snowflakes above the freezing level. Sometimes, they could detect
120 the melting layer only at cross-polarization, but not at co-polarization.

121 When dealing with detection of melting layers by radars, the following parameters are
122 commonly used by radar meteorologists to determine geometrical and dynamical properties of
123 the hydrometeors.: 1) horizontal reflectivity (Z_{HH}), 2) vertical reflectivity (Z_{VV}), 3) cross-
124 polarization reflectivity (Z_{HV} and Z_{VH}), 4) differential reflectivity (ZDR), 5) linear
125 depolarization ratio (LDR), and 6) cross-correlation coefficient (ρ_{VH} and ρ_{HV}).

126 ZDR , ρ_{VH} , and LDR are defined as follows:

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$$ZDR = 10 \log_{10} (Z_{HH}/Z_{VV}) \quad (1)$$

128
$$\rho_{VH} = \langle Z_{VV}Z_{HH} \rangle / (\langle Z_{VV}^2 \rangle \langle Z_{HH}^2 \rangle)^{1/2} \quad (2)$$

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$$LDR = 10 \log_{10} (Z_{HV}/Z_{HH}) \quad \text{or} \quad 10 \log_{10} (Z_{VH}/Z_{VV}). \quad (3)$$

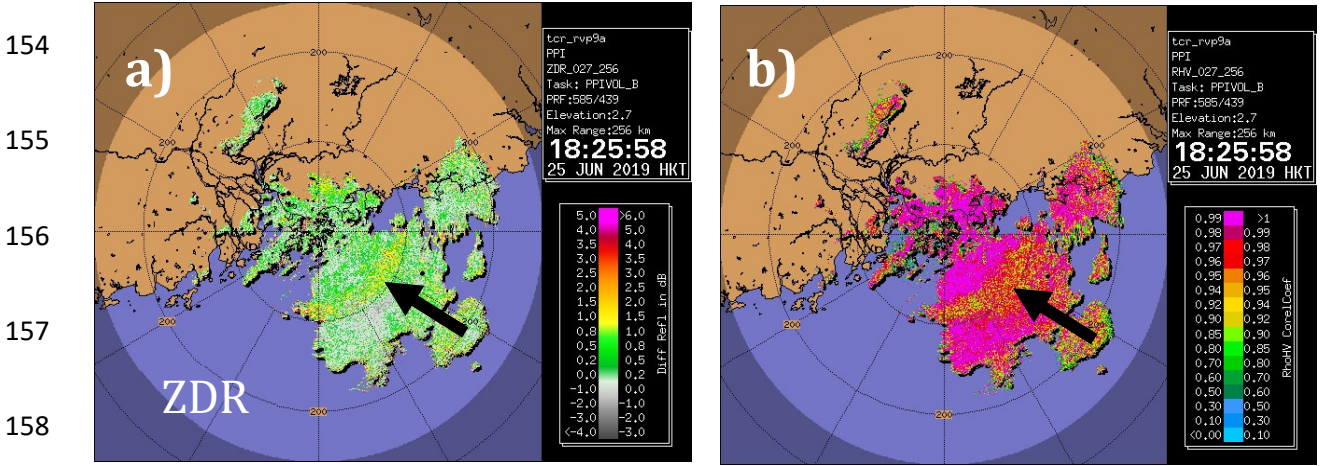
130 The subscripts attached to Z denote the polarization; the first subscript denotes the polarization
 131 of the transmitted signal, and the second one the polarization of the received signal, V = vertical
 132 polarization, H = horizontal polarization.

133 Raindrops have always an oblate shape, i.e., their width is larger than their height and they
 134 have similar shapes as pebble stones found on beaches. The differential reflectivity ZDR is
 135 primarily an indicator of the shape and size of the hydrometeors. The values of ZDR are positive
 136 for scattering from raindrops (typically 1.1 to 1.2, but can be as large as 5.0 for large raindrops).
 137 For scattering from hydrometeors in the melting layer, they are also positive, but usually
 138 slightly larger than for raindrops, and for scattering from ice hydrometeors they are slightly
 139 positive as well as slightly negative (Jameson, 1989). Thus, sometimes the melting layer is not
 140 detectable on ZDR images.

141 On the other hand, the correlation coefficient (ρ_{VH}) is a measure for the similarity of the
 142 radar backscatter in HH and VV polarizations and thus a measure of how uniformly the
 143 scatterers are distributed. As shown by Ryzhkov (2001), ρ_{VH} is a function of the mean canting
 144 angle of the hydrometeors. Its value is normally close to 1.0 for raindrops and snowflakes, but
 145 below 0.95 for hydrometeors in the melting layer.

146 As an example of such measurements, we show in Fig. 1 a ZDR image (Panel a) and a ρ_{VH}
 147 image (Panel b), which correspond to the weather radar image depicted in Fig. 8. The melting
 148 layer can be identified on the ZDR image (Panel a) as a partially circular band with a ZDR
 149 value slightly larger than 1.0 (marked by a black arrow) surrounded by areas with ZDR = 1.0
 150 representing rain in the inner section of the circular band and snow in the outer section. The

151 melting layer can also be identified on the ρ VH image (Panel b) as a partially circular band of
 152 slightly decreased ρ VH values (0.92 - 0.94). Note, that in this case the melting layer is best
 153 visible in the ρ VH image.



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 160 **Fig. 1.** a) PPI image of the differential reflectivity (ZDR) and (b) the correlation coefficient (ρ VH) acquired
 161 by the weather radar of the HKO on 25 June 2019 at 10:25:58 UTC (18:25:58 HKT) quasi-simultaneously
 162 with the Sentinel-1A data acquisition at 10:25:07 UTC (Fig. 8). The arrows mark the melting layer as a
 163 circular band of slightly increased ZDR values and of slightly decreased ρ VH values (0.92 - 0.94),

164 The height H of the melting layer can be calculated from the position of the melting layer
 165 band visible in the ZDR or the ρ VH image by applying the relationship

$$166 \quad H = R \tan \theta + H_0, \quad (4)$$

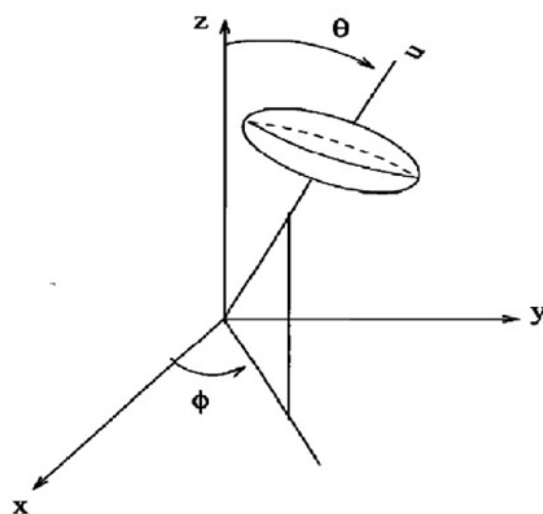
167 where R denotes the distance of the circular melting layer band from the position of the radar, θ
 168 the elevation angle of the radar beam, and H_0 the height of the weather station above mean sea
 169 level. Applied the radar images depicted in Fig. 8 and using the values $R = 90$ km, $\theta = 2.7^\circ$, and
 170 $H_0 = 500$ m in Eq. 4, we obtain for the height of the melting layer the value $H = 4.7$ km. This
 171 lies in the expected range of melting layer heights in this region during strong convective rain
 172 events. We have inserted this melting layer height as a red line in Fig. 8, Panel e. LDR is a
 173 measure of how much larger the cross-polarization (HV or VH) scattering is compared to the

174 co-polarized (HH or VV) scattering. This parameter is not available from the Hong Kong
175 weather radar. At present, operational ground-based radars for weather monitoring provide
176 measurements only at HH and VV polarizations.

177 2.2. Theories of radar backscattering from the melting layer

178 Since the diameter of hydrometeors is small (typically < 0.3 cm) compared to the wavelength
179 of the Sentinel-1 SAR (5.4 cm), the Rayleigh scattering theory can be applied (Oguchi, 1983;
180 d'Amico et al., 1998). In early scattering models (Dissanayake and McEvans, 1989; Willis and
181 Heymsfield, 1989), it was assumed that the hydrometeors have a spherical shape. In this case,
182 a horizontally (vertically) transmitted electromagnetic wave generates a purely horizontally
183 (vertically) backscattered electromagnetic wave. Due to the symmetry of the target, all vertical
184 (horizontal) components of the electric field oscillations cancel and ZDR is zero. The increase
185 of backscattered radar power from the melting layer, which is then due purely to the increase
186 of the dielectric constant.

187 However, the hydrometeors usually have an oblate or a flattened spheroidal shape. They
188 become oblate due to air resistance when falling downwards. In this case, the backscattered



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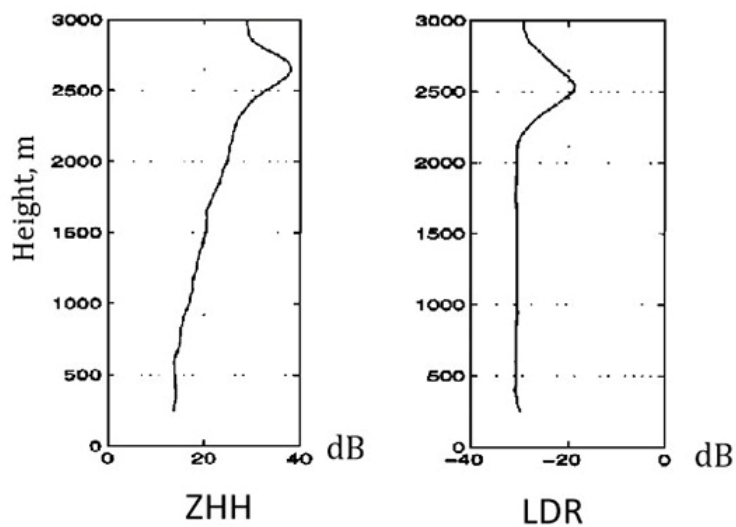
190 **Fig. 2.** Orientation of a spheroidal hydrometeor defined by the direction of its axis of symmetry, \mathbf{u} . The
191 angles θ and Φ denote the canting angle and the azimuth angle, respectively. Reproduced from D'Amico et
192 al. (1998).

193 horizontally and vertically polarized radar signals are different and consequently, ZDR is non-
194 zero. When the long axis of the hydrometeor is aligned horizontally, then the electric field
195 oscillations parallel to the long axis dominate and the horizontal backscattered radar signal
196 becomes larger than the vertical one, i.e., ZDR becomes positive (d'Amico et al., 1998). The
197 larger the raindrops, the more oblate they are, and the larger is ZDR. However, a cross-
198 polarized backscattered radar signal can only occur, when the oblate hydrometeors are tilted
199 out of plane of incidence of the transmitted electromagnetic wave (Fig. 2). The tilting of the
200 elongated hydrometeors is particularly strong in the melting layer due to large horizontal
201 gradients of the buoyancy encountered there. Thus, it is tilting, which gives rise to the large
202 cross-polarization radar signature of rain in the melting layer. If there were no tilting or wobbling
203 of the spheroidal hydrometeors, then there would be no cross-polarization signature due to
204 scattering. (However, there might be a small cross-polarization signature due to differential
205 wave attenuation between horizontal and vertical polarizations). Since the cross-polarization
206 NRCS is always smaller than the co-polarization one, LDR is always negative. Typical LDR
207 values for raindrops and ice particles are -25 to -30 dB and for melting hydrometeors -10 to
208 -20 dB (Houze, 2014).

209 D'Amico et al. (1998) have carried out detailed modeling of cross-polarization radar
210 backscattering from the melting layer. In their model, the hydrometeors in the melting layer
211 consist of ice and liquid water with varying concentrations depending on their height in the
212 melting layer. The oblate spheroidal hydrometeors are subject to tilting with respect to the
213 horizontal. Using this model, they were able to simulate quite well the profiles shown in Fig. 3.

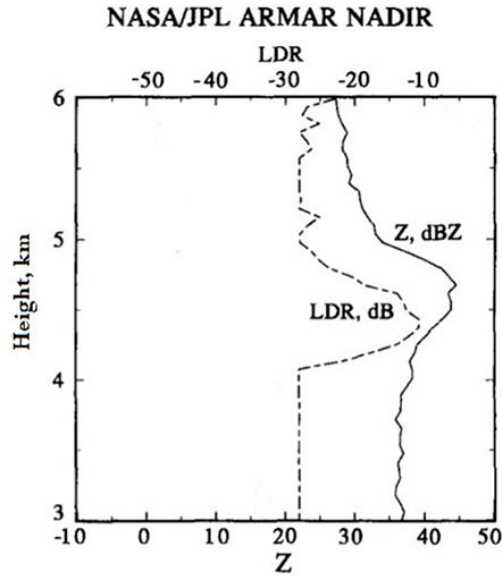
214 *2.3 Ground-based and airborne radar measurements of the melting layer*

215 In this sub- section, we present data of co-and cross-polarization measurements carried out
216 with a ground-based radar and a nadir looking airborne radar, which confirm the theory
217 presented in the previous section. They show that the melting layer manifests itself not only in
218 an increase of the co-polarized reflectivity (in these examples of Z_{HH}), but also in an increase
219 of the cross-polarization reflectivity. The ground-based measurements were carried out by the
220 fully-polarimetric C-band radar of the German Aerospace Center (DLR) at Oberpfaffenhofen,
221 Germany (D’Amico et al., 1998), and the airborne measurements by the NASA/JPL ABMAR
222 airborne RADAR (Jameson et al., 1997). Radar meteorologists usually do not plot the cross-
223 polarization reflectivity, but the linear depolarization ratio (LDR) defined by Eq. 3, which is
224 the ratio of the reflectivity at cross-polarization to the one at co-polarization or in logarithmic
225 scale, the difference between $10 \log Z_{HV}$ and $10 \log Z_{HH}$ (or $10 \log Z_{VH}$ and $10 \log Z_{VV}$), see,
226 e.g., D’Amico et al.,1998. Figs. 3 and 4 show that the reflectivity Z and LDR are strongly
227 enhanced in the melting layer where LDR takes the values are -18 dB (Fig. 3) and -11 dB (Fig.
228 4). Note that in both measurements, the peaks in Z and LDR are not collocated, which is a
229 commonly observed phenomenon, but its explanation is beyond the scope of this paper.



230

231 **Fig. 3.** Vertical profiles (in meters) of Z_{HH} and LDR measured on 17 August 1994 at 1433 LT by the DLR
 232 ground-based radar showing the melting layer in both parameters. The LDR of the melting layer is -18 dB.
 233 Note that the peaks of Z_{HH} and LDR are not collocated. Reproduced from D’Amico et al. (1998).



234
 235 **Fig. 4.** Vertical profiles of Z_{HH} and LDR measured by the NASA/JPL ABMAR airborne radar that flew
 236 over a melting layer associated with a forming tropical cyclone in the Tropical Western Pacific in 1993.
 237 The LDR of the melting layer is -11 dB. Adapted from Jameson et al. (1997).

238 3. Concurrent Sentinel-1 SAR and weather radar measurements of rain cells

239 In this section, we present four representative examples of Sentinel-1 SAR images
 240 showing areas of strong C-band radar backscattering (“bright patches”) at co- and cross-
 241 polarization and compare them with quasi-simultaneously acquired weather radar data of the
 242 HKO. The SAR onboard the Sentinel-1 satellites operates at C-band (5.4 GHz) and has
 243 different exclusive acquisition modes. Here we use only SAR images captured in the
 244 Interferometric Wide (IW) swath mode at VV and VH polarizations (spatial resolution: 20 m
 245 x 22 m, swath width: 250 km, incidence angle range: 29.1° – 46.0°). All images shown in this
 246 section are Level 1 Ground Range Detected (GRD) products provided by ESA via the
 247 Copernicus Open Access Hub (<https://scihub.copernicus.eu>). They were acquired during
 248 ascending satellite passes with the SAR antenna pointing to the right of the satellite track.

249 The Hong Kong (HK) weather radar is a dual-polarization C-band radar with a half-power
250 beam width of 0.5 degrees and has two modes of operation. One is volume scan with scanning
251 at different elevation angles (the lowest one being $\theta = 2.7^\circ$) with a range of 256 km and a repeat
252 cycle of 6 minutes. The other one is horizontal scan with a range of 512 km and a repeat cycle
253 of 12 minutes. The 64 km and 128 km images are derived from the 256 km range data. The
254 weather radar takes measurements at HH and VV polarizations, but not at cross-polarization
255 (VH or HV). Among other products, it provides reflectivity measurements converted into rain
256 rate at a height of 3 km above mean sea level in the Constant Altitude Plan Position Indicator
257 (CAPPI) display. Furthermore, also Plan Position Indicator (PPI) maps are available in real
258 time, from which vertical cross sections of the reflectivity can be generated on demand. The
259 PPI maps shown Panels e are from the 256 km range data.

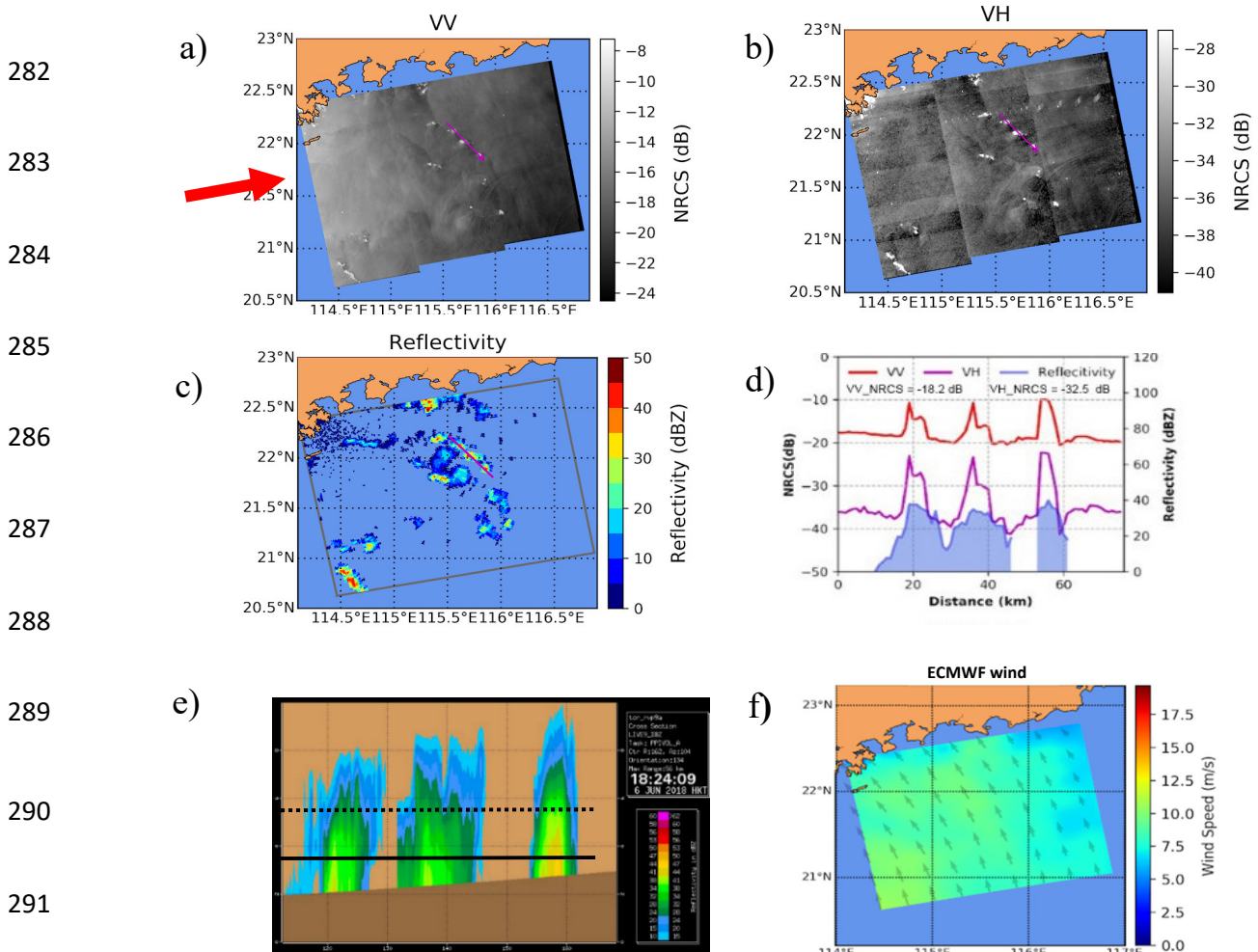
260 For all four rain events presented in this section (Fig. 5 - Fig. 8), we show in Panels a and b
261 VV- and VH- polarization images captured simultaneously by the Sentinel-1 SAR, in Panel c
262 the reflectivity image of the HK weather radar, in Panel d the profiles of the VV NRCS, VH
263 NRCS values and radar reflectivity values along the transects inserted in Panels a, b, and c , in
264 Panel e the reflectivity in the range-height indicator (RHI) presentation along transects shown
265 in Panel c together with the 3 km height line (solid black line) and the zero-degree Celsius
266 height line obtained from radiosonde data (dashed black line), and in Panel f the wind field as
267 provided by the European Centre for Medium-Range Weather Forecasts (ECMWF). Inserted
268 in Panel d are the VV NRCS and VH NRCS values calculated from the background wind
269 adjacent to the bright patches by using the C-band Geophysical Model function CMOD5n
270 developed by Hersbach (2015) for VV polarization and the one developed by Hwang et al,
271 (2015) for cross-polarization.

272 3.1. The 6 June 2018 rain event

273 The SAR images of this event (Fig. 5, Panels a and b) show very pronounced signatures of
 274 three rain cells at VV and VH polarization. The increase of NRCS (relative to the ambient area)
 275 of the three rain cells is about 9 dB in VV and 14 dB in VH polarization (Panel d). The VV
 276 NRCS and VH NRCS values of the highest peaks are -10 dB and -22 dB, respectively, such
 277 that the ratio of VH NRCS to VV NRCS is, in logarithmic scale, -12 dB. Outside these peaks,
 278 the NRCS values lie in the expected range as calculated from the ECMWF wind map using the
 279 C-band geophysical model functions (Fig. 5f).

280 S1A_IW_GRDH_1SDV_20180606T102500_20180606T102529_022235_0267D7_CCF1.SAFE

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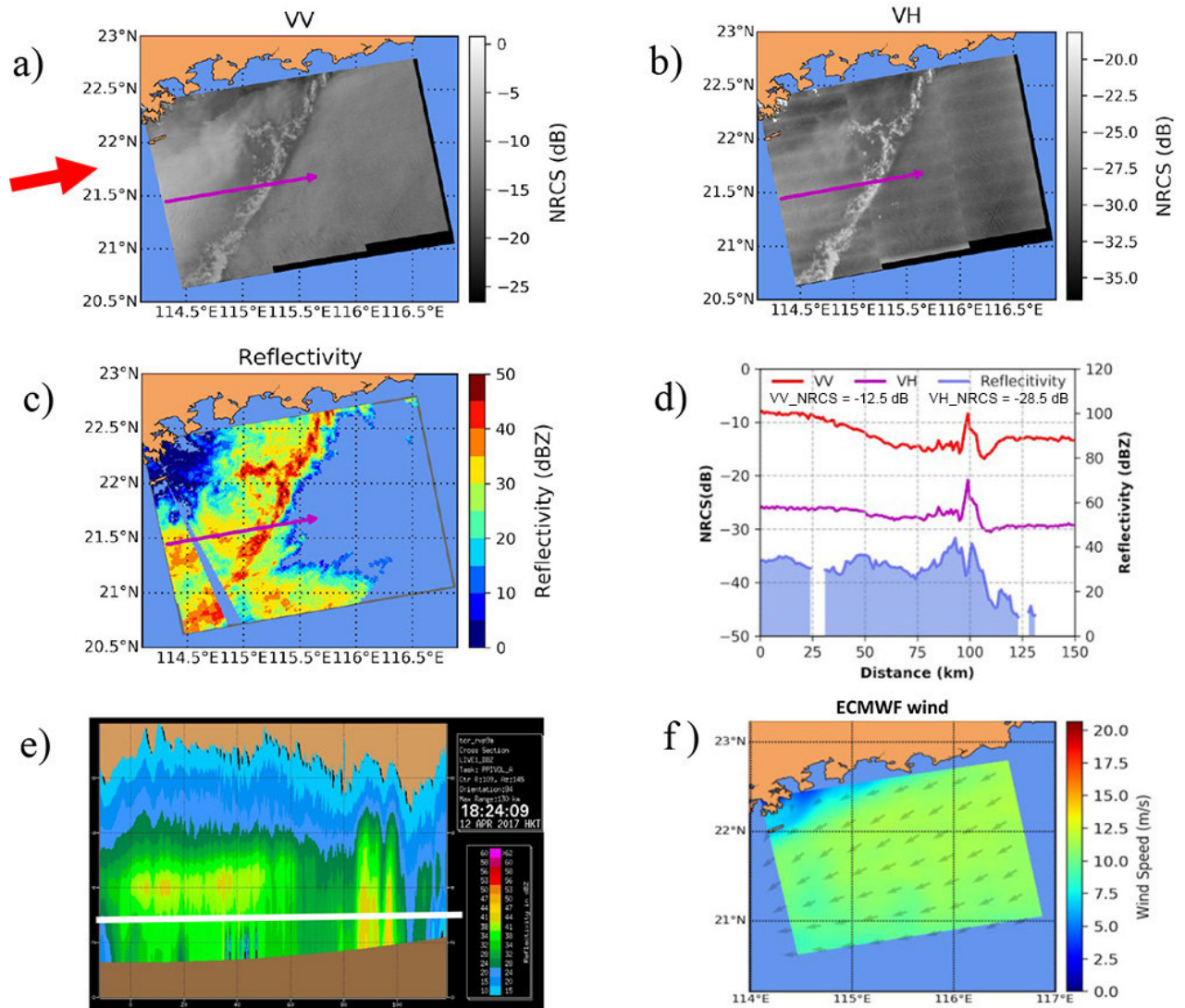
293 **Fig. 5.** Sentinel-1 A SAR images acquired on 6 June 2018 at 10:25 UTC at VV (Panel a) and at VH (Panel
294 b) over the South China Sea off the Hong Kong coast showing radar signatures of a rain band over the sea.
295 The inserted red lines denote the transects along which the variation of NRCS values was measured. The
296 thick red arrow marks the direction into which the SAR antenna is pointing. Panel c shows the CAPPI
297 reflectivity image at a height of 3 km acquired by the HKO weather radar at 10:24 UTC (18:24 Hong Kong
298 Standard Time (HKT)) together with the 3 km height line (solid black line) and the zero-degree Celsius
299 height line (dashed black line). Panel d shows the variation of NRCS in VV and VH as well as the
300 reflectivity measured by the weather radar along the transects inserted in Panels a and b. Inserted are the
301 VV NRCS and VH NRCS values of the background wind field calculated from the wind map (Panel f).
302 Panel e shows in the range height indicator (RHI) presentation the reflectivity along the transect inserted in
303 Panels a and b, and Panel f shows the wind field as provided by ECMWF.

304 *3.2. The 12 April 2017 rain event*

305 The SAR images of this event (Fig. 6, Panels a and b) show a strong rain band extending in
306 the NE-SW direction, which gives rise to pronounced peaks in the VV NRCS and VH NRCS
307 transects. The VV NRCS and the VH NRCS values of the highest peaks are -10 dB and -22 dB,
308 respectively, such that the ratio of VH NRCS to VV NRCS is, in logarithmic scale, -12 dB.
309 However, here the heights of the peaks relative to the background are lower than in the previous
310 event caused by higher ambient winds. A noteworthy feature visible in Panel d is the
311 pronounced dip in the VV NRCS profile to the right (east) of the peak. We interpret it as caused
312 by the decrease of surface scattering due to damping of the short waves (Bragg waves) due to
313 rain-generated turbulence.

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317 **Fig. 6.** Same as in Fig. 5, but for 12 April 2017 at 10:25 UTC (Sentinel-1) and 10:24 UTC (weather radar).

318 *3.3. The 3 September 2017 rain event*

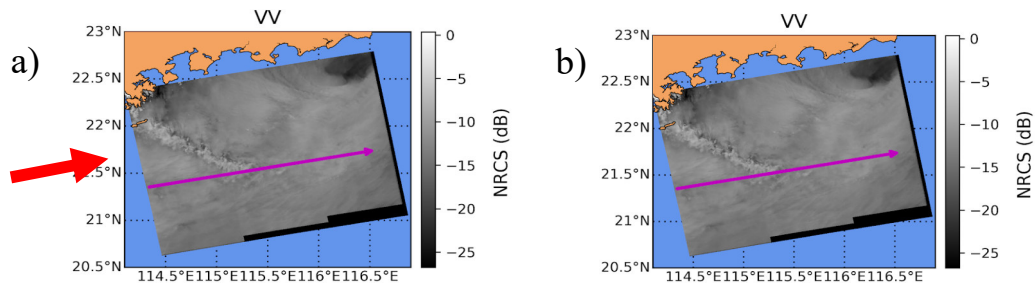
319 The SAR images of this event (Fig. 7, Panels a and b) show a strong rain band aligned in the
 320 NW-SE direction, which gives rise to the peaks in the VV and VH NRCS profiles. The VV
 321 NRCS and the VH NRCS values of the highest peaks are -10 dB and -21 dB , respectively,
 322 such that the ratio of VH NRCS to VV NRCS is, in logarithmic scale, -11 dB. Note that the
 323 weather radar image (Fig. 7, Panel c) shows also rain to the west of this rain band, but the VV
 324 and VH SAR images do not show these strong radar signatures. Here the radar signature of rain

325 is solely due to scattering from the sea surface whose roughness is modified by raindrops
 326 impinging onto the sea surface.

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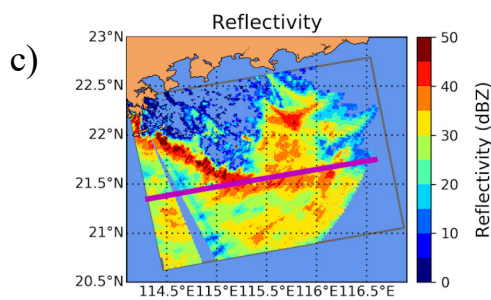
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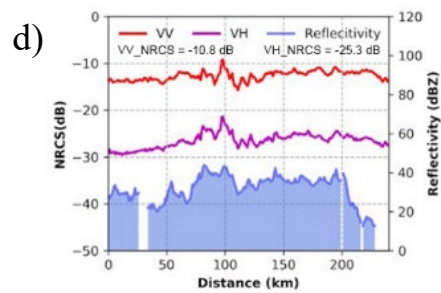
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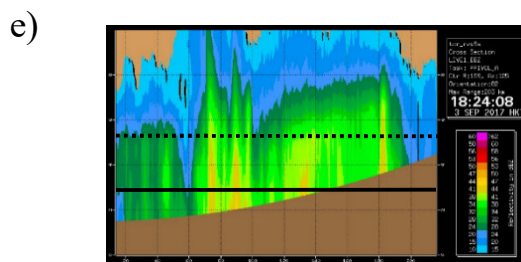
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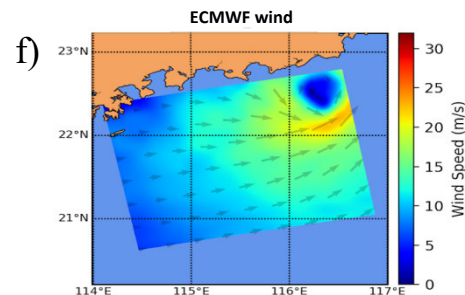
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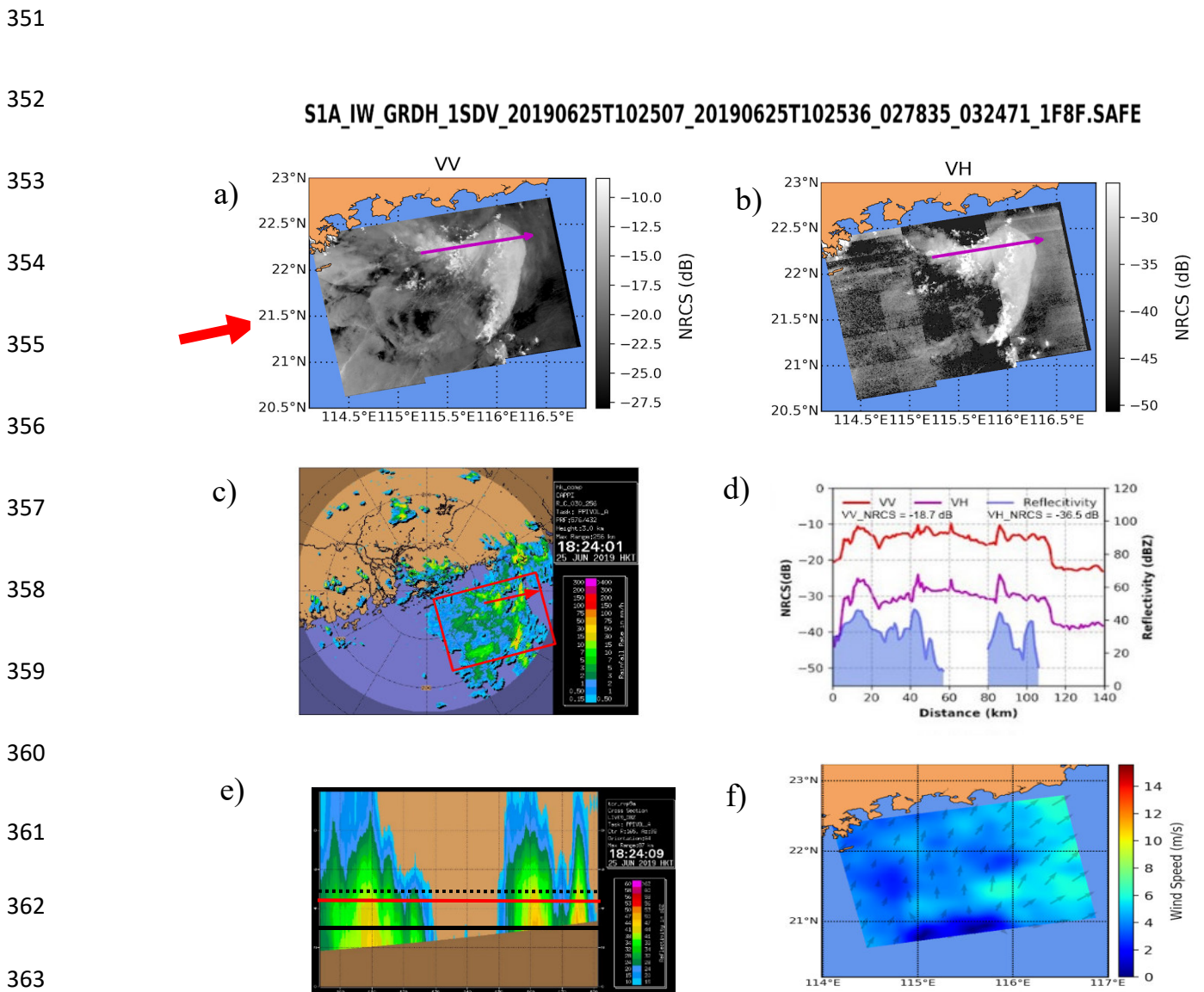


338

339 **Fig. 7.** Same as in Fig. 1, but for 3 September 2017 at 10:25 UTC (Sentinel-1) and 10:24 UTC (weather
 340 radar). This rain event is associated with the tropical storm Marawar.

341 *3.4. The 25 June 2019 rain event* Contrary to the previous SAR images showing rain cells or
 342 rain bands, the SAR images of this event (Fig. 8, Panels a and b) show a strong increase of the
 343 VV NRCS and VH NRCS values in a large area with interspersed peaks. The VV NRCS and
 344 the VH NRCS values of the highest peaks are -10 dB and -23 dB, respectively, such that the

345 ratio of VH NRCS to VV NRCS is, in logarithmic scale, -13 dB. For this event, we were able
 346 to retrieve the height of the melting
 347 layer from the HH and VV polarization data of the Hong Kong weather radar, see Fig. 1. This
 348 height is 4700 m, while the zero-degree height level measured by the radiosonde is 5200 m.
 349 The height difference is due to the fact that melting starts at the zero-degree Celsius height
 350 level, but reaches its maximum at a lower height.



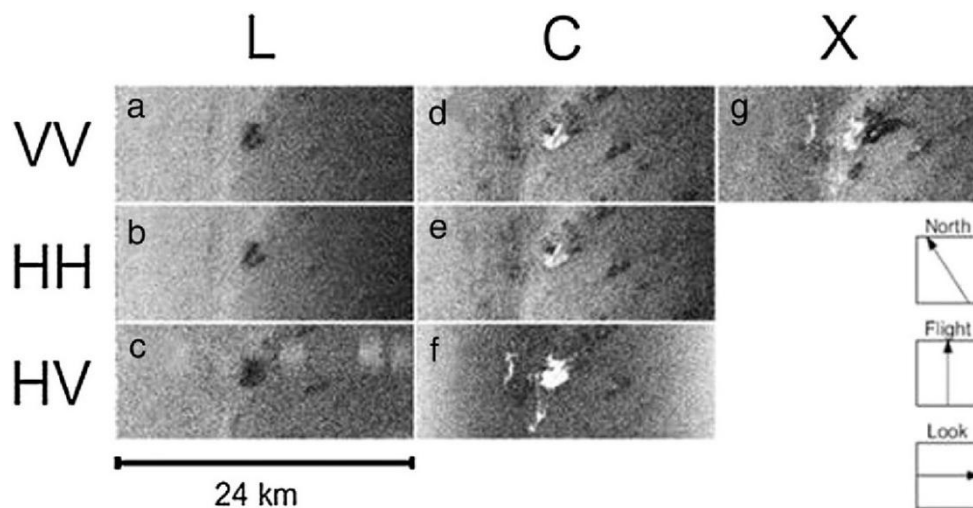
364 **Fig. 8.** Same as in Fig. 1, but for 25 June 2019 at 10:25 UTC (Sentinel-1) and 10:24 UTC (weather radar).
 365 The red line inserted in Panel e denotes the height of the melting layer as inferred from the ZHV and ρ HV
 366 images depicted in Fig. 1. Note that the melting layer is located 500 m below the zero-degree height line.

367 **4. Interplay between volume and surface scattering**

368 As stated before, the backscattered radar signal of Sentinel-1 SAR receives contribution from
369 volume scattering as well as from surface scattering. This can give rise to significant distortions
370 of the theoretically expected radar signature of a rain cells due to volume scattering as evident
371 in the Sentinel-1 SAR image depicted in Fig. 6. To further illustrate this complexity, we show
372 in Fig. 9 simultaneously acquired multi- polarization/multi-polarization SAR images with rain
373 cells from the SIR-C/X-SAR mission in 1994 (Melsheimer, 1998). These images clearly show
374 the strong variability of radar signatures of rain cells with radar frequency and polarization as
375 stated in the Introduction. For L-band, the radar signal penetrates the melting layer almost un-
376 attenuated and therefore, the L-band radar signature of the rain cell has its origin almost
377 exclusively in surface scattering. The black patch in the center of the L-band images is due to
378 impinging raindrops, which generate turbulence in the upper ocean layer and attenuate there
379 the L-band Bragg waves. When comparing the C-band VV and HH images with the HV image,
380 we see that rain cells have a higher contrast in the VH image than in the VV and HH images.
381 The reason is that the background C-band NRCS due to wind-induced surface scattering is in
382 the VH image much smaller than in the VV and HH images. Furthermore, we also note that for
383 C-band, the size of the bright patch is smaller in the VV and HH images than in the HV image
384 and that there is a small dark patch adjacent to the bright one in the HH/VV images. We interpret
385 it as caused by the superposition of volume scattering and surface scattering: In the bright area,
386 the increase of the NRCS induced by volume scattering at hydrometeors in the melting layer is
387 dominant, and in the dark area, the attenuation of the Bragg waves is dominant due to rain-
388 generated turbulence, thereby inducing the reduction of the NRCS.

389 Another remarkable feature visible in Fig. 9 is the small bright band located west of the large
390 bright patch in the center, which is visible only in the CHV image, but not in the XVV image
391 nor in the CVV and CHH images. We interpret this feature as a radar signature of a small rain

392 band in the melting layer, which is less strong than the signature of the large rain cell located
 393 in the center of the CHV image (see Fig. 9 f). This signature is not visible in the CHH and CVV
 394 images, because its NRCS value is much smaller than the NRCS of the background due to high
 395 winds. This suggests that cross-polarization is better suited for detecting scattering from the
 396 melting layer than co-polarization, because it receives less contribution from surface scattering,
 397 and therefore the signal-to-noise ratio is higher. Note, that this small rain band is also visible in
 398 the L-band VV /HH images as a faint dark band, which has its origin in the damping of Bragg
 399 waves by the rain-generated turbulence.



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402 **Fig. 9.** SIR-C/X-SAR images acquired at L-, C-, and X-band simultaneously over the Gulf of Mexico at
 403 08:11 UTC on 18 April 1994, displaying the strong dependence of the radar signature on radar frequency and
 404 polarization (reproduced from Alpers et al., 2016). Note, in particular, the difference in the rain signature
 405 patterns of the rain cell in the CVV/CHH and CVH images, which are due to superposition of volume and
 406 surface scattering in the CVV and CHH images.

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408 Fig. 10 a shows a zoom of the CVH image depicted in Fig. 9 f with a transect line inserted
 409 along which the ratios HV NRCS/HH NRCS and VH NRCS/VH NRCS, termed LDR_{SAR} (see
 410 Eq. 5) are measured. However, plotted in Fig. 10 a is $-LDR_{SAR}$. The LDR_{SAR} values of the bright

411 patch are -15 dB for HV/ HH and -16 dB for VH/VV. This shows that LDR_{SAR} depends very
412 little on the polarization of the incident pulse.

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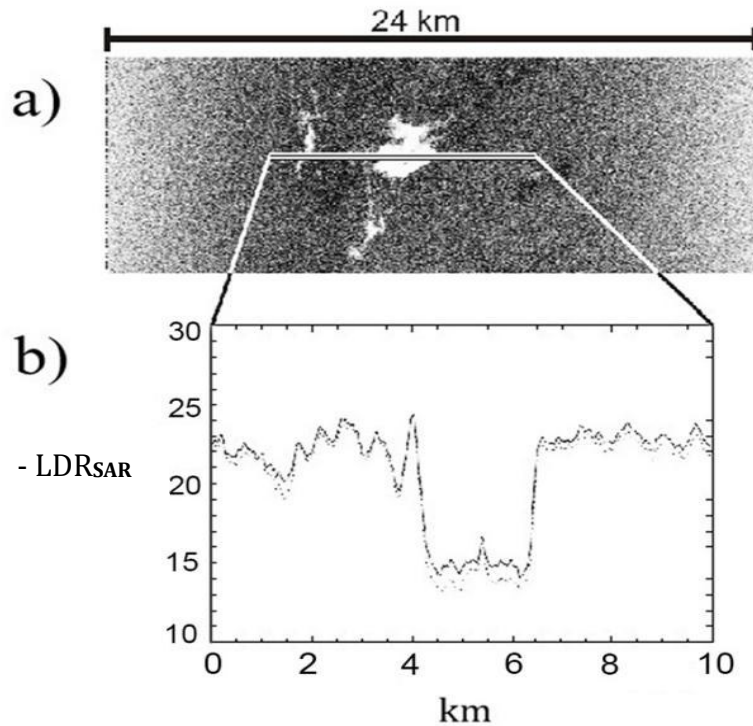
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425 **Fig. 10.** a) Section of the CHV SAR image shown in Fig. 9 f; b) Ratio of the NRCS values at HH and HV
426 polarizations (solid line), and at VV and VH polarizations (dashed line). Reproduced from Braun (2003).

427

428 Panel a of Fig. 11 shows schematically how a rain cell is imaged when volume scattering and
429 rain-related surface scattering are involved, Panel b shows the backscattered radar pulse due to
430 volume scattering from hydrometeors in the melting layer and Panel c the one due to surface
431 scattering, where, in this case, the backscattered radar power is reduced due to damping of the
432 Bragg waves by rain-induced turbulence. For co-polarization, often both scattering mechanisms
433 contribute such that the backscattered pulse attains the form shown in Panel d. For cross-
434 polarization, rain-related surface scattering contributes only very little to the total radar
435 backscattering, such that the backscattered pulse attains the form shown in Panel b. This

436 scattering geometry applies to the rain event of 12 April 2017 (Section 3.2,) where, in the VV
 437 image (Fig. 6 a), the radar signature of the rain band consists of a bright band followed by a
 438 dark band, while in the VH image it consists only of a bright band, see also the NRCS profiles
 439 depicted in Fig. 6 d.

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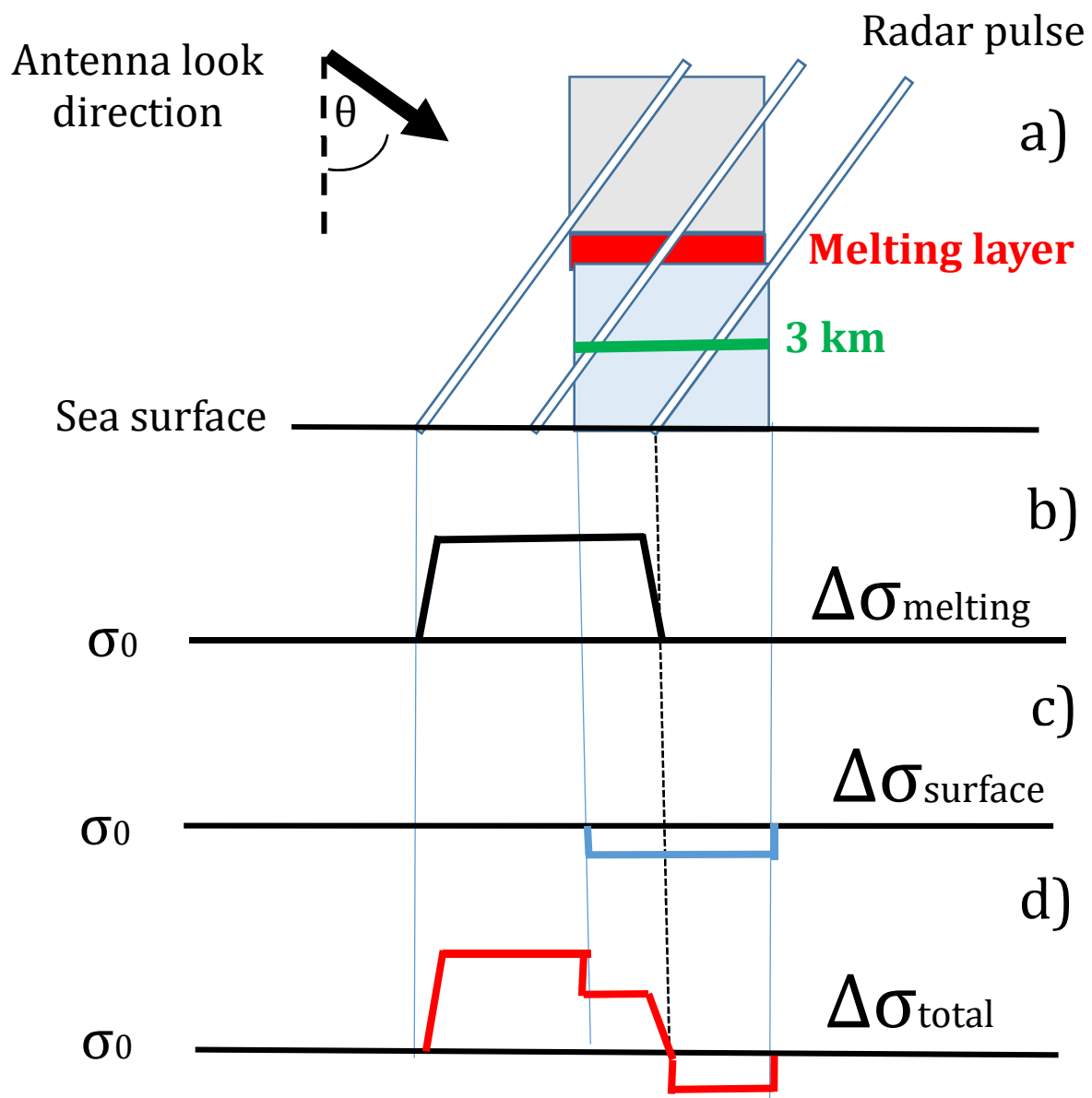


Fig. 11. a) Scattering geometry of a rain cell imaged by SAR with look direction from the left. The red
 rectangle denotes the melting layer and the green line denotes the height at which the weather radar

464 measures the reflectivity, b) Form of the backscattered radar pulse due to volume scattering from the
465 melting layer. c) Form of the backscattered radar pulse due to rain-modified surface scattering, which, in
466 this case, is reduction of the backscattered radar power due to wave damping by rain-generated turbulence.
467 d) Form of the backscattered radar pulse due to both effects. The inset σ_0 denotes the background
468 backscattered radar power and $\Delta\sigma$ the deviation from the background.

469

470 **5. Interpretation of the data**

471 The analysis of the quasi-simultaneously acquired Sentinel-1 SAR images and weather radar
472 data presented in Section 3 show that the bright patches visible in the Sentinel-1 SAR images
473 are related to rain cells (Fig. 5), rain bands (Figs. 6 and 7), or larger rain areas (Fig. 8). Note that
474 the weather radar images depicted in the Panel c of Figs. 5 – 8 show the radar reflectivity at a
475 height of 3 km, while the melting layer lies above this height. The height of the melting layer
476 can be estimated from the height of the zero-degree level, which usually is located few hundred
477 meters higher than the center of the melting layer. In one case, in the 25 June 2019 event
478 (Section 3.4), we were able to determine the height of the melting layer from weather radar data
479 of the HKO (see ZHV and ρ HV images depicted in Fig. 1). Panels e of Figs. 5 - 8 show that
480 during all four rain events hydrometeors were present in the melting layer. Panels d of Figs. 5
481 - 8 show that the peaks in the VV NRCS and VH NRCS profiles are highly correlated. In
482 addition, peaks in the SAR NRCS profiles are also correlated reasonably well with peaks in the
483 reflectivity profiles obtained from CAPPI weather radar data. (Note, that the radar signatures
484 of the rain cells in the Sentinel-1 SAR images and in the CAPPI displays refer to different
485 heights, i.e., the melting layer height and the 3 km height, respectively). Furthermore, the height
486 of the peaks relative to the background is always higher at VH polarization than at VV
487 polarization. The VV NRCS peak values range from -9 dB to -10 dB, and the VH NRCS peak
488 values from -20 dB to -24 dB.

489 In order to prove that the bright patches visible in Sentinel-1 SAR images are due to volume
 490 scattering from hydrometeors in the melting layer, we compare the SAR data with data from
 491 radar backscattering measurements from the melting layer carried out with ground-based and
 492 airborne radars. For this comparison, we employ the parameters LDR and LDR_{SAR} , where
 493 LDR denotes the Depolarization Ratio, defined by Eq. 3, which is used by radar meteorologists
 494 to localize the melting layer, and LDR_{SAR} , which we define by:

$$495 \quad LDR_{SAR} = 10 \log_{10} (\sigma_{VH}^{total} / \sigma_{VV}^{total}) \quad \text{or} \quad LDR_{SAR} = 10 \log_{10} (\sigma_{HV}^{total} / \sigma_{HH}^{total}) \quad (5)$$

496 Here σ^{total} denotes the sum of the NRCS due to volume scattering, σ^{volume} , and the NRCS
 497 due to surface scattering, $\sigma^{surface}$:

$$498 \quad \sigma^{total} = \sigma^{surface} + \sigma^{volume} \quad (6)$$

499 The subscripts denote the polarizations for transmission in analogy to the definition of LDR
 500 (Eq. 3). When calculating σ^{total} from the backscattering data, one has to correct for the
 501 attenuation of the radar pulse when it propagates through the melting layer and through the
 502 layer above containing frozen hydrometeors (-snowflakes) and the layer below containing liquid
 503 hydrometeors (rain drops). However, while for X-band, attenuation is a major effect (see, e.
 504 g., Danklmayer et al., 2009), it is a minor effect for C-band as long as the rain rate is not too
 505 high (< 20 mm/h) (Tounadre and [Morland](#), 1997). E.g., when using the empirical aR^b relation
 506 of Olsen et al. (1998) for calculating the attenuation, one obtains for a 5 km thick rain cell with
 507 rain rate of 30 mm/h an attenuation of 1.3 dB. In this investigation, we neglect attenuation, since
 508 it has no effect on our result on the nature of the scattering mechanism.

509 In all Sentinel-1 SAR images presented in Figs, 5 – 8, volume scattering is the dominant
 510 scattering mechanism in the bright patches. The contribution of surface scattering to the total
 511 scattering is particularly small in the events of 6 June 2018 (Fig. 5) and of 25 June 2019 (Fig.

512 8): -20 dB versus -10 dB and -23 dB versus -10 dB. Thus, in these cases, the contribution from
513 surface scattering can be neglected in LDR_{SAR} such that it contains, like LDR, only
514 contributions from volume scattering, We now compare LDR_{SAR} values measured in then bright
515 patches with LDR values measured in radar backscattering from the melting layer by using
516 ground-based and airborne radars. In these cases, LDR_{SAR} has peak values in the bright patches
517 of -12 db and -13 dB, which compare well with LDR values characterizing the melting layer
518 (see Section 2,3). Furthermore, the SIR-C/SAR data presented in Section 4 (Fig. 10 b) show
519 LDR_{SAR} values of -15 dB and -16 dB for horizontally and vertically polarized transmitted
520 signals, respectively, which also lie in the range of LDR values characterizing radar backscatter
521 from the melting layer as measured by ground-based and airborne radars. Thus. we conclude
522 that the scattering mechanisms causing the bright patches in the SAR images and the high LDR
523 values in radar backscattering measurements from the melting layer, must be the same, i.e., the
524 scattering mechanism is volume scattering from wobbling, non-spherical, oblate hydrometeors
525 within the melting layer.

526 **6. Summary and conclusions**

527 In this paper, we have provided evidence that the scattering mechanism causing the large
528 radar backscatter values at co-and cross-polarization often observed in Sentinel-1 SAR images
529 of the sea surface in the presence of rain (“bright patches”) is scattering from wobbling, non-
530 spherical, oblate hydrometeors within the melting layer. In the past, several other scattering
531 mechanism have been proposed, which are all based on the modification of the sea surface
532 roughness due to rain drops impinging onto the sea as described in the Introduction. In a recent
533 review paper dealing with rain footprints on C-band SAR images of the ocean (Alpers et al.,
534 2016), it was stated in the Conclusion section: “The scattering mechanism causing the bright
535 patches in C-band, co-polarized SAR images of rain cells could not be determined”. In this
536 paper, we have identified the scattering mechanism by comparing Sentinel-1 co-and cross-

537 polarization SAR data with data obtained from radar backscattering measurements from the
538 melting layer carried out with ground-based and airborne radars. We have calculated the ratio
539 of the NRCS values at co- and cross-polarization in the bright patches in the SAR images
540 (LDR_{SAR}) and compared them with the ratio of the radar reflectivity at cross-and co-polarization
541 (LDR values) measured in radar backscattering experiments from the melting layer using
542 ground-based and airborne radars. Since both ratios have similar values and since it is known
543 that the last one (LDR) characterizes the melting layer, we conclude that the bright patches are
544 caused by scattering from the melting layer. In this context, we would like to mention that such
545 scattering mechanism was already suspected by Katsaros et al. (2000) who analyzed co-
546 polarized Radarsat-1 C-band data of the hurricane Danielle in 1998 and noticed small white
547 spots within a rain cell, which they then compared them passive microwave data from the
548 Special Sensor Microwave/Imager (SSM/I) onboard DMSP satellites. They suspected that the
549 white spots result from “randomly oriented ice particles in th cloud”. We know of no paper in
550 which this idea, i.e., the comparison of C-band SAR with passive microwave data, was pursued
551 further.

552 When screening C-band co-polarization SAR images for radar signatures caused by
553 scattering from the melting layer, one must be aware of the fact that they are sometimes
554 distorted by overlapping radar signatures due to rain-induced surface scattering, as evident in
555 the SIR-C/X-SAR CHH and CVV images (compared to the CHV image) shown in Fig. 9. This
556 suggests that cross-polarization SAR images are better suited to detect radar signatures of the
557 melting layer than co-polarization SAR images. Furthermore, we conclude from Fig.10 b that
558 HH and HV C-band SAR images show similar characteristics of radar scattering from the
559 melting layer as VV and VH SAR images. The analysis of C-band co-and cross-polarization
560 Sentinel-1 SAR images presented in this paper suggests the following semi-quantitative
561 criterion for identifying areas on Sentinel-1 SAR images of the ocean surface as being caused

562 by radar scattering from hydrometeors in the melting layer: VV NRCS must have values around
563 -10 dB or larger and VH NRCS values around -20 dB, such that LDRSAR has values between
564 -15 dB and -10 dB. We expect this criterion to be applicable for incidence angles between 30
565 and 70 degrees and for wind speeds below 20 m/s. The identification of areas in C-band SAR
566 affected by scattering from the melting layer is of relevance for ocean surface wind retrieval
567 using C-band SARs, since in these areas the conventional wind retrieval algorithm is not
568 applicable.

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576 **References**

- 577 Alpers, W., Zhang, B., Mouche, A., Zeng, K., Chan, P.W., 2016. Rain footprints on C-band synthetic
578 aperture radar images of the ocean - Revisited. *Remote Sens. Environ.* 187, 169-185.
579 doi:10.1016/j.rse.2016.10.01516/j.rse.2016.10.015
- 580 Atlas, D. A., 1994a. Footprints of storms on the sea: a view from spaceborne synthetic aperture radar, *J.*
581 *Geophys. Res.* 99, 7961-7969. doi:10.1029/94jc00250
- 582 Atlas, D. A., 1994b. Origin of storm footprints on the sea by synthetic aperture radar. *Science* 266, 1364-
583 1366. doi:10.1126/science.266.5189.1364

584 Bliven, L., Branger, H., Sobieski, P., Giovanangeli, J.-P., 1993. An analysis of scatterometer returns
585 from a water surface agitated by artificial: evidence that ring-waves are the main feature. *Int. J.*
586 *Remote Sens.* 14, 2315–2329. doi:10.1080/01431169308954039

587 Bliven, F., Sobieski, P.W., Craeye, C., 1997. Rain generated ring-waves: measurements and modelling
588 for remote sensing. *Int. J. Remote Sens.* 18, 221–228. doi: 10.1080/014311697219385

589 Boodoo, S., Hudak, D., Donaldson, N., Leduc, M., 2010. Application of dual-polarization radar melting-
590 layer detection algorithm. *J. Appl. Meteorol. Climatol.* 49, 1779-1793.
591 doi:10.1175/2010jamc2421.1

592 Brandes, E.A., Ikeda, K., 2004. Freezing-level estimation with polarimetric radar. *J. Appl. Meteor.* 43,
593 1541-1553. doi:10.1175/jam2155.1

594 Braun, N., 2003, Untersuchungen zur Radar-Rückstreuung und Wellendämpfung beregneteter
595 Wasserober flächen. Ph.D. thesis, University of Hamburg, Germany, Shaker Verlag, Aachen,
596 Germany.

597 Braun, N., Gade, M., 2006. Multifrequency scatterometer measurements on water surfaces agitated by
598 artificial and natural rain, *Int. J. Remote Sens.* 27, 27-39. doi: 10.1080/01431160500239214

599 Browne, I.C., Robinson, N.P., 1952. Cross-polarization of the radar melting-band. *Nature* 170, 1078-
600 1079.

601 Contreras, R.F., Plant, W.J., 2006. Surface effect of rain on microwave backscatter from the ocean:
602 Measurements and modeling. *J. Geophys. Res., Oceans* 111(C8). doi:10.1029/2005JC003356

603 D'Amico, M.M., Holt, A.R., Capsoni, C., 1998. An anisotropic model of the melting layer. *Radio Sci.*
604 33, 535-552. doi: 10.1029/97rs03049

605 Danklmayer, A., Döring, B.J., Schwerdt, M., Chandra, M., 2009. Assessment of atmospheric
606 propagation effects in SAR images. *IEEE Trans. Geosci. Remote Sens.* 47, 3507–3518. doi:
607 10.1109/TGRS.2009.2022271

608 Dissanayake, A. W., McEvans, N. J., 1978. Radar and attenuation properties of rain and bright band.
609 IEEE Conf. Publ. 169, 125-129

610 Hwang, P., Stoffelen, A. A., van Zadelhoff, G.-J., Perrie, W., Zhang, B., Li, H., Shen, H., 2015. Cross-
611 polarization geophysical model function for C-band radar backscattering from the ocean surface
612 and wind speed retrieval, *J. Geophys. Res. Oceans*, 120, 893–909. doi:10.1002/2014JC010439

613 Houze, R. A., 2014. *Cloud Dynamics*, International Geophysics, vol, 104, Elsevier, Amsterdam, ISBN:
614 9780123742667

615 Jameson, A.R., 1989. The interpretation and meteorological application of radar backscatter amplitude
616 ratios at linear polarizations. *J. Atmos. Oceanic Technol.* 6, 908-919. doi:10.1175/1520-
617 0426(1989)006<0908:tiamao>2.0.co;2

618 Jameson, A. R., Li, F. K., Durden, S. L., Haddad, Z. S., Holt, B., Fogarty, T., Im, E., Moore, R. K.,
619 1997. SIR-C/X-SAR observations of rain storms. *Remote Sens. Environ.* 59, 267–279.
620 doi:10.1016/s0034-4257(96)00159-9.

621 Katsaros, K. B., Vachon, P. W., Black, P.O., Dodge, P.P., Uhlmann, E.W., 2000. Wind Fields from
622 SAR: Could They Improve Our Understanding of Storm Dynamics? *JOHNS HOPKINS APL*
623 *TECHNICAL DIGEST, VOLUME 21, NUMBER 1, 86-93.*

624 Kumjian, M. R., 2013. Principles and applications of dual-polarization weather radar. Part I: Description
625 of the polarimetric radar variables. *J. Operational Meteor.* 1, 226-242. doi:
626 10.15191/nwajom.2013.0119

627 Melsheimer, C., Alpers, W., Gade, M., 1998. Investigation of multifrequency/multipolarization radar
628 signatures of rain cells over the ocean using SIR-CX-SAR data. *J. Geophys. Res.* 103, 18867–
629 18884. doi:10.1029/98JC00779

Nie, C., Long, D.G., 2007. A C-band wind/rain backscatter
630 model. *IEEE Trans. Geosci. Remote Sens.* 45, 621–631. doi:10.1109/TGRS.2006.888457

631 Oguchi, T., 1983. Electromagnetic wave propagation and scattering in rain and other hydrometeors,
632 *Proc. IEEE* 71, 1029-1078. doi:10.1109/proc.1983.12724

633 Olsen, R., Rogers, D.V., Hodge, D., 1978. The α β relation in the calculation of rain attenuation. IEEE
634 Transactions on antennas and propagation 26, 318–329. doi:10.1109/TAP.1978.1141845.

635 Ryzhkov, A.V., 2001. Interpretation of polarimetric radar covariance matrix for meteorological
636 scatterers: Theoretical analysis. J. Atmos. Oceanic Technol. 18, 315-328. doi:10.1175/1520-
637 0426(2001)018<0315:ioprem>2.0.co

638 Szyrmer, W., Zawadzki, I., 1999. Modeling of the melting layer. Part I: Dynamics and microphysics. J.
639 Atmos. Sci. 56, 3573-3592. doi:10.1175/1520-0469(1999)056<3573:motmlp>2.0.co;2

640 Tournadre, J., Morland, J.C., 1997. The effects of rain on Topex/Poseidon altimeter data. IEEE Trans.
641 Geosci. Remote Sens. 35, 1117–1135. doi:10.1109/36.628780Wijesekera, H.W., Gregg, M.C.,
642 1996. Surface layer response to weak winds, westerly bursts, and rain squalls in the western
643 Pacific Warm Pool. J. Geophys. Res. 101, 977-997. doi:10.1029/95JC02553

644 Willis, P.T., Heymsfield, A.J., 1989. Structure of the melting layer in mesoscale convective system
645 stratiform precipitation. J. Atm. Sci. 46, 2008-2025

646 Zhang, G., Li, X., Perrie, W., Zhang, B., Wang, L., 2016. Rain effects on the hurricane observations
647 over the ocean by C-band synthetic aperture radar. J. Geophys. Res., Oceans 121, 14–26.
648 doi:10.1002/2015JC011044.

649