
Assessment of ocean wave spectrum using global Envisat/ASAR data and hindcast simulation

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Abstract :

Wave mode of spaceborne synthetic aperture radar (SAR) is designed for the global ocean wave observations. Despite the fact that the significant wave height inferred from SAR measurements has been validated against model output and in-situ data, SAR's primary and unique capability for operational 2-dimensional spectral description of sea state remains to be fully evaluated. In this study, we extended the previous assessment approaches by introducing a new SAR image spectral parameter, the Mean rAnge Cross-Spectrum (MACS) that focuses on the isolated wave scales along the radar line-of-sight direction. MACS is an efficient variable in that it characterizes the local wave spectra properties without need of the non-linear wave inversion procedure. The assessment is based on the multiple-year data acquired by Envisat/ASAR wave mode, along with the collocated WaveWatch III (WW3) hindcast and the in-situ buoy-observed wave spectra, for which the SAR forward transformation is systematically performed to obtain the simulated image spectra. Inter-comparison between SAR-measured and WW3-simulated MACS demonstrates that the consistency is wavelength (or wavenumber) dependent. Three typical wavelengths, around 62 m for windsea, 168 m for intermediate waves and 342 m for swell, are selected to present the MACS comparison in detail. Comparable magnitude of SAR-measured and the simulated MACS is observed for the intermediate waves and swell, while larger simulation values are predicted for the windsea waves. Spatial distribution of MACS agrees well between these two data sets for all wavelengths with high correlation coefficients (>0.8) in most of the global ocean. One exception is in the extratropics where the quantitative difference is particularly notable. In the contrary, when comparing SAR-measured and buoys-simulated MACS, the agreement increases towards the shorter (<100 m) wavelengths. We also found that the large-scale atmospheric/oceanic features persistent on SAR images lead to the overestimate of SAR MACS at long wavelengths, which is expected to bias the wave inversion. The wave spectra retrieval performance shall advance as long as such impact is properly resolved.

Highlights

► A novel assessment approach of SAR wave measurement is proposed using MACS. ► The long-time Envisat/ASAR observations is compared with model outputs and buoy. ► The MACS comparison shows the consistency is wavelength dependent. ► MACS shall validate the capability of SAR in resolving wave spectral information.

Keywords : Envisat/ASAR wave mode observations, SAR image spectral parameter, Spectral assessment

10 **1. Introduction**

11 Sea state information is crucial to managing ocean resources and safe operations for ocean
12 going activities. Global wave information has been paramount in understanding wind and wave
13 patterns including regional variability (Young, 1999). Significant wave heights are accurately mea-
14 sured by satellite altimetry within a precision of 10-20 cm with regard to *in-situ* buoy observations
15 (Queffelec, 2004; Zieger et al., 2009). These data have greatly helped the development, cali-
16 bration, and validation of numerical spectral wave models with improved predictability (Ardhuin
17 et al., 2010; Stopa et al., 2016b). While this information is important to monitor regional change
18 (Young et al., 2011), they are not sufficient to fully represent the wave conditions, particularly for
19 multimodal wave systems. Active radars, such as real aperture radars (RAR) and synthetic aper-
20 ture radars (SAR) are the operational spaceborne sensors to measure both wavelength and wave
21 directions on global scales. Of which, SAR is advantageous owing to its high spatial resolution
22 that allows to resolve the wind waves as well as the long-time series since the 1990s.

23 A SAR emits microwave pulses and precisely measure their Doppler-shifted returns. Since the
24 ocean surface is in continuous motion, the radar returns are often misplaced when converting from
25 Doppler-frequency to geo-referenced images in space. The misplacement leads to nonlinear dis-
26 tortions of wave signatures in the along-track direction referred to as the azimuth cutoff (Kerbaol
27 et al., 1998). When the local wind forcing is calm to moderate, the azimuth cutoff wavelength is
28 usually shorter than the swell components, enabling to uniquely estimate both wavelength, direc-
29 tion and spectral energy of swell systems with SAR (Collard et al., 2009; Ardhuin et al., 2017).
30 On the other hand, the high frequency waves are often distorted. This has motivated several empiri-
31 cal studies to directly estimate significant wave height (SWH) from SAR images using statistical
32 methods (Schulz-Stellenfleth et al., 2007; Stopa and Mouche, 2017; Quach et al., 2020). However,
33 the direction and wavelength information is lost especially for waves smaller than the azimuth

34 cutoff which is typically 150-200 m. (Li and Saulter, 2012) compared the subrange SWH inte-
35 grated over distinct wave scales, rather than the overall SWH of advanced-SAR (ASAR) aboard
36 Envisat satellite relative to buoys and models. Their approach in (Li and Saulter, 2012) validates
37 SAR observations in terms of the subrange wave height, but relies on the operational quasi-linear
38 inversion scheme employed by ESA since ERS (Krogstad et al., 1994). It is worth noting that such
39 a scheme is not able to fully recover the nonlinear distortions (Krogstad et al., 1994). So far, the
40 validations of SAR observations regarding ocean wave spectral retrieval are based on either total
41 or effective SWH. The inversed wave spectra has not yet been assessed in terms of their spectral
42 features relative to the reference data.

43 In the cross-track direction (range) of SAR image coordinate, the distortion is less strong and
44 the mapping could be approximated as a quasi-linear process. The Mean RAnge Cross-Spectra
45 (MACS) introduced by (Li et al., 2019) has shown its reliability in describing up to 20 m range-
46 traveling waves Sentinel-1 (S-1) C-band SAR. MACS offers opportunities to investigate the wave
47 information of isolated wave scale in the range direction without going through a non-linear SAR
48 inversion scheme or performing the hypothesis of a quasi-linear imaging mechanism. As a com-
49plementary study to the SWH assessment (Li and Saulter, 2012), we attempt to evaluate the wave
50 spectral signatures through MACS of ASAR observations with respect to wave spectral model
51 output and *in-situ* buoy measurements. Using this approach can potentially lead to a better under-
52standing of the wave dynamics while assessing the SAR and spectral wave model, WAVEWATCH3
53 (WW3) (The WAVEWATCH III® Development Group). In order to carry out the comparison of
54 MACS between SAR and WW3/buoy, we implement the nonlinear forward SAR mapping trans-
55formation in (Engen and Johnsen, 1995) for given ocean wave spectra and SAR configurations
56 to obtain the simulated SAR image spectra. In this study, following the general assessment strat-
57egy of integral wave height (Young, 1999; Li and Saulter, 2012), the quantitative relationship of
58 MACS parameter for various wavelengths is examined between WW3-simulation and SAR mea-
59surements. The global signatures of SAR MACS relative to the simulation is also investigated and
60 discussed to highlight their spatial consistency. An independent comparison with buoy observa-
61tions is invoked to further interpret the inter-comparison results between ASAR and the collocated
62 WW3-simulation.

63 Specifically in this study we use the two-dimensional wave spectra simulated from a hindcast
64 (Stopa et al., 2019) and measured by buoys to derive equivalent MACS values to compare with
65 Envisat/ASAR observations from 2002-2012. We take benefit of this entire decade of SAR data to
66 statistically compare MACS obtained at various wavelengths and at global scale. The manuscript
67 is organized as follows. In section 2 we describe the data sets and methodology: forward SAR
68 transformation and MACS definition. In section 3, we present the MACS comparison between
69 ASAR measurements and the simulation from the WW3 hindcast and buoy ocean wave spectra.
70 Discussions and conclusions follow in Sections 4 and 5, respectively.

71 **2. Data and MACS definition**

72 In this section, we first describe the Envisat/ASAR data and wave spectra from the numerical
73 wave model. Next we describe the forward SAR transformation used to map wave spectra into an
74 equivalent image cross-spectra. Lastly we describe the estimation of MACS from the SAR image
75 cross-spectra.

76 *2.1. Envisat/ASAR wave mode*

77 Envisat/ASAR operated for nearly a decade from November 2002 to April 2012. It is a C-
78 band radar (center frequency of 5.4 GHz), collecting SAR images in various modes. Wave mode
79 is dedicated to observing global ocean waves (Hasselmann et al., 2012). SAR images are acquired
80 every 100 km along the track, having spatial footprint of 10×7 km (azimuth by range) with spatial
81 resolution of 9×6 m. In this work, we use wave mode images at incidence angle of 23° in VV
82 polarization. Envisat is a polar orbit satellite, with both ascending (flying from South Pole to
83 the North Pole) and descending trajectories. To concentrate on a consistent wave direction and
84 monitor its global feature, only the data acquisitions from the ascending passes are included in this
85 study with a total number of SAR images around 3×10^6 .

86 The Level-1B products of SAR image cross-spectrum are systematically processed from the
87 single look complex (SLC) SAR images. Each image spectrum is composed of 24 discrete
88 wavenumbers ranging from $0.008 \text{ rad}\cdot\text{m}^{-1}$ to $0.2 \text{ rad}\cdot\text{m}^{-1}$ and 36 direction (Johnsen, 2005). The
89 images acquired between January 2007 and April 2012 are collocated with the operational ECMWF

90 (European Centre for Medium-Range Weather Forecasts) analysis wind vectors (Nagarajan and
91 Aiyyer, 2004). The reanalysis product is available at spatial resolution of 0.5° every 6h (0h,6h,12h,18h).
92 The wind vector at the nearest spatial and temporal point to the SAR passing time is taken as the
93 reference wind of each SAR image.

94 2.2. Hindcast ocean wave spectra

95 The wave spectra are generated from version 5.16 of the spectral wave model WAVEWATCH3,
96 hereinafter WW3 (The WAVEWATCH III® Development Group). We use the parameterizations
97 of wave generation and dissipation proposed by (Ardhuin et al., 2010) and the non-linear Discrete
98 Interaction Approximation by (Hasselmann and Hasselmann, 1985). It has been shown that this
99 model configuration works well for H_s and swell partitions in comparison to other parameteriza-
100 tion packages (Stopa et al., 2016a). The global model is implemented at latitude and longitude
101 grid of 0.5° with a spectral bin composed of 24 directions and 32 frequencies that are exponen-
102 tially spaced from 0.037 Hz to 0.7 Hz at an increment of 10%. The wind and ice fields at spatial
103 resolution of 0.2° (22 km) from the Climate Forecast System Reanalysis (CFSR) (Saha et al.,
104 2010, 2014) are used to force the model runs. The hindcast was calibrated and corrected in time
105 to match a homogenized satellite altimetry database of (Queffeuilou and Croizen-Fillon) (Stopa,
106 2018; Stopa et al., 2019).

107 We output the wave spectra directly for each longitude, latitude, and time corresponding to the
108 Envisat/ASAR acquisition. The minimum wavelength of WW3 wave spectra is 3.2 m (0.7 Hz),
109 smaller than the wave mode resolution (9 m). This would ensure that all wavelengths resolved by
110 SAR are comparable with WW3 wave spectra.

111 2.3. Buoy observations

112 The wave measurements from National Data Buoy Center (NDBC) are used in this study as
113 complementary to SAR observations and model outputs. A triple collocation data set is created by
114 limiting the spatial distance between the center of SAR images within 100 km and the temporal
115 window shorter than 30 mins. It ends up with 1263 collocation pairs.

116 The wave spectra measured by NDBC buoys, is composed of frequency from 0.04 Hz up
117 to 0.4850 Hz (Vandemark et al., 2005). We employed the Maximum Entropy Method (MEM)

118 proposed in (Lygre and Krogstad, 1986) to reconstruct the two-dimensional wave spectra from
 119 estimates of the Fourier coefficients. In specifics, this includes α_1 that represents the mean wave
 120 direction, α_2 that denotes the dominant wave direction, and r_1 and r_2 that describe the directional
 121 spreading relative to the main direction. The directional bin for buoy wave directional spectral
 122 reconstruction is set to be 10° throughout rest of this paper unless otherwise stated.

123 2.4. SAR forward transformation

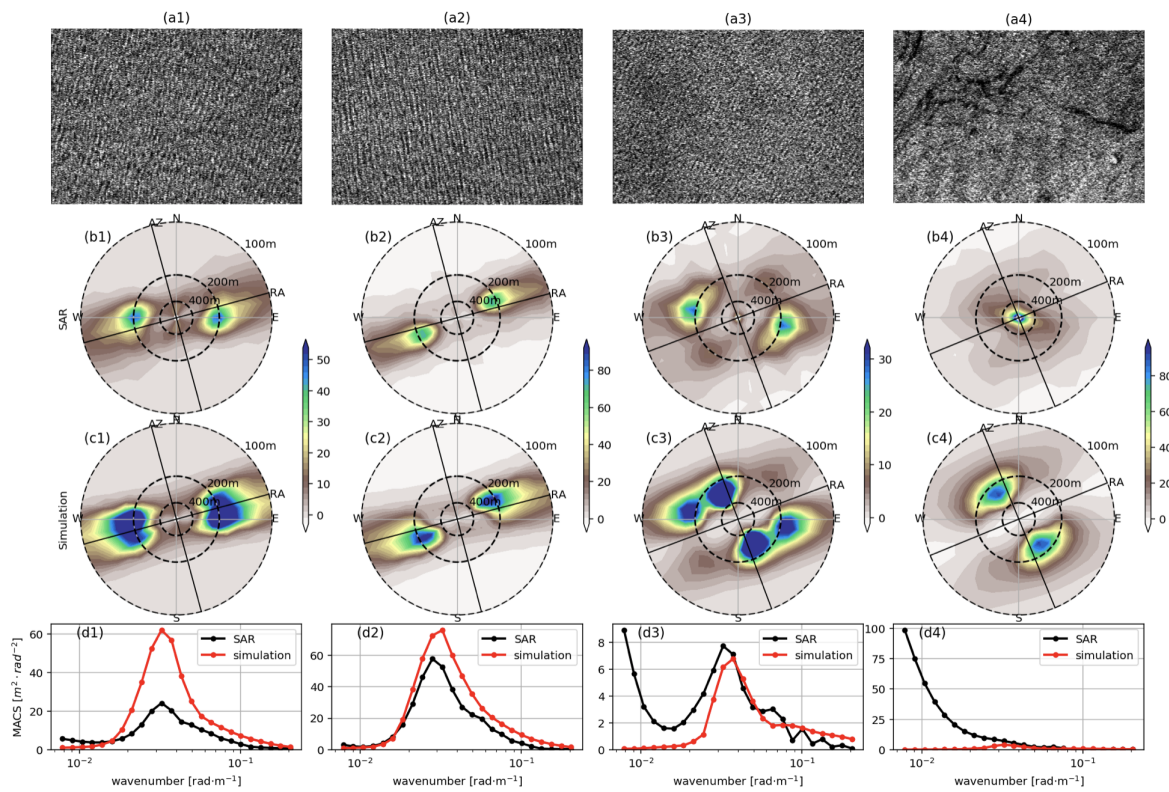


Figure 1: Examples of ENVISAT/ASAR wave mode images for definition of range MACS profile. The row (a1)-(a4) shows the SAR backscattering image. Real component of the SAR cross-spectra is given in the second row (b1)-(b4) and the corresponding simulated cross-spectra using WW3 wave spectra and the forward SAR transformation is in the third row (c1)-(c4). The polar plots of the cross spectra show the wavelength in circles from inner to the outer are 400 m, 200 m and 100 m, respectively. The bottom row (d1)-(d4) shows the MACS profile representing the energy for wavenumbers along the range direction.

124 The SAR forward transformation maps the wave spectra into SAR image cross-spectra, which
 125 is calculated using two sub-looks during the SAR integration time. The imaginary component is
 126 associated to wave motion within the time difference between the two sub-looks. It is therefore

127 widely used to reduce the 180° direction ambiguity of the swell propagation (Engen and Johnsen,
 128 1995). In addition, the cross spectra helps filter non-coherent signals typically improving the
 129 signal-to-noise ratio of ocean waves.

130 (Engen and Johnsen, 1995) presented detailed derivation of SAR image cross-spectra using the
 131 general formula for nonlinear mapping:

$$P_S^{mn}(\vec{k}, \Delta t) = \int d\vec{x} e^{-i\vec{k}\cdot\vec{x}} e^{k_x^2[\rho_{aa}(\vec{x}, t) - \rho_{aa}(\vec{0}, 0)]} [1 + \rho_{II}(\vec{x}, t)] \quad (1)$$

132 where the subscript a and I in ρ_{aa} denote the velocity bunching and real aperture radar (RAR)
 133 modulation, respectively. k_x is the wavenumber along the azimuth direction. The correlation
 134 function defined in Eq. (1) is related to the ocean wave spectrum $S(\vec{k})$ through

$$\rho_{aa}(\vec{x}, \Delta t) = \frac{1}{(2\pi)^2} \int d\vec{k} e^{i\vec{k}\cdot\vec{x}} \cdot \frac{1}{2} \left[\left| M_a(\vec{k}) \right|^2 e^{-i\omega\Delta t} S(\vec{k}) + \left| M_a(-\vec{k}) \right|^2 e^{i\omega\Delta t} S(-\vec{k}) \right] \quad (2)$$

135 where M_a represents the modulation transfer function (MTF) for RAR or velocity bunching. The
 136 detailed formulation of MTF can be found in (Engen and Johnsen, 1995; Li et al., 2019). In this
 137 study, we use the real component of SAR image cross-spectra for MACS.

138 Four SAR roughness images acquired by Envisat/ASAR wave mode are shown in Figure 1
 139 (a1)-(a4). Real component of the measured SAR and simulated WW3 cross spectra are then
 140 accordingly given in (b1)-(b4) and (c1)-(c4). In general, the most energetic wave systems appear
 141 to agree between SAR and WW3 image spectra. Despite the matched spectral pattern, WW3 has
 142 overall larger values for the dominant waves. Note that in panel (b3)&(c3), a wave system along
 143 SAR azimuth direction is predict by WW3, but not well resolved by SAR observations. Also,
 144 though it is likely that the non-ocean waves patterns inducing large-scale modulation as observed
 145 in panel (a4) impacts the cross-spectral analysis, its quantitative influence still needs to be further
 146 investigated.

147 2.5. MACS profile extraction

In this manuscript, we follow the procedure of (Li et al., 2019) to compute MACS from both observations and simulations by

$$MACS(k) = \frac{1}{N} \int_A P_s(k, \phi), \quad A \in [\phi_{ra} - 10^\circ < \phi < \phi_{ra} + 10^\circ] \quad (3)$$

148 where $P_s(k, \phi)$ represents the cross-spectrum in polar coordinate. ϕ_{ra} is SAR range direction. In
149 this study, we extend our range of wave scales from 47 m to 800 m. The smallest wavelength is
150 47 m because ASAR range spatial resolution is about 9 m and we use a factor of ≈ 5 to ensure
151 the waves are properly resolved by the Fourier Transform. The range profile ($\pm 15^\circ$ relative to the
152 line-of-sight) of SAR image cross-spectra is thus extracted, denoted as MACS profile hereinafter.
153 Figure 1 bottom row shows the MACS profiles for these four representative cases. The overall
154 MACS wavenumber distributions generally match, but there are noticeable differences in magni-
155 tude. In panel (d1) and (d2), simulated MACS profiles have larger values than observations. In
156 panel (d3), the SAR exhibits higher MACS energy for wavelengths longer than 400 m. While in
157 panel (d4), SAR MACS is constantly larger for the wavelengths longer than 150 m. This is clearly
158 due to the presence of the large-scale phenomenon as observed in the SAR image. MACS can be
159 computed for any wavelength between 30 m and 800 m with ASAR. Hereinafter, we denote as
160 $MACS_\lambda$ where λ is the wavelength. For example $MACS_{62}$, represents MACS for wavelengths of
161 62 m.

162 3. Results

163 In this section, we examine the consistency of MACS profile between SAR-observations and
164 WW3-simulations. Taking advantage of the versatility of MACS, we analyze the statistical rela-
165 tionship as well as the global patterns of MACS for three different wavelengths of 62.5 m, 168.4 m
166 and 342.0 m. We also carried out MACS comparisons with external wave measurements by buoys
167 as an attempt of interpreting the differences found between SAR and WW3-simulation.

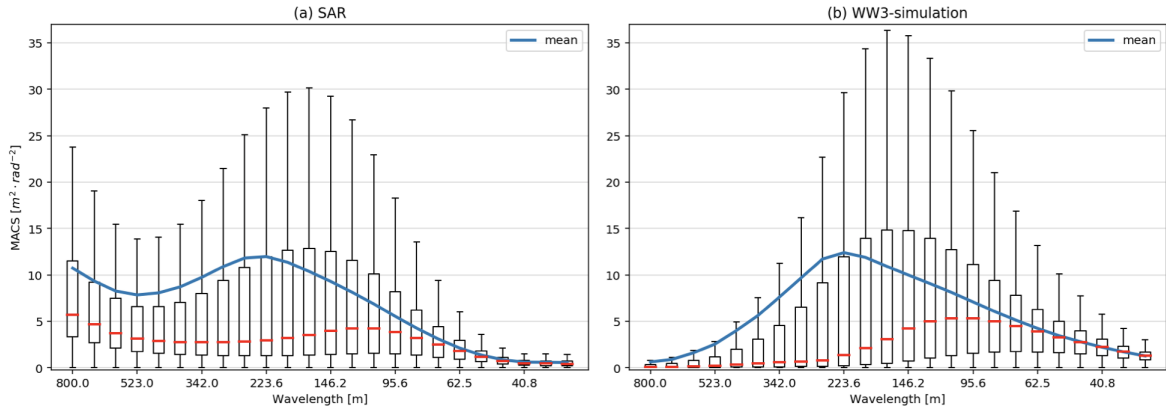


Figure 2: Box plot of MACS profile from (a) SAR-observation; (b) WW3-simulation with respect to wavelength. For MACS at given wavelength, each rectangle spans the first quartile to the third quartile (the interquartile range, IQR). The red segment inside rectangles denotes the median. The upper whisker extends to the largest data value within $1.5 \times IQR$ above the third quartile and the lower to the smallest value within $1.5 \times IQR$ below the first quartile. The blue curve represents the mean for each wave scale.

168 3.1. MACS profile

169 MACS profile of SAR-observation and WW3-simulations between January 2007 and April
 170 2012 is presented in box plot relative to wavelength in Figure 2. The central box represents the
 171 likely range of variation : the interquartile range, IQR . The whisker extends to the largest and
 172 smallest data value within $1.5 \times IQR$ from the lower and upper quartile, respectively. MACS
 173 profile of SAR shares a couple of commonality with that of WW3-simulation. First, for most of
 174 the wavelengths, MACS is not normally distributed as the distance of the median to the upper
 175 quartile is much larger than that to the lower quartile. In other words, MACS is generally right-
 176 skewed with smaller median (red segment) than the mean (blue curve). The mean and median
 177 are largely apart except over shorter wavelengths (<62.5 m) where these two are almost identical.
 178 The profile peak also differs as the mean locates at 223.6 m and the median at 95.6 m. The
 179 maximum IQR locates at wavelength of 168.4 m, different from both the median and the mean.
 180 Despite the resembling distributions of MACS for each wave scales between SAR and WW3,
 181 they also differ in several aspects. SAR MACS profile in Figure 2(a) has a clear increase towards
 182 longer wavelengths beyond 523.0 m for mean, median and IQR . While WW3-simulation shows
 183 consistent MACS decrease towards both longer and shorter wavelengths from the peak. Both data
 184 sets have comparable mean MACS except for the very long wavelengths. It is not the case for the

185 median and *IQR*. For wavelengths shorter than 250 m, the WW3-simulated *IQR* is larger than
 186 SAR-observations. As for the median, the WW3 exceeds at wavelength shorter than 146 m. The
 187 distribution of WW3-simulated MACS at one particular wavelength roughly follows a negative
 188 exponential function, while the SAR-observed is a log-normal curve (not shown). In any case,
 189 smaller *IQR* suggests a less spread distribution. On the other hand, for wavelengths longer than
 190 250 m, the slow variation of SAR MACS might result from the impact of large-scale oceanic and
 191 atmospheric phenomena as displayed in Figure 1(a4)-(d4). This also possibly results in the large
 192 spread of SAR MACS than the WW3-simulation.

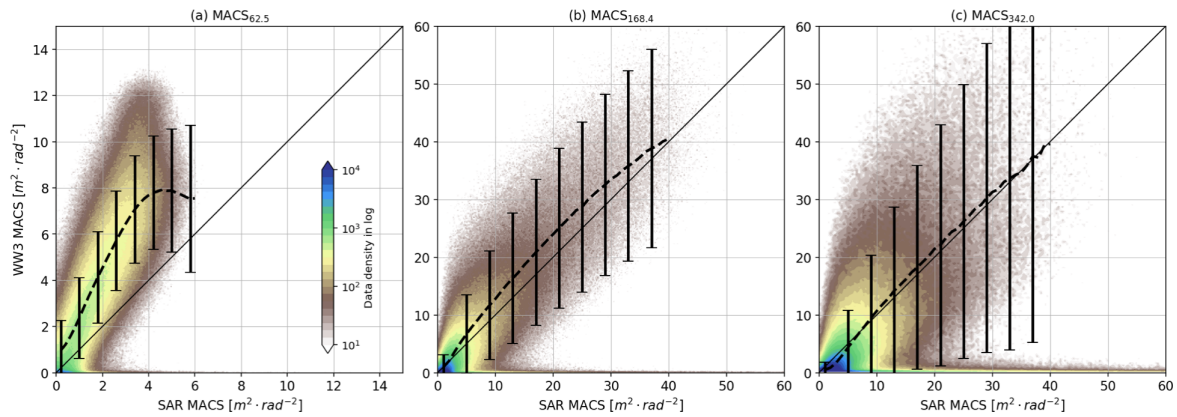


Figure 3: Q-Q plot of MACS comparison between SAR and WW3-simulation for three wavelengths (a)62.5 m; (b)168.4 M; (c)342.0 m. The dashed lines are the mean curve and the error bar stands for the one standard deviation. Color denotes data count in log scale.

193 Going further, we now focus on observed and simulated MACS for short (62.5 m), intermediate
 194 (168.4 m) and long (342.0 m) waves. Wavelength of 168.4 m has both comparable mean and
 195 median between SAR and WW3. MACS of 62.5 m exhibits smaller values in SAR observations
 196 than WW3 simulations, while it is the opposite trend for MACS of 342.0 m. The Q-Q plots of
 197 SAR MACS relative to the simulated MACS for these three selected wavelengths are presented in
 198 Figure 3. For 62.5 m as shown in Figure 3(a), WW3-simulation is consistently higher than that of
 199 SAR with data points well above the one-to-one line. If we neglect the saturation of SAR MACS
 200 beyond $4 \text{ m}^2 \cdot \text{rad}^{-2}$, slope of the linear fit to these points approximates 2. It means that for most of
 201 SAR acquisitions, the predicted MACS by WW3 is twice larger than the SAR observations. With
 202 wavelength of 168.4 m shown in Figure 3(b), the agreement improves as most of the data points

203 scatter around the one-to-one line. It should be noted that the mean curve (dashed line) slightly
 204 deviates from a linear variation. While for wavelength of 342.0 m in Figure 3(c), the mean curve is
 205 indeed well following the one-to-one curve. However, the MACS relationship is largely dispersed
 206 as represented by the larger standard deviation. For the $\text{MACS}_{342.0}$, its standard deviation gradually
 207 increases with $\text{MACS}_{342.0}$ values. For the other two wavelengths, the standard deviation is almost
 208 constant from small to large MACS values. In particular, very small MACS values are predicted
 209 by WW3-simulation as shown by the large number of data points clustered close to the horizontal
 210 axis in Figure 3(c). The spatial consistency between these two data sets is yet to be confirmed.
 211 As such, the comparison of global MACS for these three selected wavelengths are analyzed in the
 212 following.

213 3.2. Spatial analyses of MACS

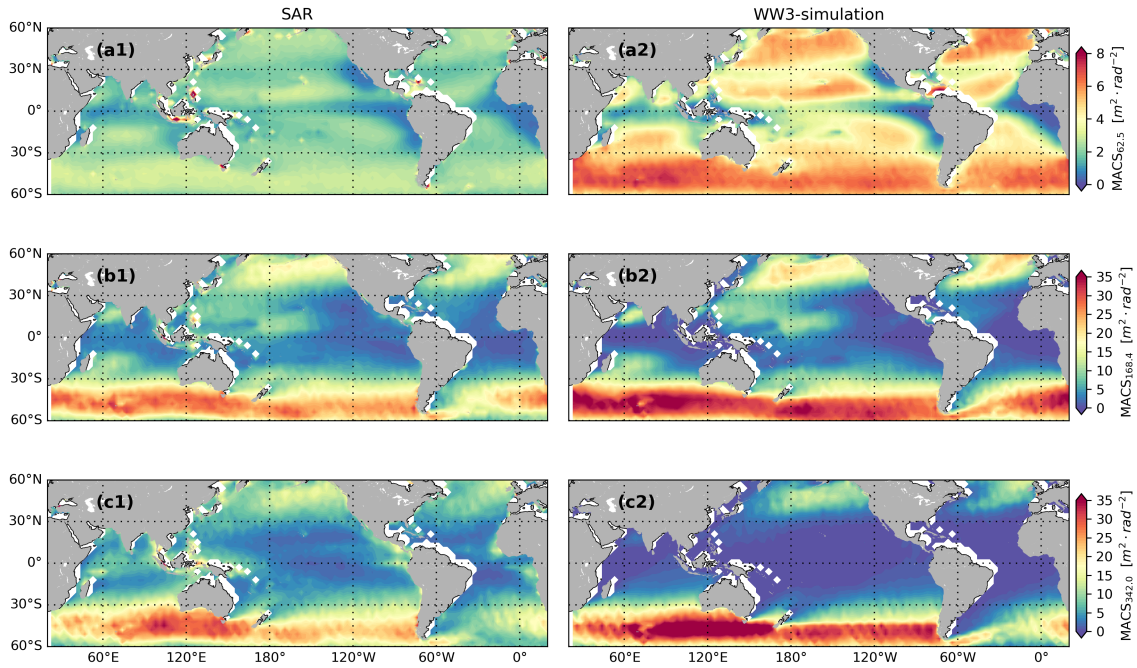


Figure 4: Global average of MACS from (left) SAR and (right) WW3-simulation for (top) 62.5 m; (middle) 168.4 m and (bottom) 342.0 m. Both latitude and longitude are binned into 2.5° by 2.5° . The bins located 50 km from the closest land are masked by blank space. Color denotes magnitude of MACS and note that the color bar dynamics differ in the three panels.

214 We also compute global maps of the three representative $\text{MACS}_{62.5}$, $\text{MACS}_{168.4}$, and $\text{MACS}_{342.0}$
 215 to describe short, intermediate and long wavelengths. In qualitative terms, the global patterns of

216 SAR-observed and WW3-simulated MACS are similar. Average of global MACS at wavelength
 217 of 62.5 m from SAR-observations (left) and WW3-simulations (right) is given in top panel of
 218 Figure 4. The spatial features both mimic that of the overall wind field (Young, 1999) as these
 219 short waves are closely coupled with moderate wind speeds around $7 \text{ m} \cdot \text{s}^{-1}$ (Hasselmann et al.,
 220 1973). Smaller $\text{MACS}_{62.5}$ are observed over the Inter Tropical Convergence Zone (ITCZ) corre-
 221 sponding to the low wind speed throughout the year (Žagar et al., 2011). Over the extratropics,
 222 larger $\text{MACS}_{62.5}$ is caused by the high wind events associated to the frequent low-pressure storm
 223 activities. However, the SAR-observed MACS is systematically smaller than the WW3-simulated
 224 values across the globe, consistently with Figures 2 and 3(a). For example, in the Southern Ocean,
 225 WW3-simulated $\text{MACS}_{62.5}$ is around $6 \text{ m}^2 \cdot \text{rad}^{-2}$, which is twice as large as the SAR-observed
 226 $\text{MACS}_{62.5}$. Such trend of smaller SAR-observed MACS exists for all the wavelengths up to 150 m
 227 (not shown here for brevity). MACS of these two data sets becomes gradually closer as the wave-
 228 length increases to approximately 170 m (see Figure 2).

229 We show $\text{MACS}_{168.4}$ in the middle panel of Figure 4. Overall, WW3-simulated and SAR-
 230 observed $\text{MACS}_{168.4}$ are in good agreement in terms of the global pattern. Similar to $\text{MACS}_{62.5}$,
 231 $\text{MACS}_{168.4}$ is also consistently high (around $25 \text{ m}^2 \cdot \text{rad}^{-2}$) throughout the year in the southern
 232 extratropics. The trade wind regions have reduced MACS in comparison to the extra-tropical
 233 regions. Yet, quantitative differences remain. Overestimates of the simulated MACS mainly locate
 234 in the extratropics, contrast to the global trend of $\text{MACS}_{62.5}$. Note that over the Arabian Sea,
 235 this overestimate is also evident during the monsoon season (seasonality not shown). It is thus
 236 speculated that WW3-simulation tends to predict larger spectral energy for 168.4 m waves at
 237 relatively high wind conditions. At low to median wind speed, the relative magnitude depends
 238 on geographic loctions. For example, SAR-observed $\text{MACS}_{168.4}$ generally exceeds the simulation
 239 in the East Equatorial Pacific Ocean. While in the Tropics, SAR-observed $\text{MACS}_{168.4}$ has larger
 240 values. This spatial pattern well corresponds to the feature presented in Figure 3(b). Larger WW3-
 241 simulated $\text{MACS}_{168.4}$ is mostly observed at larger MACS values, in other words at high sea state,
 242 like in the extratropics. While the larger SAR-observed $\text{MACS}_{168.4}$ mostly occurs at smaller MACS
 243 values as depicted by the blue cluster in Figure 3(b).

244 At last, global average of $\text{MACS}_{342.0}$ is displayed in the bottom panel of Figure 4. It is ex-

245 pected that this longer wavelength relates to wind speeds approximately equivalent to 18 ms^{-1}
 246 (Hasselmann et al., 1973). Large $\text{MACS}_{342.0}$ values are mostly located in the extratropics, partic-
 247 ularly in the Southern Hemisphere. Given the duration and fetch needed for the long waves to
 248 grow, $\text{MACS}_{342.0}$ are mostly observed in the east part of the Pacific and Atlantic Ocean, distin-
 249 guished from the spatially distributed MACS for short wavelengths. The South America shelters
 250 the $\text{MACS}_{342.0}$ in the South Atlantic. In the trade wind regions, the WW3-simulations have similar
 251 regional patterns as the SAR observations but with much lower magnitude. While in the extratrop-
 252 ics, WW3-simulation exhibit larger MACS values throughout the year. This results in the scattered
 253 comparison and large standard deviation in Figure 3(c).

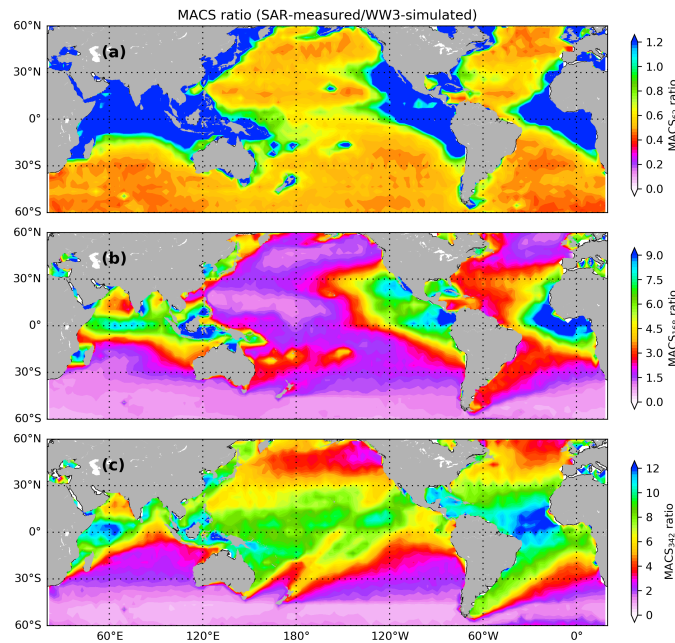


Figure 5: Global magnitude difference of MACS (simulation-SAR) for (a) 62.5 m; (b) 168.4 m; (c) 342.0 m . The latitude/longitude bin of 2.5° is used in this figure.

254 To further assess the difference in the geographical pattern, we first computed the MACS mag-
 255 nitude difference (WW3-SAR) as shown in Figure 5. The magnitude difference is uniformly posi-
 256 tive for $\text{MACS}_{62.5}$ across the globe in Figure 5(a). This corresponds to the constantly larger WW3-
 257 simulation as presented in both Figure 3 (left panel) and Figure 4 (top panel). With increasing
 258 wavelength, MACS difference shows significant spatial variability. For example, both $\text{MACS}_{168.4}$
 259 and $\text{MACS}_{342.0}$ have much higher positive values in the southern extratropics than the rest of the

260 global surface in Figure 5(b) and (c), respectively. In the contrary, $\text{MACS}_{342.0}$ difference is nega-
 261 tive in the trade winds regions due to the smaller WW3-simulation as observed in Figure 4 bottom
 262 panel. It is worth noting that the straight boundary line at latitude of 45°S in both Figure 5(b) and
 263 (c) are present throughout the year. Investigations of this abrupt alignment change will be further
 264 addressed.

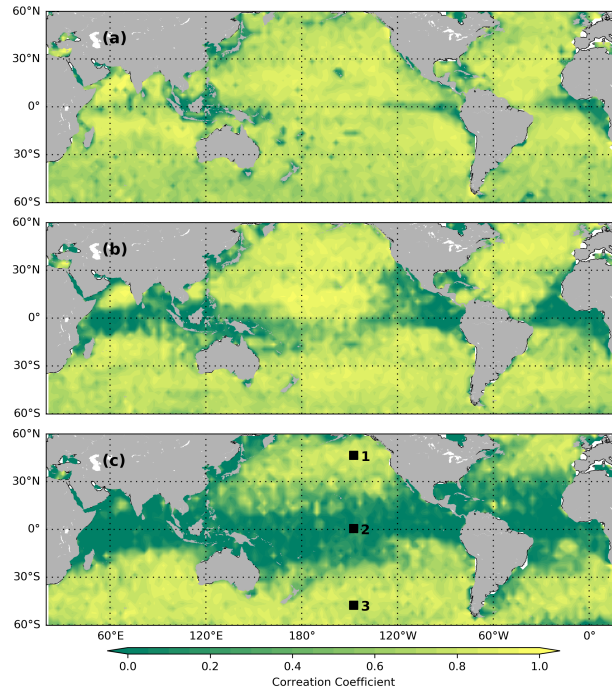


Figure 6: Global correlation coefficients of MACS between SAR measurements and WW3-simulation for (a) 62.5 m; (b) 168.4 m; (c) 342.0 m. The latitude/longitude bin of 2.5° is used in this figure. The three black rectangle indicate the areas selected for detailed correlation analysis in the following.

265 The Pearson correlation coefficients for MACS at 62.5 m, 168.4 m and 342.0 m are calculated
 266 from the monthly time series over each latitude/longitude bin of 2.5° , and shown in Figure 6. As in
 267 Figure 6(a), $\text{MACS}_{62.5}$ between the two data sets is highly correlated with correlation coefficient
 268 larger than 0.8 in most of the open ocean. Similarly, $\text{MACS}_{168.4}$ has strong correlation on the
 269 global scale, except over a narrow band at the equator ($\pm 10^\circ$) where the correlation coefficient
 270 decreases to 0.1 as in Figure 6(b). The low correlation along the equator extends to the entire trade
 271 winds region, reaching $\pm 30^\circ$ for $\text{MACS}_{342.0}$ as in Figure 6(c).

272 To further analyze the location dependent correlations, three areas of each covering 5° in both

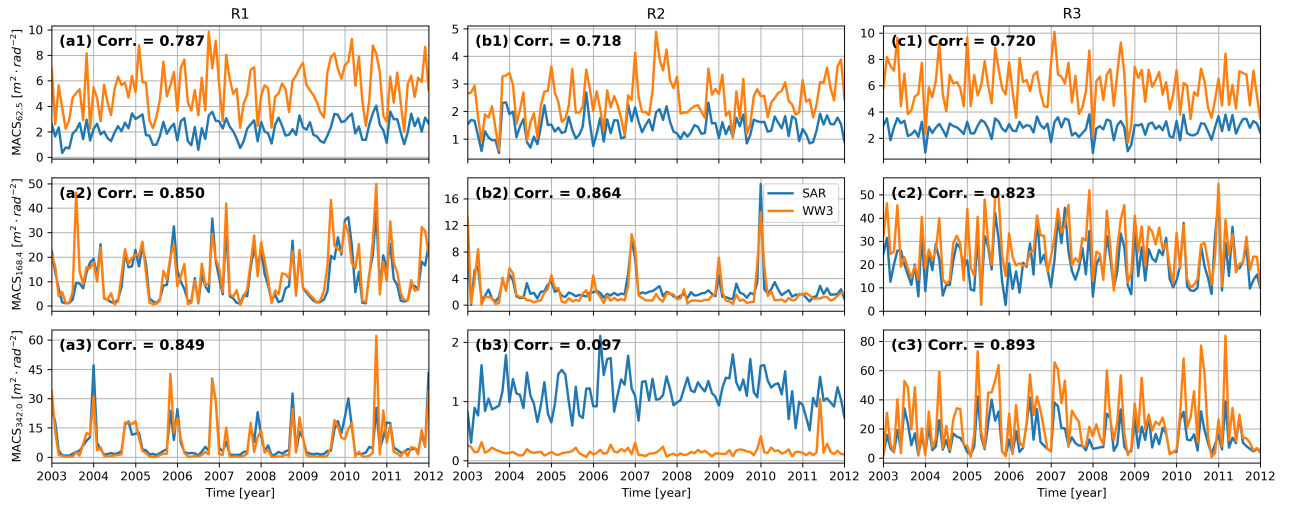


Figure 7: Time series for MACS over the three areas annotated in Figure 6, from left to right are R1, R2 and R3, respectively. For each area, from top to bottom are 62.5 m, 168.4 m and 342.0 m. The correlation coefficient is accordingly given in each plot.

273 latitude and longitude are selected and annotated by black rectangle in Figure 6(c). The monthly
 274 time series of MACS for 62.5 m, 168.4 m and 342.0 m over each area are then plotted in top,
 275 middle and bottom panel of Figure 7, respectively. The variation trend of temporal $MACS_{62.5}$
 276 is found similar for both data sets except that WW3-simulation has consistently larger values.
 277 Despite that the simulated and observed MACS differentiate approximately by a factor of 2 over
 278 the time period, the co-variation results in the correlation coefficients higher than 0.70 for all these
 279 three areas. While for $MACS_{168.4}$ in the middle row, both data sets show comparable variation
 280 trends as well as quantitative values. Ocean waves of 168.4 m is better resolved by wave mode
 281 than the 62.5 m because they are less subject to the accuracy of input winds. This produces the high
 282 correlations (>0.80) found for all three areas. Contrast to the shorter wavelength in Figure 7(a1),
 283 MACS in (a2) exhibits much stronger seasonal changes. In winter, long ocean waves are generated
 284 by the high wind events associated with the winter storms and the averaged $MACS_{168.4}$ reaches up
 285 to $25 m^{-2} \cdot rad^{-2}$. As the winter storms recede, the winds lowers and $MACS_{168.4}$ accordingly reaches
 286 the minimum values in summer close to zero. For the long waves of $MACS_{342.0}$, both R1 and R3
 287 see consistent variation of SAR observation and WW3-simulation. Note that the WW3-simulation
 288 is greatly underestimated over R2 as shown in Figure 7(b3), resulting in the lower correlation
 289 coefficient of 0.097. This agrees well with the negative MACS difference in Figure 5(c). We

290 attributed this discrepancy to the pollution of SAR-observed MACS by atmospheric or air-sea
 291 interaction features, including rain impact and wind streaks et al. In fact, high occurrence of such
 292 phenomena has been detected by the automatic classification of Sentinel-1 SAR wave mode data
 293 Wang et al. (2019) and particularly in the Tropics.

294 3.3. Triple comparison with buoy measurements

295 The global signatures of MACS strongly resemble for both data sets. Meanwhile it is found
 296 that the WW3-simulation is generally larger than the SAR MACS. This quantitative difference also
 297 depends on the spatial locations at the globe. Taking advantage of the numerous Envisat/ASAR
 298 acquisitions, a triple comparison between SAR, WW3 and buoy measurements is carried out to
 299 further diagnose the difference between these data sets.

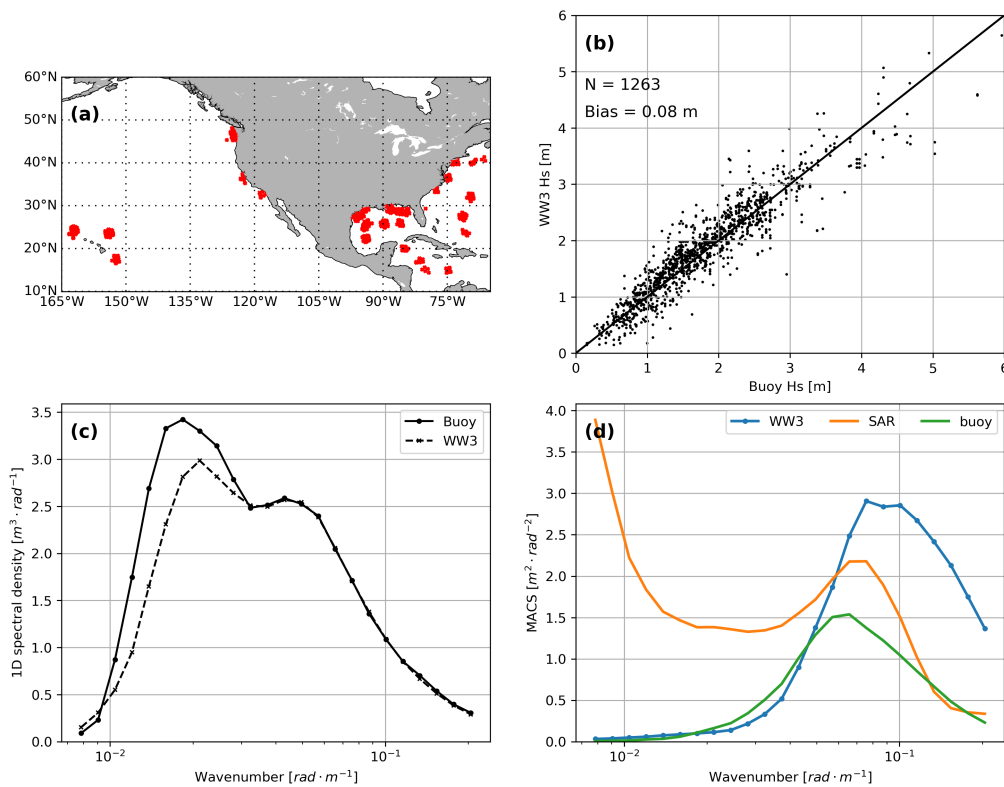


Figure 8: Comparison of triple collocation between SAR, buoy and WW3. (a) Position of NDBC buoys included in this study. (b) Comparison of significant wave height between collocated WW3 and buoys. (c) One-dimensional wave spectra from buoy and WW3. (d) The averaged MACS profile over all collocation pairs.

300 To extend the inter-comparison with *in-situ* measurements, the NDBC wave buoys that are

301 capable of obtaining two-dimensional wave spectra are collocated with the Envisat/ASAR wave
 302 mode data set. This ends up with 1218 collocated data points. The spatial positions of these
 303 collocated wave buoys are shown in Figure 8(a). Of which, 714 collocated data points are scattered
 304 in the Gulf of Mexico and 64 points off the west coast and the rest (443 points) are around the
 305 Hawaii. We first compared the significant wave height of both buoys and WW3, which are in good
 306 consistency with negligible biases. The averaged one-dimensional wave spectra from all buoys
 307 measurements with corresponding WW3 simulations are then given in Figure 8(b). Both data sets
 308 present high conformity for most of the wavelengths, except at the long waves of 350 m where
 309 buoy tends to measure slightly larger wave spectral density. The two wave peaks are well captured
 310 by WW3 and buoys. One is long swell (wavelength of 330 m) coming from remote storms in the
 311 Southern Ocean and the north extratropics. The other corresponds to locally generated wind sea
 312 at wavelength of 120 m. This comparison well evidences the capability of WW3 in accurately
 313 modelling the one-dimensional ocean wave spectra.

314 However, the MACS spectra from SAR, WW3 and buoys show quite striking disagreement
 315 as shown in Figure 8(d). At low wavenumber, average of SAR MACS still displays the abrupt
 316 increase, while WW3 and buoy are in good agreement with weak spectral energy. Towards the
 317 higher wavenumber, all show a decreasing trend but with different spectral level. In particular,
 318 WW3 has the highest MACS values and buoy has the lowest. SAR lies in the middle and has
 319 comparable MACS with buoy for waves shorter than 60 m. The differing MACS between WW3
 320 and buoy contrasts the alignment of one-dimensional wave spectra in Figure 8(a). This indicated
 321 that the directional pattern of both wave spectra might be different. To confirm, the mean wave
 322 direction as well as the spectral spread for both wind sea and swell part are calculated. The
 323 partition of wind sea from swell is based on the assumption of a fully developed sea state where
 324 the wind and waves are in equilibrium. The separation wavenumber k_s is set as the wavenumber
 325 where its phase speed equates the local wind speed. The mean wave direction and the directional
 326 spread are then computed in terms of the following formulas (Herbers et al., 1999)

$$\tan\phi_m = \frac{\int_{k_0}^{k_1} \int_{-\pi}^{\pi} \sin\phi S(k, \phi) dk d\phi}{\int_{k_0}^{k_1} \int_{-\pi}^{\pi} \cos\phi S(k, \phi) dk d\phi} \quad (4)$$

and

$$\sigma_{\phi}^2 = \frac{\int_{k_0}^{k_1} \int_{-\pi}^{\pi} \sin^2(\phi - \phi_m) S(k, \phi) dk d\phi}{\int_{k_0}^{k_1} \int_{-\pi}^{\pi} S(k, \phi) dk d\phi} \quad (5)$$

327 where k is the wavenumber and ϕ is the wave direction. For the wind sea, $k_0 = k_s$ and for the
 328 swell part, $k_1 = k_s$. $S(k, \phi)$ is the two-dimensional wave spectra from WW3 hindcast or the buoy
 329 measurements.

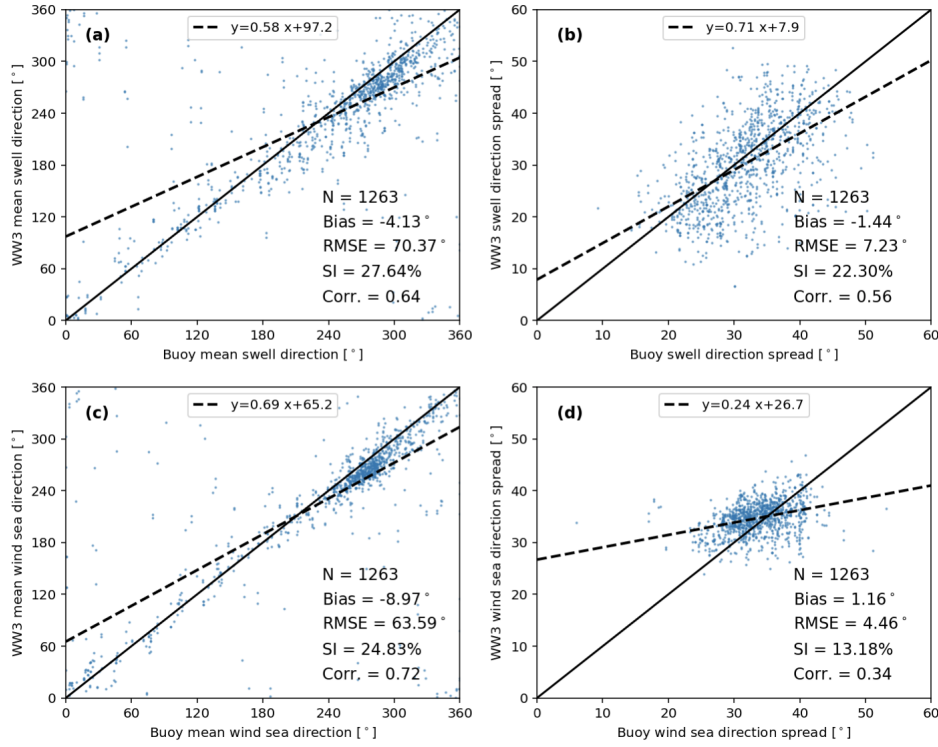


Figure 9: Comparison of mean wind sea in (a) and swell direction in (c) between WW3 outputs and buoy measurements with the directional spread accordingly shown in (b) and (d). Metrics are annotated on the bottom right.

330 The calculated mean wave direction and directional spread for both wind sea and swell part are
 331 presented in Figure 9. As reflected by the metrics, WW3 and buoy wave spectra are well matched
 332 for the swell waves. The mean wave direction of both data sets scatter tightly around the one-to-
 333 one line as shown in Figure 9(a). While the swell direction spreads appears to loose relationship
 334 with large standard deviation in comparison to the magnitude. By comparison, bias of the mean
 335 wind sea direction in Figure 9(c) is -8.97° , which is larger than that of the wave direction. Though
 336 bias of the spectral spread for wind sea is small of 1.16° (Figure 9(d)), the lower correlation

337 coefficient of 0.34 suggests that these two are not well related. In fact, the linear slope of least-
 338 squared fit to these points is 0.24, which is much smaller compared to the 0.71 for swell waves in
 339 Figure 9(b). The impact of wind sea on the simulated MACS profile is two-fold. On one hand,
 340 the slightly shifted wind sea direction might result in differing MACS magnitude along the range
 341 direction. On the other hand, the wind sea spread could cause the nonlinear velocity bunching to
 342 be different between buoy and WW3 cases. This would accordingly change the magnitude of SAR
 343 image spectra as well as the MACS.

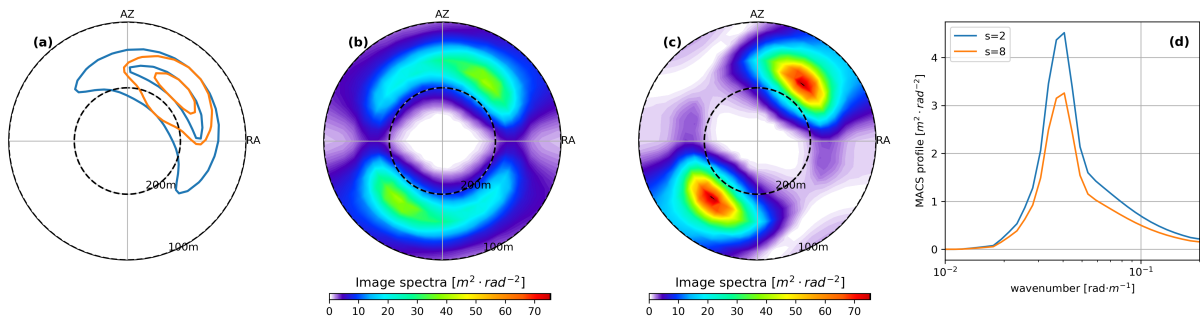


Figure 10: (a) The normalized directional wave spectrum for $s = 2$ (blue curve) and $s = 8$ (orange curve) in Eq. (6). The contour lines give the 25% and 75% relative to the maximum spectral energy. The simulated SAR image cross-spectrum is given in (b) $s = 2$ and (c) $s = 8$, respectively. (d) The accordingly extracted MACS profile.

To demonstrate this assumption, two SAR cross-spectra are simulated based on the JONSWAP spectrum and the following directional spreading function (Mitsuyasu et al., 1975):

$$D(k, \phi) = |\cos[(\phi - \bar{\phi})/2]|^{(2s)} \quad (6)$$

344 where ϕ is the wave direction and $\bar{\phi}$ denotes the dominant wave direction. The parameter s de-
 345 termines the concentration degree of the spreading function relative to the mean direction. For
 346 simplicity, two constant values of $s = 2$ and $s = 8$ are set to calculate the directional wave spectra
 347 as shown in Figure 10 (a). The contour lines represent the 25% and 75% of the maximum wave
 348 spectral energy, respectively. The mean wave direction is 45° from the azimuth, the wind speed is
 349 $8m \cdot s^{-1}$ and the wind fetch is 500 km. The wave spectrum of $s = 2$ (blue curve) displays wider
 350 spread compared to that of $s = 8$ (orange curve). The combination effect of wave direction devi-
 351 ation from the range axis and the wider spread function for $s = 2$ results in larger wave spectra

352 magnitude along the radar line-of-sight. In consequence, the simulated image spectra of $s = 2$
353 shown in Figure 10 (c) is larger than that of $s = 8$ in Figure 10 (b) in the range direction. This
354 corresponds to the higher MACS profile simulated based on the wide-spread wave spectrum (blue
355 curve) as given in Figure (d). Note that the configuration of mean wave direction is similar to that
356 of the mean wind sea direction in Figure 9. The results that larger direction spread yields higher
357 MACS profile, in accordance with the slightly greater wind sea direction spread in Figure 9(d), to
358 some extent explain the MACS comparison in Figure 8(d). Further in-depth and comprehensive
359 evaluation of WW3 outputs relative to the buoy measurements in terms of the spectral perspective,
360 rather than the integrated wave height should be devised.

361 4. Discussion

362 As a parameter defined relative to variable wavelengths, MACS offers new perspectives to
363 make comparisons between SAR observations and the reference data produced by WW3. In
364 general, the global patterns of SAR-observed MACS promisingly resemble that of the WW3-
365 simulation. Yet the quantitative disagreements are noticeable. As demonstrated by the percentile
366 analyses of MACS profile in Figure 2, SAR and WW3 have particularly marked difference for long
367 waves (wavelength longer than 300 m) and wind sea (wavelength shorter than 100 m). The MACS
368 overestimation of wind sea relative to the WW3-simulation is consistent on the globe as shown in
369 Figure 5(a). While the difference for long waves is region dependent as in Figure 5(c). As illus-
370 trated in Figure 1, the long waves derived from SAR images are subject to impact of atmospheric
371 and/or oceanic features on the sea surface, which pollutes the wave signals in the MACS analyses.
372 In fact, the influence of large-scale features on radar backscatter also depends on the local wind
373 speed. As concluded in (Wang et al., 2019), the rain is hard to detect at high winds. As such, its
374 impact on the spectra at long wavelength is negligible so that $\text{MACS}_{342,0}$ has consistent values for
375 both R1 and R3 regions in the Southern extratropics. While for R2 at low winds, SAR-observed
376 $\text{MACS}_{342,0}$ is much higher as shown in Figure 7(b3).

377 A test is performed as a first attempt to illustrate the impact of other phenomena on MACS
378 estimates. In general, SAR image spectra of these patterns have an unusually high tail at low
379 wavenumber of MACS profile similar to that in Figure 1(d4). A simple criteria is employed to

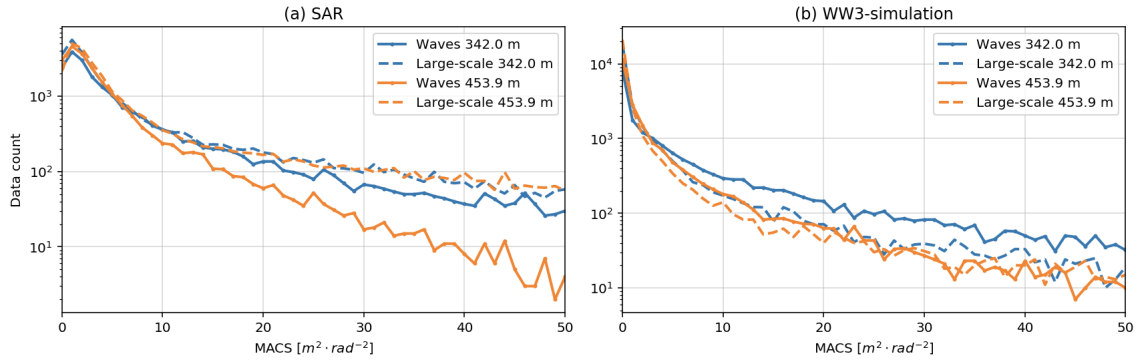


Figure 11: Histogram of (a) SAR and (b) WW3-simulated $MACS_{342.0}$ and $MACS_{453.9}$ with (dashed curves) and without (solid curves) potential impact of large-scale features on SAR images.

380 sort out the cases with such high-tail form. If the averaged MACS for wavelengths longer than
 381 342.0 m is larger than its counterpart for shorter wavelengths (<342.0 m), this case is assumed
 382 to be impacted by the large-scale features. Otherwise, ocean wave signatures are expected to be
 383 dominant in this case. The histogram of MACS for two wavelengths of 342.0 m and 453.9 m is
 384 presented in Figure 11. For SAR-measured MACS in Figure 11(a), all cases with large-scale fea-
 385 tures tend to have larger MACS magnitude in comparison to the dominant waves. The two curves
 386 of $MACS_{342.0}$ (blue) are closer to each other in comparison to those of $MACS_{453.9}$ (orange). This
 387 is indicative of the enlarging impact of these large-scale features with wavelengths. While WW3
 388 wave spectra are only able to predict surface wave properties, the MACS contrast between the
 389 pure waves (solid line) and potential large-scale (dashed) in Figure 11(b) is not as evident as that
 390 in Figure 11(a). Given the non-negligible difference shown in Figure 11(a), processing procedure
 391 is essential to identify the presence of large-scale phenomena and filter out their contributions in
 392 the SAR image spectrum for a proper interpretation of the image cross-spectra. As a matter of
 393 fact, on-going efforts are being made to classify these features based on a deep learning tech-
 394 nique for Sentinel-1 observations. Valid algorithms are expected to be deployed and a consistent
 395 reprocessing from ASAR to Sentinel-1 shall then be feasible for improved wave measurements.

396 5. Summary

397 Spaceborne SAR has been proven to be an advantageous sensor in global wave observations
 398 (Hasselmann et al., 2012). Despite the previously extended study to evaluate SAR wave observa-

399 tions based on the subrange wave height (Li and Saulter, 2012), the capability of SAR mapping
400 isolated wave component remains undisclosed. This study further advances the SAR wave vali-
401 dation towards the image spectral level through the newly defined MACS parameter. One of its
402 advantages is its versatility, allowing the comparison to be directly made for various wavelengths
403 without the complicated SAR inversion scheme.

404 The large volume of data acquired by Envisat/ASAR aids the examination of MACS relation-
405 ships with respect to the collocated WW3 hindcast wave spectra. Both data sets show a couple
406 of similarities in MACS signatures. First of all, MACS magnitudes of all wavelengths are com-
407 parable between SAR observation and WW3-simulation. The global patterns of SAR and WW3
408 derived MACS agree well with high correlations in the open ocean. However, the quantitative
409 inconsistency between these two is not only wavelength variant, but also regionally dependent.
410 WW3 appears to constantly predict larger MACS magnitude for short wavelength (<100 m) at
411 global scale. For long waves (>300 m), such overestimate by WW3 only exhibits in the south-
412 ern extratropics with opposite trend in the trade winds where WW3 predicts consistently smaller
413 values. In contrast to the well aligned significant wave height (Li and Saulter, 2012; Stopa and
414 Mouche, 2017), the difference observed by MACS of various wave scales is expected to offer new
415 insights into the assessment approach of SAR observations.

416 Even with the assumption that SAR forward transformation used in this paper is able to ac-
417 curately reproduce the wave imaging process, several points still need to be addressed in order
418 to better interpret the results of MACS comparison. On one hand, the large-scale impact should
419 be further quantified as effort to isolate the MACS quantity that is associated with ocean surface
420 waves. This will in turn help refine the SAR wave inversion and further enhance the utility of SAR
421 measurements to infer the realistic ocean swell partitions. In addition, other geophysical appli-
422 cations, such as air-sea interactions and sea ice monitoring shall also benefit. On the other hand,
423 the spectral spread has been demonstrated to have impact on the MACS magnitude along with the
424 mean wave direction. The inconsistency observed between buoy-based and WW3-based simula-
425 tions also invokes the necessity of validating the numerical outputs in terms of the two-dimensional
426 wave spectra rather than the integrated parameters.

427 In this paper, we focused on the assessment of MACS profile from the Envisat/ASAR wave

428 mode observations. There are also multiple SAR sensors in orbit now, including Sentinel-1 con-
429 stellation, Radarsat Constellation Mission, Gaofen-3 et al. Instrument characteristics, such as spa-
430 tial resolution, swath and incidence angles, generally differ among these satellites. While the com-
431 monly used validation procedure through significant wave height is limited to evaluate the SAR
432 wave measurements. This MACS approach can be readily extended to grade the performance of
433 SAR observations from the spectral point of view as well as to determine the consistency between
434 sensors.

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