
Design and field testing of a non-linear single-beam echosounder for multi-frequency seabed characterization

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Abstract :

Seabed mapping and characterization are best performed using several frequencies and several angles of incidence. This is often an issue because of the need to employ different sonars, with distinct frequencies but co-located as much as possible to image the same patch of seafloor. This article presents the design, calibration and field testing of a multiple-frequency single-beam echosounder (SBES), mounted on a mechanical pan-and-tilt head. It uses very high transmitting levels to produce non-linear effects and generate harmonics of a 100 kHz fundamental frequency. PZT transducers are used to transmit high acoustic powers and PDVF transducers enable the reception of scattering levels over a very broad frequency band (for the different harmonics). Tank experiments are used to verify effective harmonic generation. The shock distance (at which harmonics are at their maximum level) is measured as 2 m from the transmitter and recommended as the minimum far-field range. Non-linear transmission losses (distinct from linear losses) are calibrated using a full metal sphere 38.1 mm in diameter and of known frequency response, up to ranges commensurate with the depths expected in the field (30 m). The -3 dB beamwidth varies from at 100 kHz to at 300 kHz. Harmonics are used to resolve phase ambiguities in detecting seabed depths. Backscattering strengths are matched to the Generic Seafloor Acoustic Backscatter (GSAB) model to derive the best-fitting parameters. Field validation took place in the Bay of Brest (France) in May 2016, over three different types of seafloor (namely: sandy mud; gravel; gravelly coarse sand with maerl). Additional in situ calibration was used. The echosounder was pointed at angles from (nadir) to by steps. One of the areas surveyed ("Carré Renard"), commonly used for instrument calibration and comparison with other measurements, showed differences 1 dB at 200 kHz. Videos and photographs of the seafloor were used to ground truth interpretations of the curves. The results show that these curves measured with the echosounder are relevant for seabed classification and characterization. The different shapes and levels of BS when compared to ground truth are coherent with the Jackson model. The main limit of this prototype of echosounder is the signal to noise ratio, in particular for high frequency harmonics (kHz). The in situ calibration is unavoidable because of the non-linear parameter variations with water characteristics (temperature, salinity...). Calibrated curves from 100 kHz to 300 kHz can be directly compared to other measurements, for example to calibrate other instruments.

Keywords : Underwater acoustics, Non-linear acoustics, Backscatter strength (BS), Seabed characterization, Single-beam echosounder (SBES)

1 **1. Introduction**

2 Single-beam echosounders (SBES) have been used since the 20th century pri-
3 marily for hydrographic purposes. Their first aim was to achieve bathymetric
4 requirements such as reliable detections of the seabed and precise positioning
5 of the soundings, but more recently, they are also became reference systems
6 for seabed characterisation and classification. Different algorithms have been
7 developed to address the challenges, for example received pulse envelope alter-
8 ation [1][2], or the signal echo modification according to frequency [3]. However,
9 seabed acoustic response depends on the frequency as well as the incidence angle
10 [4][5][6][7]. Therefore, to be discriminant, the acoustic response of the seafloor
11 must be measured according to several incident angles θ and transmitted fre-

12 quencies f . This yields reflectivity or backscattering strengths $BS(f, \theta)$ specific
13 of a seabed type [8].

14 In the context of traditional SBES, the angular issue is solved by mechanically
15 tilting the system even if, obviously, the use of multi-beam echosounders would
16 be more appropriate [9]. As for frequencies, transmitting a large diversity of
17 frequencies implies the use of several systems (single- or multi- beams) on the
18 same vessel, requiring larger vessels and increasing survey costs. Where the
19 angular measurements are practicable, multi-frequency measurements are most
20 often limited by space requirements on board [10].

21 The device presented in this paper is a SBES mechanically tilted to reach angles
22 from 0° (nadir) to 60° . The system is designed to generate multiple frequen-
23 cies perfectly simultaneously with a unique transducer head, a strong asset
24 for seabed characterisation or classification surveys. The generation of these
25 harmonic frequencies is based on the propagation medium's non-linear proper-
26 ties [11][12][13], producing frequencies multiples of the fundamental frequency
27 transmitted (100 kHz here, yielding harmonics at 200 kHz, 300 kHz, etc.). This
28 approach is widely used in medical acoustics and non-destructive inspection [14]
29 but seldom in underwater acoustics, even though the feasibility of characteriz-
30 ing underwater targets thanks to harmonic frequencies was demonstrated e.g.
31 in [15].

32 In Section 2, we shall summarise the underlying theory and present how it in-
33 formed the design of transmitter and receivers, whose non-linear properties are
34 measured in tanks and at sea. Section 3 will explain how acoustic data is pro-
35 cessed to get accurate seabed backscattering strengths $BS(f, \theta)$. Section 4 will
36 present sea trials in the Bay of Brest (France) and compare the results with
37 reference measurements from [16] and with established seabed response models
38 like [17]. Finally, Section 5 will discuss the need for *in situ* calibration and
39 envisageable improvements.

40 **2. Theory, design and validation of a harmonic single-beam echosounder**

41 The non-linear properties of acoustic wave propagation in water [11][13] are
 42 used to generate multiple frequencies with a system classically employed in
 43 underwater acoustics: the SBES. The echosounder described in this paper is able
 44 to generate several isolated frequencies, harmonics of the lower one, perfectly
 45 simultaneous in time and space.

46 *2.1. Using non-linearities in an underwater acoustics context*

47 To generate several frequencies within a single transmitter, we take advan-
 48 tage of the non-linear propagation of acoustic waves in sea water [11][13]. The
 49 principle is based on the 3-D quadratic non-linear equation for fluids in terms
 50 of the acoustic potential $\Phi(\mathbf{X}, t)$ [18][19]:

$$\Delta\Phi(\mathbf{X}, t) - \frac{1}{c_0^2} \frac{\partial^2 \Phi}{\partial t^2} = \frac{2}{c_0} \mathcal{A} \left(\frac{\partial \Phi}{\partial t} \right) + \frac{1}{c_0^2} \frac{\partial}{\partial t} \left[(\nabla \Phi)^2 + (\beta - 1) \frac{1}{c_0^2} \left(\frac{\partial \Phi}{\partial t} \right)^2 \right] \quad (1)$$

51 where \mathbf{X} are the 3-D coordinates and t the propagation time (omitted from
 52 the later expressions of Φ , to simplify the equation); c_0 is the sound speed in
 53 the given fluid (water), and β the non-linear coefficient [20][21]. $\mathcal{A}(\ast)$ is a linear
 54 operator related to attenuation. In water, it takes into account the thermovis-
 55 cous attenuation $-\frac{b}{2\rho_0 c_0^3} \frac{\partial^2 \ast}{\partial t^2}$ [22], in which b is the viscosity coefficient and ρ_0
 56 the density of the medium, and it also accounts for the relaxation [18][23].

57 As the acoustic wave propagates through water, non-linear processes will trans-
 58 fer some energy from the fundamental frequency to its harmonics [13][24][25]. To
 59 observe these non-linear phenomena, the power transmitted needs to be much
 60 higher than with traditional echosounders. This constraint is often a limitation
 61 to using non-linear acoustics. Previous studies and the model by [18] and [26]
 62 helped us to improve the development and design of the echosounder, making
 63 it efficient in terms of acoustic energy for each harmonic frequency.

64 *2.2. Constraint on the transmitter: high power*

65 According to [13], harmonic frequencies appear in the signal during its prop-
66 agation through the medium, when only one single frequency is actually trans-
67 mitted by the transducer. The main constraint, in practice, is that a very high
68 acoustic level must be transmitted into the water, at the transducer head. Elec-
69 tronic components must therefore be able to generate a high amplitude signal
70 and the transducer itself must be designed to support such a high pressure
71 variation on its surface, while avoiding cavitation and the generation of third
72 harmonics when the transmitted signal is not sinusoidal. The transmitter (Tx)
73 developed for this purpose is an 18 cm-diameter disk formed with composite-
74 PZT [27], which resonates at 100 kHz (see figure 1). Its composition and large
75 surface are enough to support high power at 100 kHz, allowing this fundamental
76 frequency to be transmitted. The harmonic frequencies generated during prop-
77 agation are therefore 200 kHz, 300 kHz, etc. The source level estimated from
78 linear measurements of the transmitter sensitivity is 228.5 dB re. $1\mu\text{Pa}$ @ 1m.

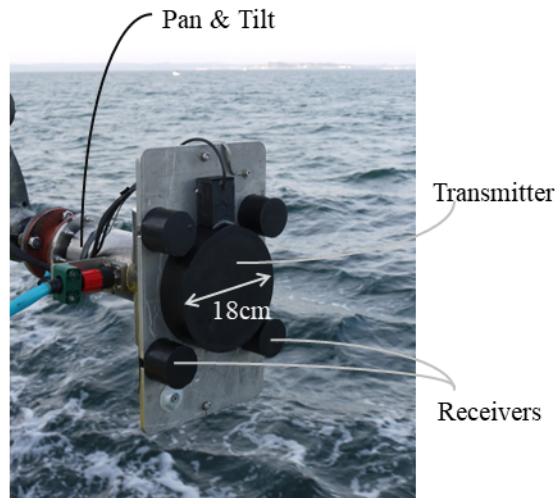


Figure 1: Multi-frequency SBES before a survey, with one transmitting cylindrical transducer in the center, and four receivers spaced 20 cm apart.

79 *2.3. Constraints on the receiver(s): the spread of frequencies*

80 To receive all harmonic frequencies, the receivers must be wide-band. They
81 must also be very sensitive because the harmonic levels could be quite low,
82 especially at very high frequencies. PVDF (Polyvinylidene fluoride) technology
83 [28] respects these criteria and was consequently selected. The receivers (Rx)
84 are in our case made of one layer of PVDF, with a backing formed by a layer of
85 vinyl and a large syntactic foam as background. They have the shape of a small
86 disk 3 cm in diameter to optimise the sensitivity/aperture constraints at high
87 frequencies. Four receivers are placed around the Tx transducer as shown on
88 figure 1. Their vertical spacing is about 20 cm and is useful for seabed detection
89 through interferometry.

90 *2.4. Validation of harmonic frequencies generation*

91 The effective generation of harmonic frequencies with the selected transducer
92 shape and material is done by measuring the harmonic levels at several ranges
93 from the transmitter in fully-controlled environments. These measurements
94 were done in two tanks: one 10 m-long and filled with fresh water (at Sorbonne
95 University, Paris, France), and one 35 m-long filled with sea water (at Ifremer,
96 Brest, France). The experiments both consisted in emitting a continuous wave
97 (CW) with the Tx transducer of figure 1 and receiving the direct-signal with
98 a calibrated hydrophone Reson TC4034. Measurements were obtained every 2
99 or 3 meters in the small tank, and every 5 meters in the large tank. The level
100 $L(r)$ of each harmonic, depending on the range r is calculated using a band-pass
101 filter. Results are shown on figure 2. We can perfectly observe the creation of
102 the harmonic along the range before the shock distance L_c [18] (around 2 m)
103 where their levels are increasing. After the shock, the levels decrease with
104 range, i.e. it is a transmission loss, mainly due to the geometrical divergence of
105 the signal within the medium. The attenuation is close to negligible on these
106 short distances (around 3 dB/km in fresh water and 33 dB/km in salt water).
107 We can notice a minute inflection at 10 m. This is explained by the different

	Small tank	Large tank	Survey at sea
Type of water	Fresh water	Salt water	Salt water
Sound speed (c_0)	1450 m/s	1498 m/s	1499 m/s
Water density	1000 kg/m ³	1028 kg/m ³	1027 kg/m ³
Temperature	9.8 °C	11.8 °C	12.3 °C
Salinity	0 psu	37 psu	36 psu
Particles in suspension	None Clear water	None Clear water	A lot Turbid water
β (dimensionless)	3.35	3.59	[3.59 ; 3.60]

Table 1: Characteristics of the water in the tanks and during the sea trials, measured *in situ*. The non-linear coefficient β is estimated with the empirical Blackstock formula [26][29] from the measurements of temperature and salinity. Because acoustics measurements in tanks were done horizontally i.e. the SBES axis crossed only one layer of water, the non-linear coefficient is constant during propagation. However, at sea, measurements are done vertically or while tilting the SBES, therefore its axis crossed several layers of water of different composition. The non-linear coefficient consequently varies during the propagation, and it is therefore given as a range of values.

108 water conditions between each tank. The respective characteristics of these two
109 environments are contrasted with conditions during the sea survey in table 1.

110 These different sets of measurements show that, in each environment, the
111 transmitter effectively and efficiently creates harmonic frequencies. The results
112 also show the importance of knowing where the shock appears, i.e. when the
113 harmonics are at their maximum levels. This is as important as knowing the
114 far-field distance, in an operational point of view. Indeed, for ranges lower than
115 L_c , measurements are not recommended as all the harmonic frequencies are not
116 fully generated. This distance is therefore a characteristic of the multi-frequency
117 echosounder and needs to be kept in mind by future users.

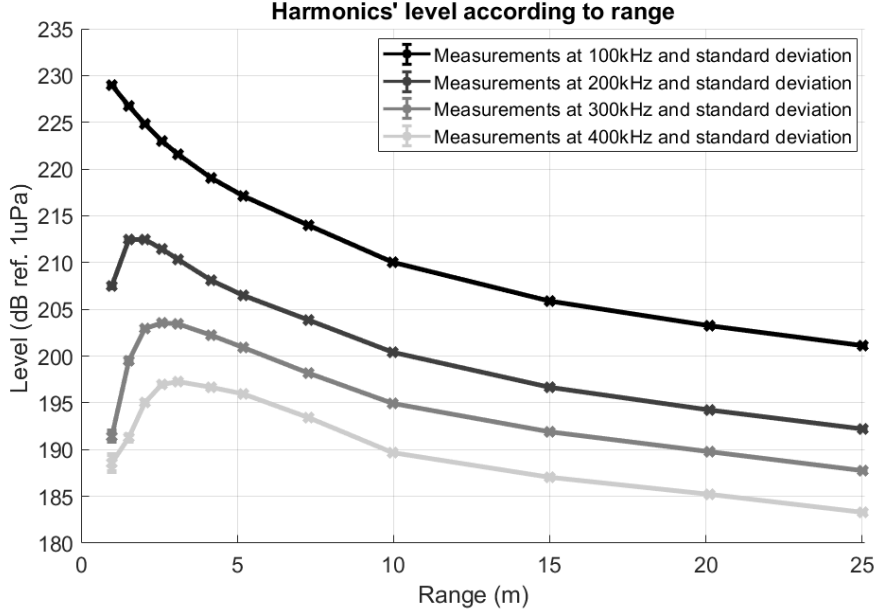


Figure 2: Measurements of the generation of harmonic frequencies in a small ($< 10 m$) freshwater tank and in a large ($\geq 10 m$) salt water tank, according to the range from the transmitter with the maximum level at emission. At each range, 100 measurements are averaged. Associated standard deviations are not very noticeable because they are all < 0.9 dB.

118 *2.5. Directivity patterns and equivalent beam apertures*

119 To estimate the reflectivity level of the seafloor at different incidence angles,
 120 we need to know the directivity pattern $D(f, r, \varphi)$ of the echosounder to calculate
 121 its equivalent beam aperture $\phi(f, r)$ for each frequency. The combined two-way
 122 directivity $10 \log(D(f, r, \varphi))$ is measured in the tanks for different ranges r from
 123 the echosounder, pointing angles $\varphi \in [-15^\circ; +15^\circ]$, and they are calculated for
 124 each frequency f . Figure 3 shows the directivity patterns at $r = 20 m$ for
 125 the fundamental frequency of 100 kHz and the first harmonics at 200 kHz and
 126 300 kHz. We can observe the variations of the main beams' aperture according
 127 to frequency [30], and also asymmetries of the side-lobes, mainly due to the
 128 layout of the PZT component of the transducer (in spiral).

129 The equivalent aperture $\phi(f, r)$ of the echosounder is calculated for each fre-
 130 quency by integrating the corresponding measured directivity patterns [31] (fig-
 131 ure 3). When measuring the directivity patterns for different r and plotting
 132 their equivalent apertures $\phi(f, r)$ we obtain the results of figure 4, showing the
 133 increase of beamwidths with range. At 100 kHz, they vary from 6.3° at 10 m to
 134 6.8° at 30 m, at 200 kHz from 4.0° at 10 m to 4.6° at 30 m and at 300 kHz from
 135 3.1° at 10 m to 3.9° at 30 m.

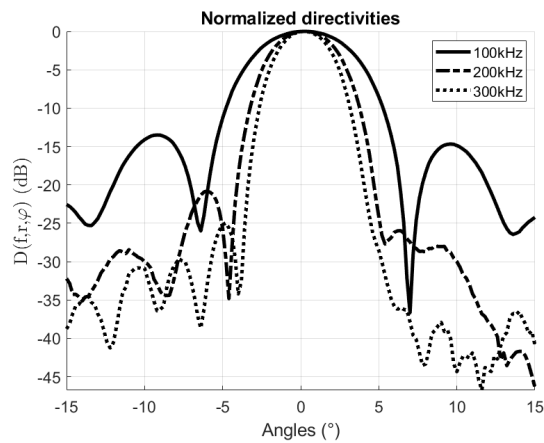


Figure 3: Measured directivity patterns $10 \log(D(f, r, \varphi))$ at $r = 20 \text{ m}$ for $f = 100 \text{ kHz}$, $f = 200 \text{ kHz}$, $f = 300 \text{ kHz}$. At each angle, 4 measurements are averaged. Standard deviations σ stand in the following interval for each frequency: $\sigma_{100 \text{ kHz}}(\varphi) \in [2.6; 6.1] \text{ dB}$, $\sigma_{200 \text{ kHz}}(\varphi) \in [2.0; 7.3] \text{ dB}$, $\sigma_{300 \text{ kHz}}(\varphi) \in [2.3; 6.7] \text{ dB}$.

136 2.6. Measurements of the operating gain and range variations

137 The echosounder aims to measure the absolute acoustic response of the
 138 seabed. It is therefore essential to evaluate: 1) its total operating gain ac-
 139 cording to frequency, $G(f)$, due to electrical connections, processing, etc., and:
 140 2) the transmitted level to which is directly related a specific decrease of each
 141 harmonic with range as observed in section 2.4. In the case of backscatter mea-
 142 surements, we include both the transmit level and its decrease during two-way
 143 propagation, expressed as a variable noted $\mathcal{L}(f, r)$. Indeed, because of non-linear
 144 propagation, acoustic forward transmission losses $TL_{fw}(f, r)$ to the target differ

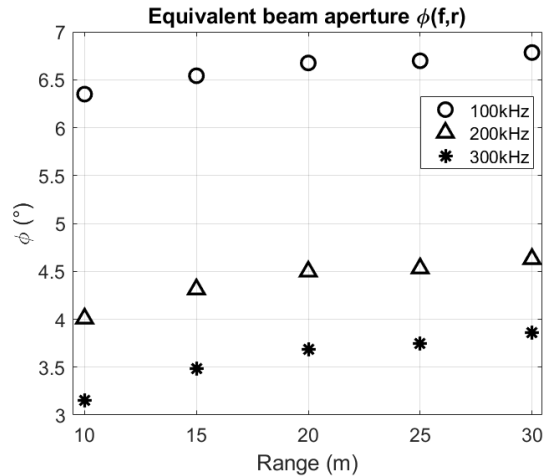


Figure 4: Equivalent beam apertures $\phi(f, r)$ of the main lobe according to range and frequency, calculated from the directivity patterns measured between 10 m and 30 m.

145 from the classical, linear model (proportional to $20 \log r + \alpha r$ [31] with α the lin-
 146 ear attenuation coefficient). Likewise, the operating gain cannot be calculated
 147 either with linear theoretical formulae [32].

148 For practical use, we propose to create look-up tables of each gain and frequency
 149 level according to the range: $G(f) + \mathcal{L}(f, r)$, that will be used to calculate the
 150 seabed response (sonar equation) in place of all the unknown parameters (see
 151 equation 2). This can be achieved with measurements on a calibrated target
 152 [33][34], moved along the axis of the echosounder. The principle is to compare
 153 the received backscattering level of the controlled point target with its actual
 154 target strength $TS(f)$ whose frequency spectrum is perfectly known [35]. The
 155 target used for our measurements is a full-metal sphere (tungsten, carbide and
 156 cobalt) of diameter 38.1 mm, chosen because its frequency responses have no
 157 anti-resonance at the frequencies we use (respectively 100 kHz, 200 kHz, 300
 158 kHz). The final outcomes are look-up tables of $G(f) + \mathcal{L}(f, r)$ according to
 159 range and frequency. For our objective, the sphere is moved from 10 m to 30 m
 160 range which gives a sufficient range of look-up tables for surveys in the Bay of
 161 Brest (depths $\leq 30m$) (and of course, for larger depths, the calibration should

162 increase to similar ranges). For this experimental setup, the associated sonar
 163 equation is:

$$20 \log (V_{Rx}(f, r)) = 20 \log (V_{Tx}(f)) + S_h(f) + S_v(f) \\ + 10 \log (D(f, r, \varphi)) - TL_{fw}(f, r) - TL_{bw}(f, r) + TS(f) + G_o(f) \quad (2)$$

164 with f the harmonic frequency, V_{Rx} and V_{Tx} respectively the received and
 165 transmitted voltages, S_h and S_v respectively the receiver and transmitter sen-
 166 sitivities, $D(f, r, \varphi)$ is the combined directivity function at transmission and
 167 reception, φ the angle in the beam (i.e $D(f, r, \varphi = 0^\circ) = 1$ on the beam-
 168 axis), TL_{fw} and TL_{bw} respectively the transmission losses forward (from the
 169 transmitter to the sphere) and backward (from the sphere to the receiver),
 170 and $G_o(f)$ encompasses the electrical gains. Because of the non-linear oper-
 171 ation of the echosounder, the perfectly known parameters are only $V_{Rx}(f, r)$,
 172 the target strength of the sphere $TS(f)$ (i.e. its backscattering cross section
 173 [36]) and $D(f, r, \varphi)$. Measurements on the target are done on the axis of the
 174 echosounder so that $10 \log (D(f, r, \varphi)) = 0$. Consequently, we can define the
 175 difference $20 \log (V_{Rx}(f, r)) - TS(f)$ as the sum of an operating gain $G(f)$ and
 176 a level range variations $\mathcal{L}(f, r)$ such as:

$$G(f) + \mathcal{L}(f, r) = 20 \log (V_{Rx}(f, r)) - TS(f) \quad (3)$$

177 Measured $G(f) + \mathcal{L}(f, r)$ and their corresponding best-fitting curves used as
 178 look up tables are shown for the fundamental frequency and its 2 first harmonic
 179 on figure 5. Finally, $G(f) + \mathcal{L}(f, r)$ contains the propagation losses, Tx and Rx
 180 sensitivities, the fixed transmit level $20 \log (V_{Tx}(f))$, electrical gains, and signal
 181 processing gains of the echosounder we wished to estimate, and that will be
 182 useful for seafloor reflectivity calculations.

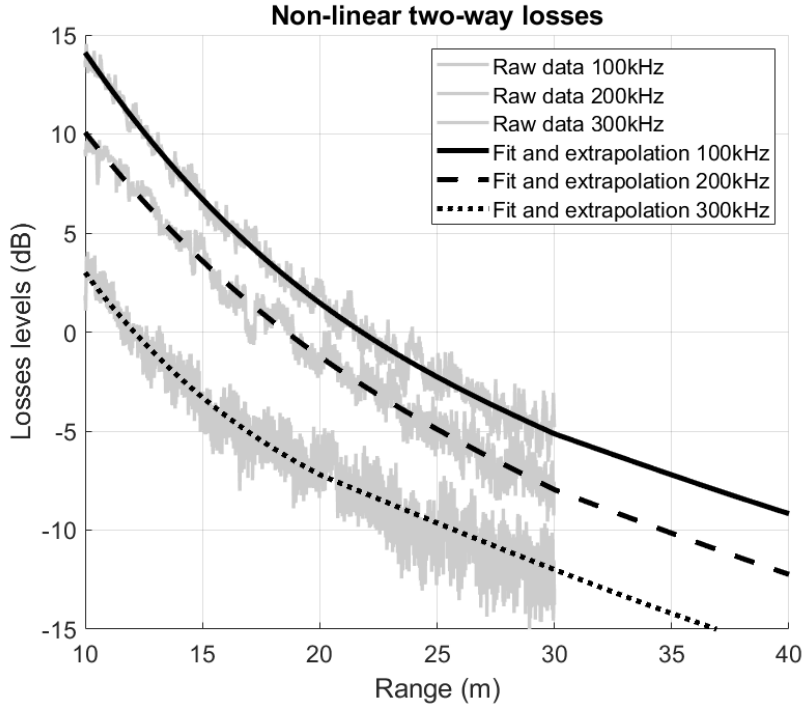


Figure 5: Grey: measurements of $G(f) + \mathcal{L}(f, r)$ in the large tank of Ifremer (sea water) according to the range from the echosounder in operational mode (i.e. with the maximum level at emission). Black: best-fitting curves used as look-up tables.

183 3. Seabed reflectivity processing

184 Raw data from the multi-frequency echosounder are time-sampled values of
 185 received levels $20 \log(V_{Rx}(r))$, with $r = ct/2$, in which t is the listening time,
 186 i.e. the time after emission of the signal. Signals for each harmonic frequency
 187 are extracted thanks to a band-pass filter and noted $20 \log(V_{Rx}(f, r))$. The
 188 transmit signal, also called pulse, is a 100-kHz sine wave of duration T . Each
 189 harmonic received signal is perfectly in-phase and investigated separately. From
 190 these received time signals, the echo of the seabed is detected and its reflectivity
 191 index, or backscattering strength $BS(f, \theta)$, is computed (in decibels) as:

$$\begin{aligned}
BS(f, \theta) &= 20 \log(V_{Rx}(f, r)) - 20 \log(V_{Tx}(f)) - S_h(f) - S_v(f) \\
&- 10 \log(D(f, r, \varphi)) + TL_{fw}(f, r) + TL_{bw}(f, r) - G_o(f) - 10 \log(A(f, \theta)) \quad (4)
\end{aligned}$$

192 with θ the incidence angle on the seabed, $D(f, r, \varphi)$ the directivity (combin-
193 ing Tx and Rx) of the echosounder for the frequency f at the range r taken at
194 the angle $\varphi = \cos^{-1}(h/r)$ the angle of the sample in the beam (with h the water
195 height at nadir on a supposed flat seabed), $TL_{fw}(f, r)$ and $TL_{bw}(f, r)$ respec-
196 tively the transmission losses forward (from the transmitter to the seabed) and
197 backward (from the seabed to the receiver), and $A(f, \theta)$ the insonified area on
198 the seafloor (see section 3.2). Directivity patterns of the echosounder $D(f, \varphi)$
199 for each frequency are also measured in the tanks with hydrophones, at varying
200 range (their apertures slightly change during propagation). Using the look-up
201 tables of $G(f) + \mathcal{L}(f, r)$ computed in section 2.6, we can write:

$$BS(f, \theta) = G(f) + \mathcal{L}(f, r) - 10 \log(D(f, r, \varphi)) - 10 \log(A(f, \theta)) \quad (5)$$

202 where $r = h / \cos(\theta)$ is the flat seabed approximation linking r and θ .

203 3.1. Bottom echo detection

204 The sounding (i.e. the time-sample of the seafloor-echo coming from the
205 center of the echo-sounder beam) is detected with two methods, depending on
206 the incidence angle [16]: 1) on the center of gravity computed on the intensity
207 values for angles near the nadir, 2) from phase differences, thanks to the receivers
208 vertically aligned for other angles. The sounding range is noted r_s and its
209 equivalent received time $t_s = 2r_s/c$. We can note that the seafloor echoes of
210 the harmonic frequencies are in some cases very useful to improve detection
211 (for example in case of phase ambiguities, due to the relatively large distance
212 between two receivers) because the phase ramp at high frequencies is shorter
213 and steeper than that of the fundamental frequency, because of their shorter
214 beamwidths. Around the sounding sample, indexed by i , several time-samples

215 are retained (this is the equivalent of the "snippets" of multibeam echosounders
 216 [37] [38]). They are averaged to compute $BS(f, \theta)$ for one ping. As in [16],
 217 samples i are retained when the condition $\varphi_i \in [-1^\circ; +1^\circ]$ is valid with φ the
 218 angle of the samples in the beam.

219 3.2. Insonified area

220 The insonified area is calculated thanks to a geometrical model using the
 221 echosounder equivalent along-track ϕ_{al} and across-track ϕ_{ac} beam apertures
 222 [31], the incidence angle θ , and the effective pulse length T_{eff} (defined below)
 223 which takes into account the signal loss of energy during transmission. In our
 224 case, ϕ_{al} and ϕ_{ac} both equal the equivalent beam aperture measured in section
 225 2.5 because of the SBES symmetry, i.e. $\phi_{al} = \phi_{ac} = \phi(f, r)$. The insonified
 226 area model is composed of two regimes, near-nadir and oblique-angle, such as
 227 [39] (assuming the slope along-track is flat):

$$A(f, \theta) = \min \left(\pi \frac{r^2}{\cos \theta} \left(\frac{\phi(f, r)}{2} \right)^2, \frac{cT_{\text{eff}}(f)}{2 \sin \theta} . r . \phi(f, r) \right) \quad (6)$$

228 The effective pulse lengths are computed for each frequency by measuring the
 229 difference of acoustic energy between the desired rectangular pulse and the pulse
 230 actually transmitted by the echosounder. Indeed, when the pulse is transmitted
 231 by the Tx transducer, its bandwidth creates transitory effects on the shape of
 232 the signal. The energy of the signal actually transmitted is therefore lower than
 233 the perfect rectangular pulse energy given electronically to the transducer. This
 234 difference of acoustic energy is taken into account by using an effective pulse
 235 length T_{eff} whose amplitude is unity and whose energy is proportional to the
 236 theoretical pulse energy by a factor called Sa_{corr} in [16] and [35], defined as:

$$10 \log(T_{\text{eff}}(f)) = 10 \log(T(f)) + Sa_{\text{corr}}(f) \quad (7)$$

237 with $T(f)$ the theoretical signal duration chosen by the user at $T(100 \text{ kHz}) =$
 238 $600 \mu\text{s}$. Values of $Sa_{\text{corr}}(f)$ and $(T_{\text{eff}}(f))$ are given in table 3.2 for the fundamental
 239 frequency (100kHz) and the first two harmonics (200 kHz and 300 kHz).

Frequencies	100 kHz	200 kHz	300 kHz
$Sa_{\text{corr}}(f)$	-0.37 dB	-0.49 dB	-1.03 dB
$T_{\text{eff}}(f)$	551 μs	536 μs	473 μs

Table 2: Proportionality coefficient $Sa_{\text{corr}}(f)$ between the theoretical pulse energy and the effective pulse energy, measured in the tanks for the fundamental frequency (100 kHz) and the first two harmonics (200 kHz and 300 kHz). Effective pulse lengths are associated to these values.

240 3.3. Resulting $BS(f, \theta)$ measurements

241 To estimate the backscattering strength (i.e. the $BS(f, \theta)$ curves) of a given
242 seabed, the SBES has to be tilted mechanically to reach discrete incidence angles
243 $\theta_j \in [0^\circ, 5^\circ, 10^\circ, \dots, 60^\circ]$. This is obtained with the pan & tilt device shown in
244 figure 1. On a given surveyed area, 150 pings are recorded for each tilting
245 angle. As recommended in [16], seabed samples i of each ping are retained to
246 be part of a $BS(f, \theta_j)$ value (average) when their incidence angle on the seafloor
247 $\theta_i = \theta_s + \varphi_i + \gamma_s$ is included in the interval $[-1^\circ; +1^\circ]$ around the desired angles
248 θ_j , i.e. :

$$BS(f, \theta_j) = 10 \log \left(\frac{1}{N} \sum_{i=1}^N \sigma_{BS}(f, \theta_i) \right) \text{ if } \theta_i \in [\theta_j - 1^\circ; \theta_j + 1^\circ]$$

where $\theta_i = \theta_s + \varphi_i + \gamma_s$ (8)

249 with $\sigma_{BS}(f, \theta_i) = 10^{BS(f, \theta_i)/10}$, θ_s the incidence angle of the sounding on
250 the seafloor ($\cos \theta_s = h/r_s$), φ_i the angle of the time-sample i in the beam (with
251 respect to the axis), γ_s the roll values at the time of the sounding s , and N the
252 number of samples i that respect the condition $\theta_i \in [\theta_j - 1^\circ; \theta_j + 1^\circ]$.

253 During our survey, the sea was perfectly calm (World Meteorological Organi-
254 sation Sea State Code 0) and the roll of the ship was always $< \pm 1^\circ$ so that
255 almost all values were averaged. We consequently obtain $BS(f, \theta)$ values for all
256 incidence angles θ_j from 0° to 60° with a step of 5° .

257 *3.4. Fitting the $BS(f, \theta)$ curves*

258 In the following, the discrete measurements $BS(f, \theta_j)$ are fitted with the
259 heuristical model GSAB (Generic Seafloor Acoustic Backscatter) for seafloor
260 backscattering strength [40], to get seabed $BS(f, \theta)$ curves that can be anal-
261 ysed in section 4. The model describes the BS into three parts thanks to six
262 parameters [41]:

$$BS(\theta) = \left(A. \exp\left(-\frac{\theta^2}{2B^2}\right) + C. \cos^D(\theta) + E. \exp\left(-\frac{\theta^2}{2F^2}\right) \right) \quad (9)$$

263 with A regulating the specular amplitude, B controlling the angular width of
264 the specular regime, C giving the average backscatter level at oblique incidence,
265 D being the angular decrement of the backscatter (equal to 2 for Lambert law),
266 E the transitory maximum level and F its angular half-extent.

267 **4. Sea trials and results**

268 Sea trials took place in the Bay of Brest (France) in May 2016 aboard R/V
269 *Thalia* of Ifremer. Three areas with distinct seafloor types (see section 4.1) were
270 surveyed in order to demonstrate the feasibility of discriminating seabeds with
271 our echosounder. The SBES was mounted on a pole on the starboard side of
272 the vessel (see figure 1). A pan&tilt system was used to tilt the sounder at
273 several angles, from 0° (nadir) to 60° , with a 5° step. At each angle, data were
274 acquired while the vessel was drifting slowly. This drift ensured a minimum of
275 acoustic noise from the vessel's engines or electrical on-board devices, because
276 the sounder was a prototype and therefore not fully fitted with filters against
277 other types of acoustic noise. The calm weather during the survey ensured the
278 vessel drifted for a distance short enough to assume the seafloor is the same for
279 all pings.

280 *4.1. Area descriptions*

281 Measurements were done onto three areas of the Bay of Brest chosen for
282 their distinct seabed types (see map on figure 6). Area 1 is at the mouth of the

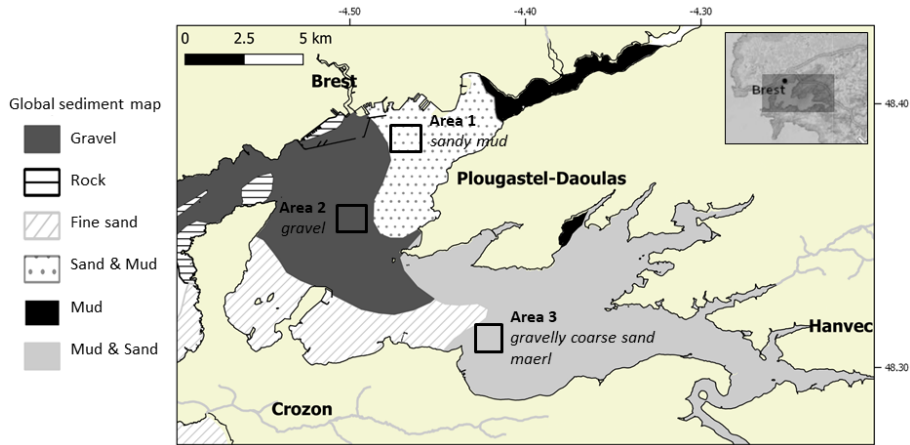


Figure 6: Areas surveyed in the Bay of Brest (France). The global sediment map comes from data.shom.fr (www.shom.fr/HOM/GEOL_SEDIM_MONDIALE) and land information come from geo.data.gouv.fr. At the time of the survey, the water heights were constant for all pings: $h = 20.5\text{ m}$ for Area 1, $h = 17\text{ m}$ for Area 2, and $h = 31\text{ m}$ for Area 3.

283 small Elorn river. Area 2 is in the so-called "Carré Renard", a plateau in the
 284 center of the Bay and also a well-surveyed area for echosounder calibration [16].
 285 Finally, Area 3 is at the mouth of another small river, the Aulne. According
 286 to the morpho-sedimentological map in [42], created from [43] and [44], Area 1
 287 is composed of "sandy mud" or "muddy sand", Area 2 is mostly "gravel" with
 288 rare pebbles, and Area 3 is composed of "gravelly coarse sand" with maerl and
 289 episodic rocks. During the survey, videos and photographs of the seafloor were
 290 taken in these areas (cf. figure 7). They show sand and mud in Area 1, pebbles
 291 and brittle-stars in Area 2, and a hard seafloor (rock) and a large amount of
 292 shells in Area 3.

293 4.2. Raw results

294 The raw results take the form of several $BS(f, \theta)$ curves for frequencies of
 295 100 kHz and above, for all 3 areas surveyed. At first, we compare on figure 8 the
 296 results at the fundamental frequency (100 kHz) for the different areas. Crosses,
 297 triangles and circles show the raw measurements (averages of acoustic intensity

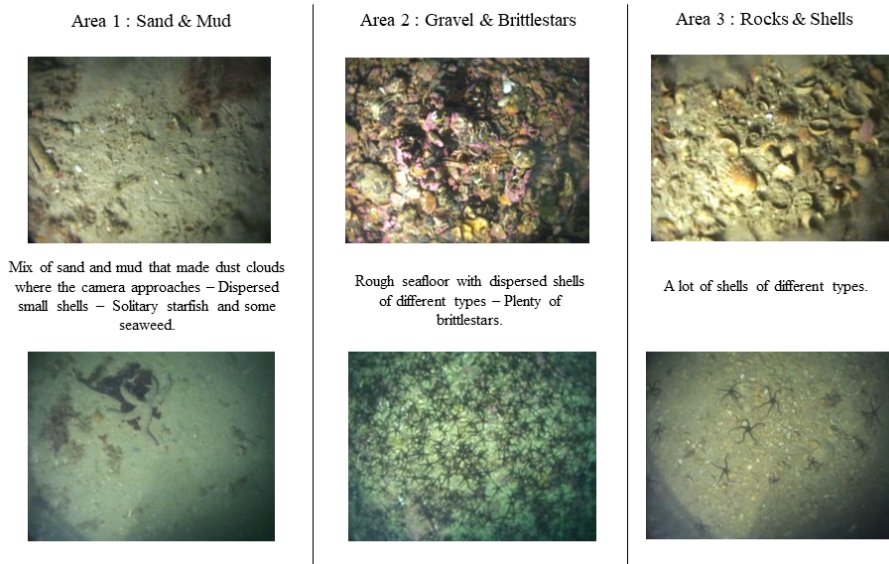


Figure 7: Seafloor photographs in the three areas studied, taken during the survey, with visual descriptions. Data collected by the authors.

298 values) and lines show the fit of the GSAB model to these measurements. We
 299 observe differences in shape and level according to the areas, as expected. Area
 300 3 has a hard and rough seafloor; correspondingly, the $BS(f, \theta)$ curve has a
 301 generally low level and is flattened at the nadir angles. Conversely, the curve
 302 of Area 1 (sandy/muddy seafloor) has a very large range of levels, from -6.4 dB
 303 at 0° to -26.8 dB at 60° , and a high specular level. The curve of Area 2 is in
 304 between those two descriptions, with a high global BS level but a medium range
 305 of BS values according to incidence angles and a visible specular regime, not as
 306 strong as Area 1. These effects of specular flattening are commonly observed
 307 [45][46][47] when the seabed rugosity changes from structures finer than the
 308 wavelength (like sand or mud at 100 kHz) to macro-structures close or larger
 309 than the wavelength (like pebbles, rocks). The specular shape can disappear,
 310 like for Area 3, on hard seafloor, as demonstrated e.g. by [17] (roughness effect).
 311 We can also compare (see figure 9) raw results in one area for the fundamental
 312 frequency (100 kHz) with two of its harmonic frequencies (namely 200 kHz and

313 300 kHz). We observe frequency variations where, in particular, the shapes of
 314 the $BS(f, \theta)$ curves are modified, mostly on the specular parts which decrease
 315 with frequency and where Bragg backscattering [31] for grazing angles inversely
 316 increases.

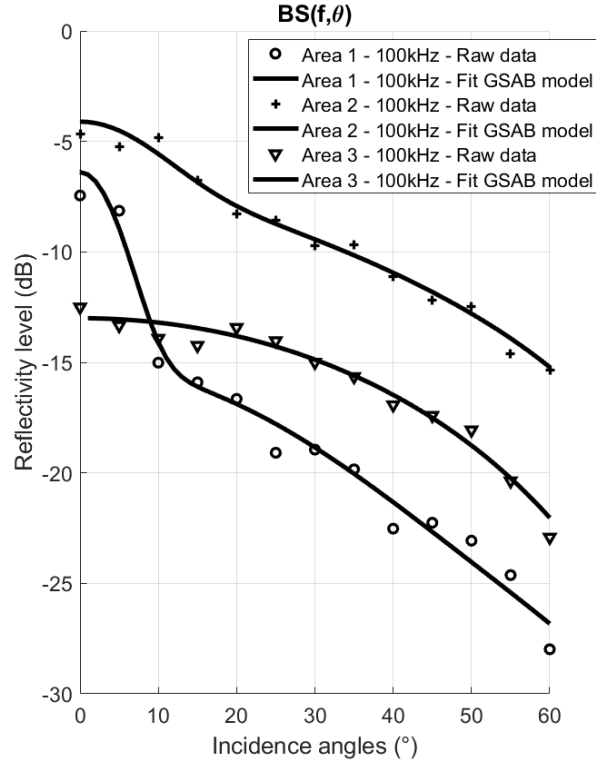


Figure 8: $BS(f, \theta)$ curves of the fundamental frequency 100kHz on the three areas surveyed: (1) sand & mud, (2) pebbles & brittle-stars, (3) hard seafloor (rocks) & shells. The raw measurements are respectively indicated with crosses, triangles and circles. The lines correspond to the respective GSAB model model fits.

317 4.3. Calibration on reference Area 2 ("Carré Renard")

318 Data were acquired in area 2 because it is a known reference area for
 319 echosounder calibration [16], and it was therefore possible to compare our re-
 320 sults to reference curves noted $BS_{\text{ref}}(f, \theta)$. Our Ifremer colleagues kindly shared

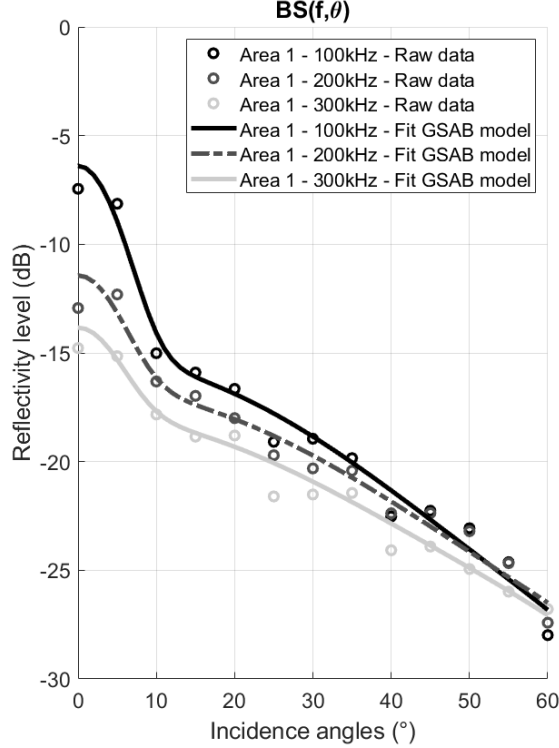


Figure 9: $BS(f, \theta)$ curves of the fundamental frequency (100 kHz) and two harmonics (200 kHz and 300 kHz) on Area 1 (sand & mud). The raw measurements are indicated with circles and the GSAB model fits with lines.

321 two reference curves at 200 kHz and 333 kHz, reported in [16]. Their 200-
322 kHz curve $BS_{\text{ref}}(200 \text{ kHz}, \theta)$ can be usefully compared to our measurements of
323 $BS(200 \text{ kHz}, \theta)$. The 333-kHz curve can be used with caution to compare with
324 our own measurements at 300 kHz. The comparison is plotted as the difference
325 $BS_{\text{ref}}(f, \theta) - BS(f, \theta)$ according to incidence angles for 200 kHz and 300 kHz
326 respectively on figures 10 and 11. We see that those differences follow a curve
327 whose shape can be explained by several biases. The first one is visible in the
328 range variations ($\mathcal{L}(f, r)$) estimated in section 2.6, which can appear because of
329 a difference in water composition (salinity) or turbidity between the measure-
330 ments in the tanks and *in situ* (see table 1) that may impact the generation of

331 non-linearities [48][49] and therefore the levels of harmonic frequencies. The sec-
 332 ond bias is due to the difference of variation of β during the propagation. Indeed,
 333 the Tx signal propagates horizontally in the tanks and vertically or obliquely
 334 during the survey. Thus, whereas the non-linear coefficient is constant along
 335 the propagation in tank, it is variable *in situ*, introducing modification in the
 336 harmonic generation and sustain. A last bias comes from slight errors in the op-
 337 erating gain $G(f)$, from *in situ* sensitivity variations, electronics or processing
 338 adjustments. Thanks to the references curves, these biases can be quantified
 339 *in situ* and properly accounted for. Thus, the difference between the reference
 340 curve $BS_{\text{ref}}(f, \theta)$ and the raw-results for each incidence angle $BS(f, \theta)$, noted
 341 $G_{\text{corr}}(f) + \mathcal{L}_{\text{corr}}(f, \theta) = BS_{\text{ref}}(f, \theta) - BS(f, \theta)$, is a correction which added to
 342 the $BS(f, \theta)$ calculation in equation 5, gives:

$$\begin{aligned}
 BS_{\text{calib}}(f, \theta) = & G(f) + G_{\text{corr}}(f) + \mathcal{L}(f, \theta) + \mathcal{L}_{\text{corr}}(f, \theta) \\
 & - 10 \log(D(f, h/\theta, \varphi)) - 10 \log(A(f, \theta)) \quad (10)
 \end{aligned}$$

343 The value $BS_{\text{calib}}(f, \theta)$ obtained after calibration on Area 2 is the absolute
 344 reflectivity level of this area. This calibration is done for the two frequencies of
 345 which reference reflectivity curves are available: 200 kHz and 300 kHz.

346 To apply the calibration to the other areas, we have to transform incidence
 347 angles to range, thanks to the measurements of echosounder altitude (i.e. the
 348 range h at nadir): $r = h / \cos(\theta)$. This gives a correction $G_{\text{corr}}(f) + \mathcal{L}_{\text{corr}}(f, r =$
 349 $h / \cos(\theta))$, function of range, and we can therefore calibrate the $BS(f, \theta)$ curves
 350 of each area by doing the same transformation. At the end, we obtain calibrated
 351 reflectivity curves of the three areas, shown in figure 12. We can see that the
 352 shape of the curves discriminate clearly between the different seafloor types,
 353 and also that the variations of those shapes for one area with frequency is not
 354 the same for each seabed type.

355 The raw results (figure 8 and 9) and the calibrated results (figure 12) al-
 356 low us to conclude that the curves $BS_{\text{calib}}(f, \theta)$ obtained with the harmonic
 357 frequencies are able to discriminate seabed responses according to incidence an-

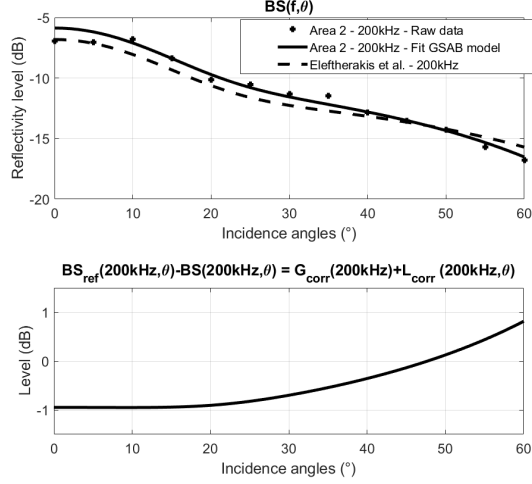


Figure 10: Top: $BS(f, \theta)$ curves for harmonic frequency 200 kHz on Area 2 (pebbles & brittle-stars). Raw measurements are indicated with crosses; the full line shows the GSAB model fit [31]; the dashed line corresponds to $BS_{\text{ref}}(200\text{kHz}, \theta)$ curves from [16] on the same area. Bottom: gain and range variation corrections, i.e. differences $BS_{\text{ref}}(200\text{kHz}, \theta) - BS(200\text{kHz}, \theta) = G_{\text{corr}}(f) + \mathcal{L}_{\text{corr}}(200\text{kHz}, \theta)$ between the reference reflectivity curve and the raw results.

358 gles and their absolute levels. Indeed, clear differences are observed between
 359 responses of seabed from the 3 areas surveyed that correspond to variations of
 360 the seabed composition. Also, modifications of the curve shape are observed
 361 between frequency responses like in Area 1 (sand & mud). These results clearly
 362 show the interest of multi-frequency single-beam echosounders for seafloor char-
 363 acterisation. They also demonstrate the importance of clearly mapping the
 364 characteristics of the instrument, in controlled tank environments and through
 365 a full and thorough calibration *in situ*.

366 5. Discussion

367 5.1. *In situ* calibration

368 The results of the calibration on the reference area show the clear neces-
 369 sity of a calibration *in situ* to obtain absolute reflectivity levels. Preliminary

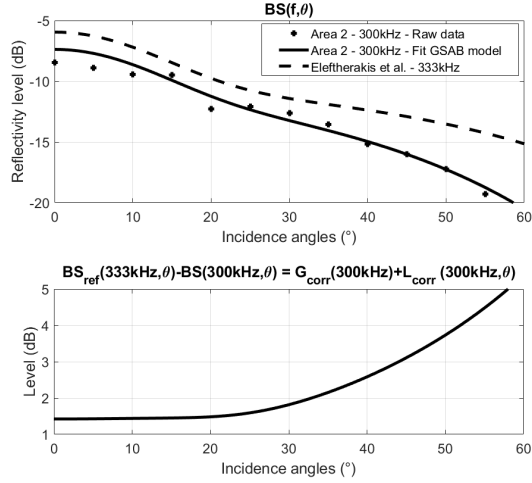


Figure 11: Top: $BS(f, \theta)$ curves for harmonic frequency 300 kHz on area 2 (pebbles & brittle-stars). Raw measurements are indicated with crosses; the full line shows the GSAB model fit [31]; the dashed line shows the $BS_{\text{ref}}(333\text{kHz}, \theta)$ curves from [16] on the same area. Bottom: gain and range variation corrections, i.e. difference $BS_{\text{ref}}(333\text{kHz}, \theta) - BS(300\text{kHz}, \theta) = G_{\text{corr}}(f) + \mathcal{L}_{\text{corr}}(300\text{kHz}, \theta)$ between the reference reflectivity curve and the raw results.

370 tank measurements are essential to characterise the entire instrument, through
 371 parameters like its directivity, the effective pulse length, electrical gains, es-
 372 sential to calculate the backscattering strength. In our case, they were also
 373 extremely useful to validate the generation of harmonics, and determine the
 374 shock distance. The calibration is essential to measure the true seafloor acous-
 375 tic responses of multiple areas, and ultimately this harmonic echosounder can
 376 be used as a reference system to calibrate other sounders, from single-beam to
 377 multibeam.

378 5.2. Seafloor acoustic characterisation and classification

379 Our prototype multi-frequency SBES uses non-linear acoustics to generate
 380 several harmonic frequencies. The seafloor reflectivity variations presented in
 381 section 4, as a function of incidence angles and for several frequencies, are fully
 382 consistent with the generic acoustic responses studied and modeled by Jackson
 383 in [47] and [50]. Even if the frequencies used in this article are mostly beyond

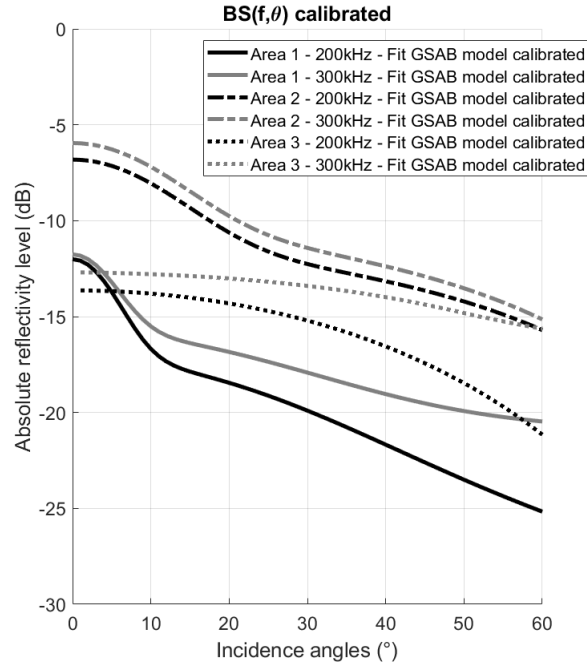


Figure 12: Absolute $BS_{\text{calib}}(f, \theta)$ curves after calibration for the 3 areas and the two first harmonics 200kHz and 300kHz.

384 the original validity domain of this model (up to 100 kHz), other studies (e.g.
385 [51][52]) already show it can be safely extended up to 240 kHz. The acoustic
386 response of a sandy-muddy seabed cover a large range of BS values from the
387 nadir to the grazing angles and generate a strong specular effect, whereas a
388 hard and rough seabed like rock has a flat response with a specular nonexistent.
389 These variations are found in our results (see figure 12) and give us confidence
390 that classification and characterisation of seabed types are feasible solutions
391 with the harmonic single-beam echosounder. The frequency variations of the
392 seabed responses are a major point for classification because it adds a lot of
393 information. The possibility to measure several frequency responses simultane-
394 ously and therefore perfectly on the same seabed is a real asset of this type of
395 echosounder.

396 5.3. Improving the non-linear echosounder

397 This multi-frequency SBES allows the concurrent use of three frequencies at
398 once (central frequency of 100 kHz and two harmonics at 200 kHz and 300 kHz
399 respectively), using a CW signal at transmission. By improving the system
400 and specifically its signal-to-noise ratio, our next improvements will aim to
401 access higher harmonics at 400 kHz, 500 kHz etc., providing more information on
402 seabed types. The use of much higher frequencies (and therefore access to much
403 smaller wavelengths) will also prove an asset for the imaging of less reflective
404 targets like marine vegetation. Some types of macrophytes have limited gas
405 content in their leaves and blades, but are detectable by using higher frequencies
406 (≥ 400 kHz). This multi-frequency SBES, augmented with its pan & tilt system,
407 can therefore prove very useful for studies of marine vegetation (in particular the
408 mapping of canopy heights and the quantification of biomass) [53]. It can also
409 be advantageously used for fisheries application, using the frequency-response
410 of particular fish species or plankton (e.g [54] [55]). Other small-scale targets
411 would also become more accessible, like gas bubbles in the water column above
412 gas seeps or small oil inclusions in oil spills.

413 To be more efficient in measuring seabed acoustic responses curves, we can think,
414 in future developments, about a system which could be able to generate beams
415 simultaneously at a series of incident angles, such as a multi-beam echosounder
416 [46], and following the first works at low frequency of [56] and [57].

417 6. Conclusion

418 The use of different technologies have enabled the development of a multi-
419 frequency single-beam echo-sounder (SBES), using non-linear acoustics to trans-
420 mit several harmonic frequencies. Our design generates a central frequency at
421 100 kHz and several harmonic frequencies at 200 kHz and 300 kHz in particular.
422 Bespoke, wide-band receivers were built to maximise backscatter measurements
423 over ranges ≤ 30 m, commensurate with the depths expected in field surveys.
424 The generation of harmonic frequencies was checked and quantified through

425 tank experiments. A complete processing methodology was presented, enabling
426 to fully calibrate the echosounder, and we showed the importance of *in situ*
427 calibration to account for variability in the marine environments. Mounted on
428 a pan & tilt unit, the SBES is able to measure absolute seafloor reflectivity
429 $BS_{\text{calib}}(f, \theta)$, according to incident angles and to different frequencies, at the
430 same time and for the exact same patch of seabed. The multi-frequency SBES
431 was tested in a survey in the Bay of Brest (France), measuring different types of
432 seabed concurrently imaged with seafloor photographs and videos. One of the
433 areas ("Carré Renard") benefited from previous measurements, and we were
434 able to demonstrate the consistency of the different measurements, matching
435 seabed types and differences. These results prove that acoustic seafloor charac-
436 terisation and classification is possible with this kind of instrument.

437

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