

# Corrigendum: Data-driven and learning-based interpolations of along-track Nadir and wide-swath SWOT altimetry observations

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We detected an error in the datasets used for testing the FP-GENN/ConvAE algorithms in the paper. The other algorithms used in the paper (OI, AnDA, VE-DINEOF) are not affected. We precise that the FP-GENN/ConvAE algorithms remains strictly identical but the datasets used with this algorithm oversampled the observations with a factor of 5, leading to an overestimation of the FP-GENN/ConvAE performances. Hopefully, the scientific conclusions remains unaffected: as already stated in the previous version, FP-GENN is still the best algorithm among all the methods tested in the paper but we had to produce a new set of results taking into account this correction. We updated the Figures and qualified a bit some of the comments and conclusions in this corrigendum accordingly.

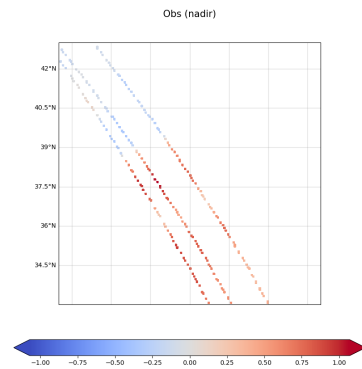
## 1 NEW SETUP OF THE NN-BASED ALGORITHMS

In the previous work of [2] over the Mediterranean sea, using an along-track data aggregation of  $t_k \pm d$  days over a specific day  $t_k$  helps to improve the performance for AnDA. In the first version of the paper, and because of the bug in the dataset used for FP-GENN/ConvAE, it was also the case and an aggregation of  $\pm 5$  days was used. After correction, it is no longer the case, neither for AnDA nor for neural-based methods. As a consequence, all the methods now use value of  $d = 0$ . Figure 1 gives an example on August 4, 2013 of the two types of datasets used in this work (along-track nadir with/without wide-swath pseudo-observations).

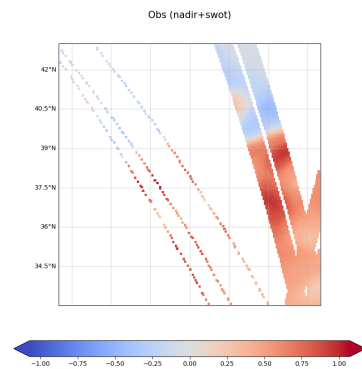
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(a) nadir ( $d=0$ )



(b) nadir ( $d=0$ ) + swot

Fig. 1. along-track nadir and wide-swath pseudo-observations for August 4, 2013

Next, using a 0-day aggregation of the along-track nadir data also influences the best configuration of the NN-based interpolators. If the unsupervised strategy often led to the best performance in the previous version, it is now the supervised strategy that behaves best: the inputs are the observations involving high missing data rates and the targets are the gap-free NATL60 data. The DUACS OI product is also used as a covariate in the inputs, because we think that this may give a prior information about how the anomaly field  $d\mathbf{x}$  is distributed.

According to this new FP-GENN/ConvAE setup, we provide in Section 2 an updated version of Figures 2, 3 and Table 1 with the corrected statistics corresponding to the FP-GENN/ConvAE algorithms.

## 2 EVALUATION

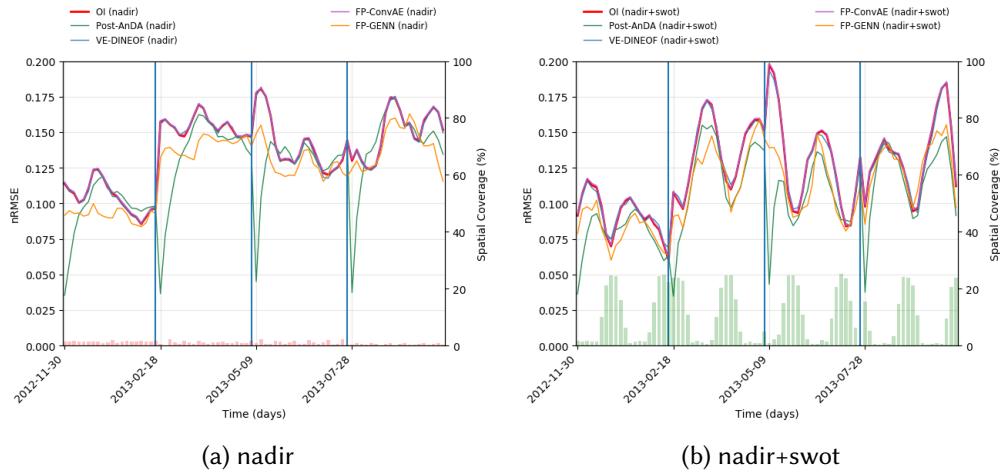


Fig. 2. Daily spatial nRMSE computed on the 80-days non-continuous validation period for OI, (post-)AnDA, VE-DINEOF, FP-ConvAE and FP-GENN. The spatial coverage of 0-days accumulated along-track nadir and wide-swath SWOT data are respectively provided by the red and green-colored barplots

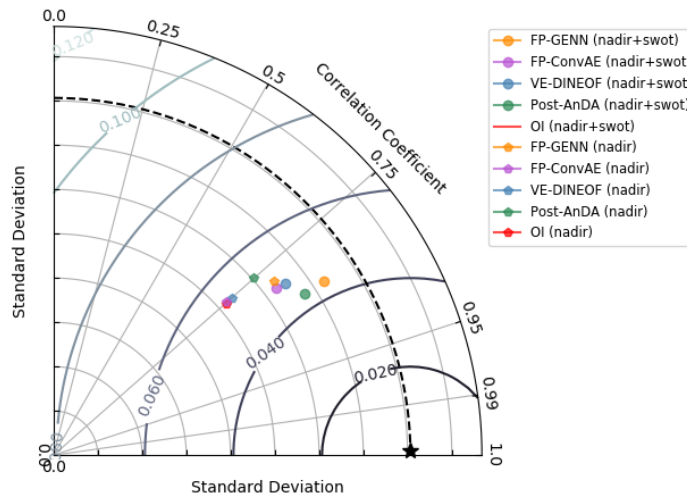


Fig. 3. Taylor diagram computed on the 80-days non-continuous validation period for OI, (post-)AnDA, VE-DINEOF, FP-ConvAE and FP-GENN

	Model type	median	$q_{0.5}$	$q_{0.95}$
nadir	OI	0.14	0.10	0.17
	AnDA	0.14	0.10	0.17
	VE-DINEOF	0.14	0.10	0.17
	FP-ConvAE	0.14	0.10	0.18
	FP-GENN	<b>0.13</b>	<b>0.09</b>	<b>0.16</b>
nadir + SWOT	OI	0.12	0.08	0.17
	AnDA	0.11	0.08	0.15
	VE-DINEOF	0.12	0.09	0.17
	FP-ConvAE	0.12	0.09	0.16
	FP-GENN	<b>0.11</b>	<b>0.07</b>	<b>0.15</b>

	Model type	median	$q_{0.5}$	$q_{0.95}$
nadir	$\nabla_{\text{OI}}$	0.52	0.40	0.64
	$\nabla_{\text{AnDA}}$	0.52	<b>0.40</b>	<b>0.63</b>
	$\nabla_{\text{VE-DINEOF}}$	0.53	0.41	0.65
	$\nabla_{\text{FP-ConvAE}}$	0.54	0.42	0.66
	$\nabla_{\text{FP-GENN}}$	<b>0.52</b>	0.41	0.64
nadir + SWOT	$\nabla_{\text{OI}}$	0.49	0.35	0.66
	$\nabla_{\text{AnDA}}$	<b>0.45</b>	<b>0.32</b>	0.63
	$\nabla_{\text{VE-DINEOF}}$	0.52	0.40	0.67
	$\nabla_{\text{FP-ConvAE}}$	0.51	0.36	0.68
	$\nabla_{\text{FP-GENN}}$	0.48	0.36	<b>0.45</b>

Table 1. Daily SSH and SSH gradient field median nRMSE and associated 5th and 95th percentile computed using the  $4 \times 10$  days at the center of the 4 validation periods for OI, (post-)AnDA, VE-DINEOF, FP-ConvAE and FP-GENN for both nadir use only and joint assimilation/learning with wide-swath SWOT data

The conclusions remain unchanged even if the performance of FP-GENN is lower than initially described in the first version of the paper. This is also the case when computing the radially averaged power spectra as a spatial domain averaged over the 80-days validation period and the associated signal-to-noise ratio for joint use of along-track nadir with SWOT data (not shown here): we now observe that AnDA lead to a better constraint of the SSH spectrum compared to the actual OI capabilities. It produces a spectrum closer to the ground truth real spectrum, by catching up the submesoscale range up to 70km (when picking up signal-to-noise ratio equals to 0.5) when considering a joint learning from along-track nadir and additional wide-swath SWOT data. It does not seem to be the case for FP-GENN, but this should be possible to improve this results by improving the fixed-point solver of the algorithm and using a gradient-based version inspired by 4DVar data assimilation [1].

Last, we also provide the updated versions of both SSH and gradient field reconstructions with updated version of FP-GENN/ConvAE on August 4, 2013:

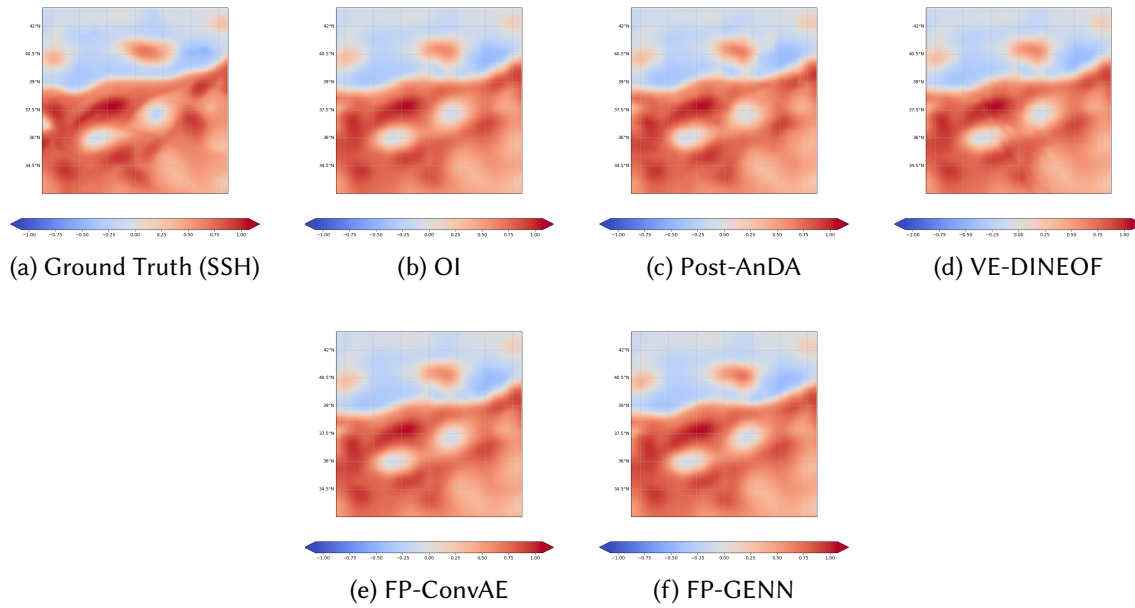


Fig. 4. Global SSH field reconstruction (August 4, 2013) obtained by OI, (post-)AnDA, VE-DINEOF, FP-ConvAE and FP-GENN using along-track nadir data only

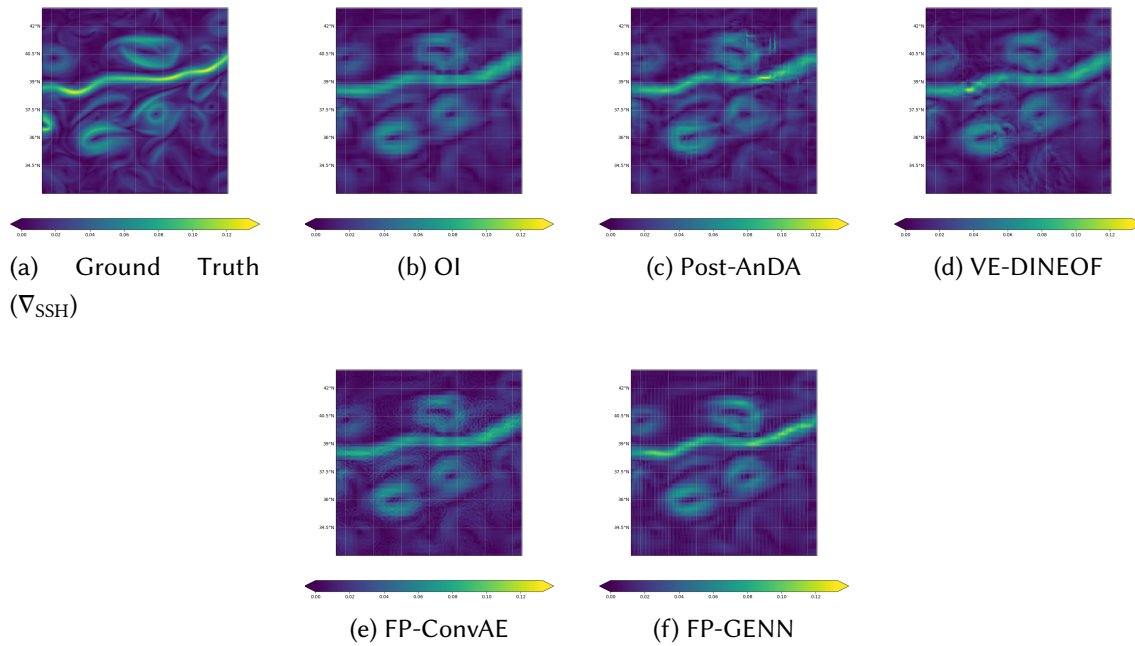


Fig. 5. Global SSH gradient field reconstruction (August 4, 2013) obtained by OI, (post-)AnDA, VE-DINEOF, FP-ConvAE and FP-GENN using along-track nadir data only

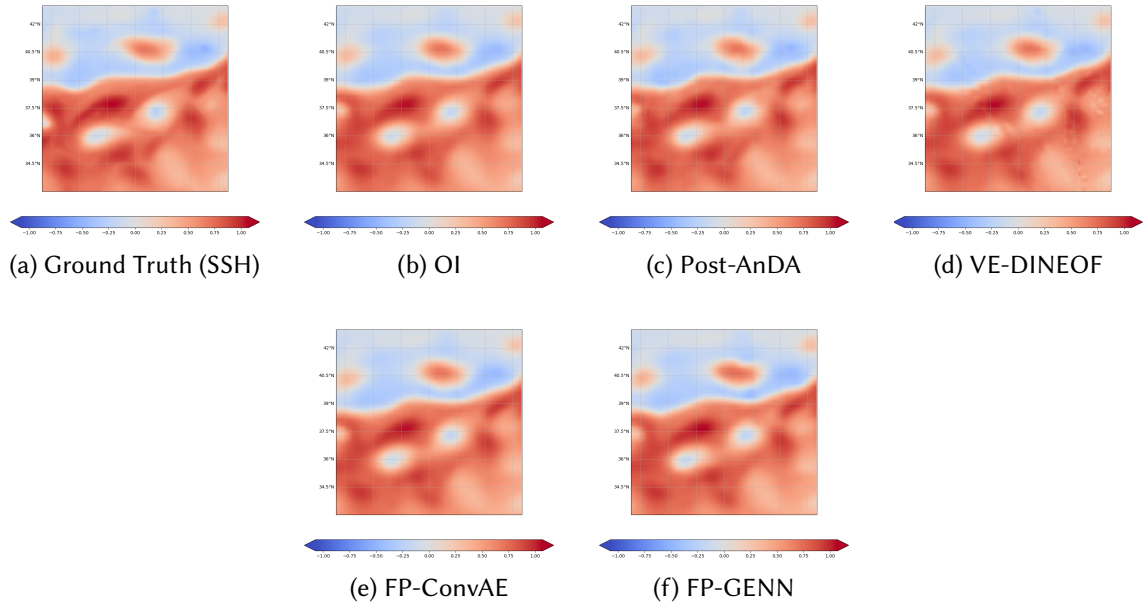


Fig. 6. Global SSH field reconstruction (August 4, 2013) obtained by OI, (post-)AnDA, VE-DINEOF, FP-ConvAE and FP-GENN using along-track nadir and wide-swath SWOT data

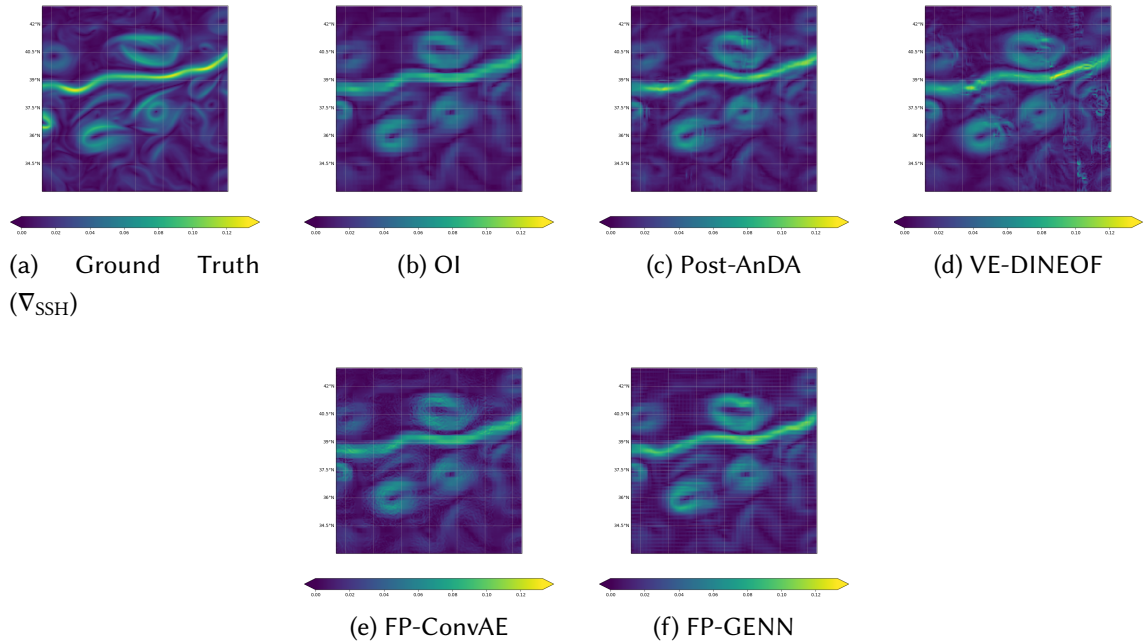


Fig. 7. Global SSH gradient field reconstruction (August 4, 2013) obtained by OI, (post-)AnDA, VE-DINEOF, FP-ConvAE and FP-GENN using along-track nadir and wide-swath SWOT data

## REFERENCES

- [1] Ronan Fablet, Lucas Drumetz, and Francois Rousseau. 2020. Joint learning of variational representations and solvers for inverse problems with partially-observed data. (2020). arXiv:[cs.LG/2006.03653](https://arxiv.org/abs/cs.LG/2006.03653)
- [2] M. Lopez-Radcenco, A. Pascual, L. Gomez-Navarro, A. Aissa-El-Bey, B. Chapron, and R. Fablet. 2019. Analog Data Assimilation of Along-Track Nadir and Wide-Swath SWOT Altimetry Observations in the Western Mediterranean Sea. *IEEE Journal of Selected Topics in Applied Earth Observations and Remote Sensing* (2019), 1–11. <https://doi.org/10.1109/JSTARS.2019.2903941>