
Experimental study of the shear flow effect on tidal turbine blade loading variation

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Abstract :

Tidal turbine arrays are planned to be installed in areas with strong currents where the flow can often be sheared throughout the water column. To study the shear flow effects on tidal turbine, four vertical velocity profiles are generated in a flume tank and are imposed to a three-bladed horizontal axis turbine model. Results show that the sheared velocity profiles do not impact the turbine average performance but are responsible for an increase of blade root streamwise load variations. Blade root streamwise load is moreover linked to the turbine rotational frequency and its harmonics. The velocity perceived by the blades during their rotation is estimated over the rotor area and is compared to the angular phase average of the streamwise load measured on the blades. The phase average of the load and the velocity perceived by the blades are highly correlated even if a varying phase lag has been noticed between these two quantities. This phase lag is dependent on the rotational speed of the turbine, on the incoming flow shear, and is probably caused by the turbine induction effects. This experimental study is a first step to understand the effect of shear velocity profiles on tidal turbines better.

Keywords : Marine renewable energies, Tidal turbine, Tidal velocity profiles, Inflow shear effects, Streamwise blade root loads, Angular phase average, Laser Doppler Velocimetry

23 1. Introduction

24 Each potential tidal area being unique, a lot of works has been carried out to characterize
25 tidal current velocity profile and turbulence [20, 39, 29, 23, 11, 27]. This fine characterization
26 of tidal stream properties is of key importance to evaluate the performance and lifetime of
27 potential tidal turbines installed in these sites. Three main physical phenomena have to be
28 taken into account: the turbulent intensity and the size of turbulent structures (the length
29 scale) [5], the presence of waves at the surface [12], and the current velocity gradient over the
30 water column [26].

31
32 The effects of turbulence on tidal turbines have been studied from many points of view.
33 Mycek et al. [31] demonstrate that, even if averaged performance stays quite identical with or
34 without turbulence, instantaneous behaviour fluctuates drastically when the turbulence inten-
35 sity increases. The turbulence intensity has also a significant impact on the wake development
36 [10]. A high level of turbulence makes the wake dissipates much faster than at low turbulence.
37 For a high upstream turbulence intensity rate, the flow has almost recovered its upstream con-
38 ditions, 6 diameters downstream from the turbine, in terms of velocity, turbulence intensity,
39 and shear stress [31]. Gaurier et al. [18] and Druault and Germain [9] point out that large-scale
40 turbulent structures, created by the interaction between a wide bathymetric obstacle and the
41 flow, are strongly correlated to turbine loads and dominate its frequency response under 1 Hz.
42 Thiébaud et al. [37] also show that large vertical scale eddies are responsible for a high-stress

43 regime of fatigue on the components of a tidal energy converter, reducing the lifetime of its
 44 components. The estimation of wave loading on tidal turbine has been investigated as well
 45 by [14, 7]. Results demonstrate that wave action induces large variations in turbine power
 46 and thrust compared to current only conditions. They concluded that the cyclic amplitude of
 47 loads is directly related to the wave conditions and that regular wave amplitude and frequency
 48 govern turbine wave-induced loads for both waves following or opposing the current.

49 The effects of shear flow on wind turbine have intensively been studied for several years.
 50 From these studies, it has been shown that the impact on the global turbine performance is
 51 limited. The blade loads are however significantly impacted and the performance evaluation
 52 is complicated [41, 36, 35, 24]. In the marine renewable energies field, only a few studies exist
 53 on this subject. Using CFD simulations, Mason-Jones et al. [26] focus on these specific effects
 54 and conclude that torque, power, and axial thrust, related to a chosen blade, have a cyclic
 55 behaviour in a highly shear flow. More precisely, they link the angular behaviour of the power
 56 to the velocity perceived by the blade. They conclude that the maximum power is shifted of an
 57 angle of $\approx 70^\circ$ from the point where the blade should theoretically view the maximum of the
 58 velocity. They assume this difference comes from the induction effect of the turbine. Badshah
 59 et al. [3] come to the same conclusion, without any angular shift between the maximum power
 60 and the maximum velocity. They also study blade fatigue and deformation. From numerical
 61 results, Ke et al. [22] conclude that for a three-bladed horizontal axis turbine, the effect of a
 62 shear flow on turbine performance is small if the shear rate is small. On the contrary, when the
 63 shear increases, it becomes responsible for severe fluctuations of the device loading. Gaurier
 64 et al. [15, 18] study the impact on the blade loading of a shear and turbulent flow, generated
 65 by a wide bathymetric obstacle. Phase average loads show a dependency on the incoming
 66 shear velocity profile but, no link between loads variations and velocity variations could be
 67 established. Finally, Ahmed et al. [1] model the interaction between an inflow-shear and an
 68 horizontal-axis tidal turbine, accounting or not, for turbulence environment. They show that
 69 for both turbulent cases, the turbine rotor influences axial velocity and approach-flow turbu-
 70 lent structures about 1 D upstream to the rotor. The wake also extends beyond 10 D for both
 71 cases. The wake topology is slightly modified by the onset turbulence. That causes a small
 72 wake distortion and slightly aids the break-up of the vortex structures and makes the wake
 73 recovery slightly faster. When looking at phase-average load and surface pressure, being in re-
 74 alistic conditions only contributes to a small component of the overall load fluctuation. Vinod
 75 et al. [40] mimic sheared-turbulent inflow with the use of an active-grid turbulence generator
 76 in a 0.61 m x 0.61 m test section water tunnel. They found an increase of $\approx 30\%$ in torque
 77 fluctuations on a ≈ 0.3 m diameter rotor for sheared inflow.

78
 79 The purpose of this paper is thus to investigate the impact of vertical shear velocity profiles
 80 on both the estimation of tidal turbine performance and the loads experienced by the blades.
 81 To carry out this study, four incoming velocity profiles are generated in an 8 m² section flume
 82 tank using a grid arrangement. A three-bladed horizontal axis tidal turbine of 1 MW capacity,
 83 at scale 1:20, is set in these shear flows and its behaviour, e.g. performance and blade loads,
 84 is studied. In this work, the turbulent intensity is kept low in order to only focus on the
 85 shear-inflow effects. The aim of this paper is to identify the blade load variations accounting
 86 for the shear velocity effect only.

87 After a short description of the experimental setup, incoming velocity profiles are presented.
 88 Then, the focus is done on the evaluation of the turbine power coefficient, strongly dependent
 89 on the velocity chosen for its estimation. Next, blades' streamwise load behaviours are analysed
 90 in a temporal and spectral point of view, as well as versus the angular position of the rotor.
 91 Finally, phase averaged blade loads are compared to velocity perceived by the blade during its
 92 rotation. Similarities and differences between phase average loads and blade apparent velocity

93 are commented and a deeper analysis is proposed.

94 2. Experimental set-up and inflow characteristics

95 2.1. Flume tank and tidal turbine prototype

96 The tests have been carried out in the wave and current circulating tank of IFREMER, in
 97 Boulogne-sur-Mer (France) presented in Figure 1. The test section is 18 m long, 4 m wide
 98 and 2 m deep. The tank is equipped with two pumps which set the 700 m³ of water in
 99 motion to generate current up to 2.2 m/s [16]. In this work, the velocity can be separated
 100 into three components denoted (U, V, W) along the $(\vec{x}, \vec{y}, \vec{z})$ directions respectively. The
 101 x -axis is the main flow direction, the y -axis is oriented from the observation windows towards
 102 the wall, and the z -axis is directed from the tank bottom to the free surface (see Figure 4).
 103 Each velocity component is separated according to the Reynolds decomposition as follows:
 104 $U(x, y, z, t) = \bar{U}(x, y, z) + u'(x, y, z, t)$, where \bar{U} is the temporal mean value of U and u' is its
 105 fluctuating part.

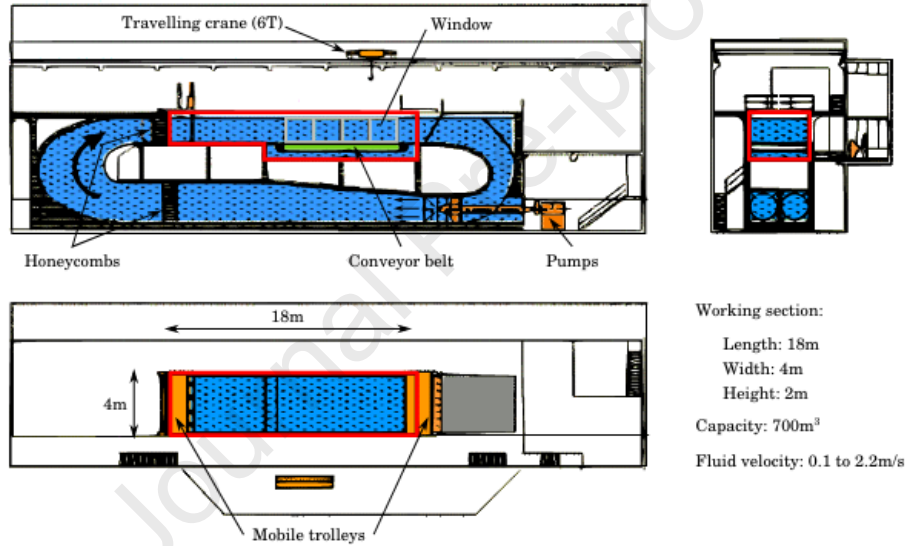


Figure 1: Schematic view of the IFREMER flume tank.

106 The flume tank is equipped with a grid and a honeycomb structure to homogenize the
 107 inflow and control the turbulence. Thanks to these structures, \bar{U} remains constant over the
 108 tank height, with an almost uniform vertical velocity profile. However, this velocity profile
 109 significantly differs from *in-situ* ones, since the bathymetry induced velocity shear is absent in
 110 the tank. It is also the case from the turbine rotor point of view. To recreate velocity profiles
 111 corresponding to what is observed *in-situ*, three "Panels" have been designed [30, 25]. These
 112 Panels are made of multiple layers of wire meshes (Figure 2). The non-uniformity of layers
 113 distribution along the z -axis generates a vertically sheared velocity profile, like those used in
 114 wind tunnels [32]. Thanks to the grid and meshes arrangement presented in Figure 2, each
 115 Panel provides a different sheared velocity profile. Including the *Original grid* case, four case
 116 studies are thus created with the corresponding velocity profiles described in part 2.2.

117 To evaluate the shear effect of velocity profiles on tidal stream turbines, a 1:20 scale three-
 118 bladed horizontal axis turbine of 1 MW capacity, is used (Figure 3). The rotor of diameter
 119 $D = 2R = 0.724$ m is composed of three 307 mm long blades made in carbon fibre which follow
 120 a NACA 63 – 418 profile [17]. The turbine is equipped with a motor driven by a controller. A
 121 slipping is moreover connected to the axis and allows to transfer the signals from the different

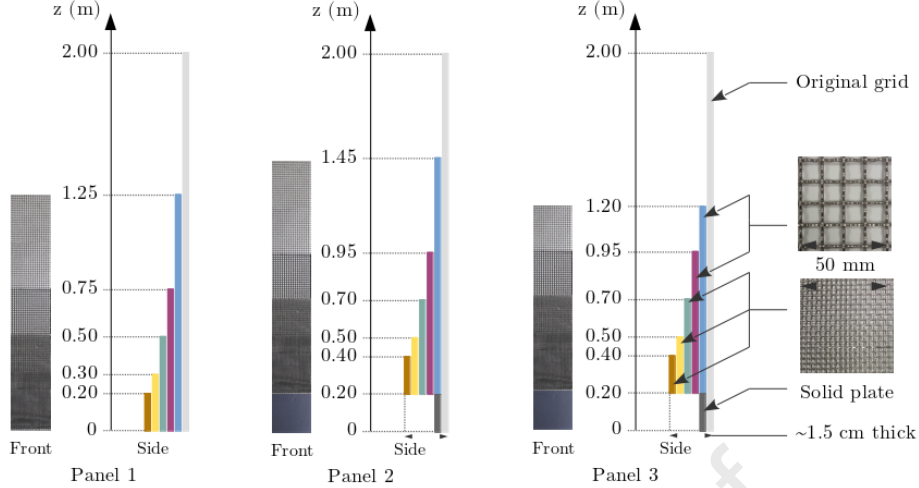


Figure 2: Grids and meshes arrangement, named *Panel 1* to *3*, for generation of realistic sheared velocity profiles. Coarse mesh is made with 2 mm thickness wires evenly-spaced every 10 mm. Fine mesh is made with 0.7 mm thickness wires evenly-spaced every 2 mm.

122 rotating sensors present on the rotor. These signals then go up into the stanchion to the
 123 surface.

124 Each turbine's blade root is equipped with load-cells which measure two forces (F_x and
 125 F_y) and three moments (M_x , M_y , and M_z), as detailed in Figure 3. A rotating cartesian
 126 coordinate system (\vec{e}_x , \vec{e}_y , \vec{e}_z) is associated with each blade root. The global rotor torque and
 127 thrust are also measured by a specific instrumentation. The uncertainty of measurement is
 128 0.2% for the loads and 0.04 tr/min for the rotational speed, according to the manufacturer.
 129 Since the turbine's rotor is not equipped with angular position sensor, we made the hypothesis
 130 that this angular position can be processed through the blade F_y measurements, as previously
 131 done in Gaurier et al. [18]. This idea is based on the fact that the blade weight is projected
 132 on the \vec{e}_y direction for every time step. The complete processing is described in the following
 133 three steps procedure:

- 134 1. The fluctuating parts of the F_y signals are first extracted for each blade.
- 135 2. They are then filtered with a band-pass filter around the rotation frequency f_r . This step
 136 enables the weight component of the blade to be kept only. This constitutes the main
 137 hypothesis of this method: the blades' weight only responds at the rotation frequency
 138 and no other physical perturbation affects the F_y signals at the rotation frequency.
- 139 3. Using the phase of these sinusoidal signals, we get the three θ_i angles corresponding to
 140 the three blades. Then, we defined a convention: the main rotor angle is defined with
 141 $\theta = 0$ rad corresponds to blade 1 at the top dead centre. This main rotor angle is the
 142 average of the three θ_i (re-phased for blade 2 and 3, with $\pm 2\pi/3$ rad). The average
 143 is only processed if the difference between the three re-phased θ_i is lower than a given
 144 threshold.

145 A possible uncertainty source concerning this method is the temporal precision: when the
 146 turbine rotation speed is set to the designed tip speed ratio, the blade rotation is 5° between
 147 each time step, which can lead to an error of 2.5° .

148 To evaluate the impact of shear velocity profile on the turbine behaviour, the turbine is
 149 positioned 12.5 m downstream of the panels' assembly and the honeycomb structure. The
 150 rotor is set in the centre of the test section, with the turbine hub at $(y, z) = (2 \text{ m}, 1 \text{ m})$, as
 151 presented in Figure 4.

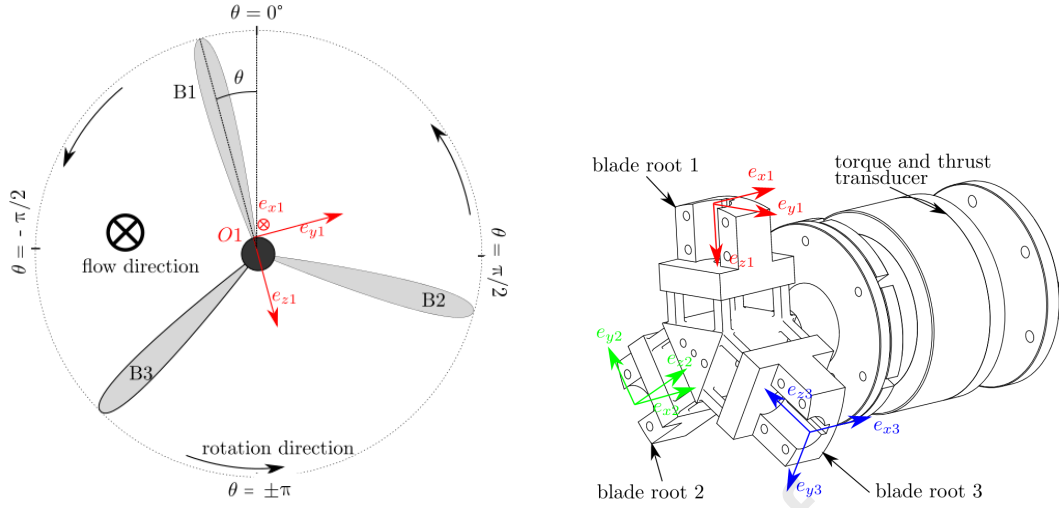


Figure 3: Blade axis and rotation direction of the turbine (left) and blade roots and torque Q and thrust T transducer (right).

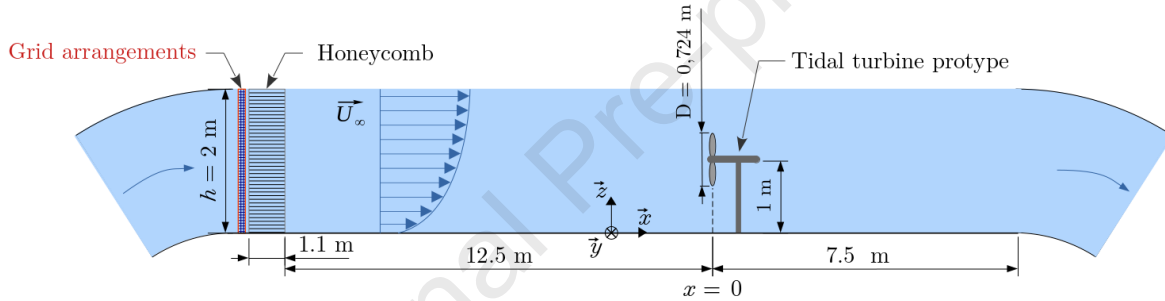


Figure 4: Schematic view of the experimental set-up, with the turbine fixed 12.5 m downstream the honeycomb outlet.

152 2.2. Incoming vertical velocity profiles characterization

153 The incoming flow is assumed to be steady and constant, with the imposed velocity: $U_\infty =$
 154 1 m/s and $V_\infty = W_\infty = 0$ m/s. To characterize incident velocity profiles, a 3 Components
 155 Laser Doppler Velocimetry system (3C LDV) is used. Before measurements, the tank is seeded
 156 with $10 \mu\text{m}$ diameter silver coated glass micro-particles. 3C LDV sampling frequency depends
 157 on the number of particles viewed by the sensor of the probe during the measurement. The
 158 LDV acquisition frequency is higher than 100 Hz for the three components of the data used
 159 in this study.

160 According to the 3C LDV measurements, we established that V and W are always smaller
 161 than 0.02 m/s on the study region. For the four study cases, V and W are thus neglected
 162 in the rotor plane. In the following, the study is consequently focused on the streamwise
 163 component U of the velocity only. To characterise the velocity profile along the tank height,
 164 measurements are carried out every 5 to 20 cm, depending on the degree of precision required
 165 to capture the variation of U . On each measurement point, the acquisition lasts 180 s. The
 166 obtained velocity profiles $\overline{U}(z)$ are presented in Figure 5. The standard deviation of $U(z, t)$,
 167 denoted $\sigma(U(z))$, is presented in the same figure to highlight the fluctuating part of the flow.

168 As expected, the *Original grid* generates an almost uniform velocity profile over the tank.
 169 On the contrary, the *Panel 3* velocity profile presents a strong velocity gradient throughout
 170 the water column. Nevertheless, *Panels 1* and *2* create more complicated velocity profiles

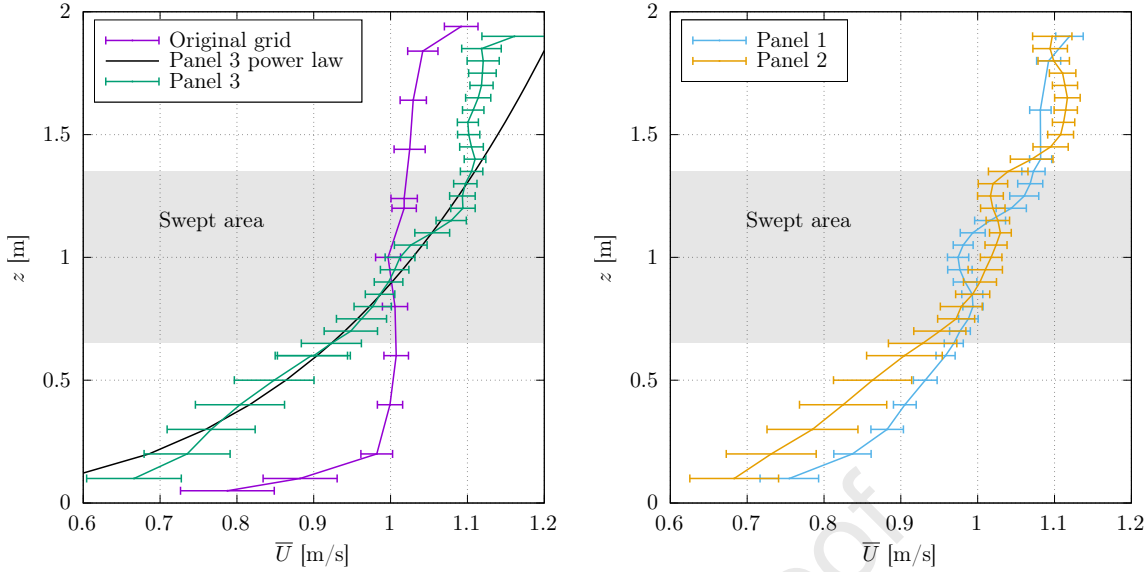


Figure 5: Vertical profiles of the streamwise velocity $\overline{U}(z)$ obtained for the *Panels* describes in Figure 2. Data come from 3C LDV measurements in the rotor plane for the four cases. Error bar represents standard deviation $\sigma(U(z))$. The grey shaded zone materializes the area covered by the turbine blade. *Panel 3* power-law coefficient: $\alpha = 4$ and $U_0 = 1.23$ m/s (see equation 1).

171 because they both present a low-velocity zone in the swept area. For *Panel 1*, this zone is
 172 located around $z = 1$ m while it is around $z = 1.3$ m for *Panel 2*.

173 At sea, the current velocity profile is usually non-linear as well. These profiles show multiple
 174 slopes depending on the site, the tidal range, the direction of the flow, and the wave conditions.
 175 Their velocity gradients are thus not constant along the depth. One way to define their
 176 slope is to use power-laws, enabling the profiles to be compared using a unique coefficient α .
 177 $U_{PowerLaw}(z)$ is defined as:

$$U_{PowerLaw}(z) = U_{ref} \times \left(\frac{z}{D_e}\right)^{1/\alpha} \quad (1)$$

178 with U_{ref} corresponding to the surface velocity (or velocity at mean depth), D_e represents
 179 the depth of the water column and z is the distance from the bottom. In the Alderney
 180 Race (France), a large study has been carried out, using towed ADCP [34]. During this
 181 survey, the waves' effects have been neglected by the authors. They found current velocity
 182 profiles following equation 1, with α between 4 and 14. A trend stands however out: the
 183 power-law corresponding to $\alpha = 7$ is representative of many marine renewable energy sites
 184 [11, 20, 38, 23]. To link our case to what is encountered *in-situ*, we determine the power-
 185 law that best fits the *Panel 3* velocity profile over the rotor height. It gives the following
 186 parameters: $U_{ref} = 1.23$ m/s, and $\alpha = 4$. This curve is plotted in Figure 5. The obtained
 187 coefficient α is in the range of the Alderney Race and provides the most sheared possible
 188 case. The shear velocity profile generated by *Panel 3* is thus representative of *in-situ* vertical
 189 velocity profile. Additionally, the *Panel 1* case and the *Panel 2* case, which generate complex
 190 velocity profiles, correspond to more specific *in-situ* cases, caused by site-specificity.

191 The introduction of the *Panels* may furthermore generate turbulence, which can be quan-
 192 tified by the 1D turbulence intensity I_{1D} :

$$I_{1D} = \frac{\sigma(U)}{\overline{U}} \quad (2)$$

193 Turbulence intensity over the tank height for the four cases is plotted in Figure 6. Turbulence
 194 intensity ranges from 1% to 3% over the rotor height, for *Original grid* and *Panel 1* cases. It
 195 reaches 3.5% in the bottom part of the rotor for the *Panels 2* and *3* cases. This is due to the
 196 solid plate used at the very bottom part of the grid and meshes arrangement, which strongly
 197 reduces the averaged velocity in this area and acts as a backward-facing step avoiding the flow
 198 to go through the last rows of the honeycomb structure.

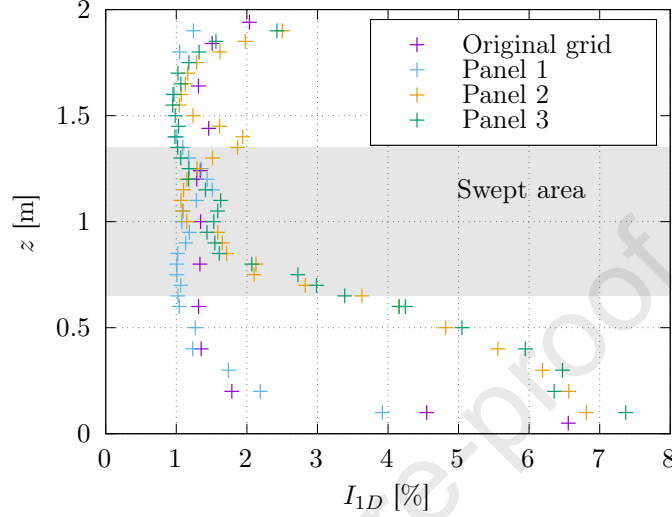


Figure 6: Turbulence intensity I_{1D} over the water column for the four cases.

199 To complete the characterisation of the four velocity profiles over the rotor height, their
 200 mean velocity, mean 1D turbulent intensity, and maximum mean velocity difference $\Delta_{max}\bar{U}$
 201 are gathered in table 1. With the use of the *Panels*, three shear velocity profiles have been
 202 generated, while the *Original grid* provides a uniform profile over the rotor height. Moreover,
 203 for all cases, the mean velocity on the rotor area is the same and the turbulence intensity is
 204 low: $\widehat{\bar{U}} = 1.0$ m/s and $\widehat{I_{1D}} \leq 2.5\%$, with \square the temporal average and \square the spatial average
 205 over the rotor area of the turbine.

206 In the following, we will consequently focus on the effect of the shear on the turbine only.
 207 In the next section, the turbine response to these velocity profiles is studied and compared
 208 between cases.

Case	$\widehat{\bar{U}}$ [m/s]	$\Delta_{max}\bar{U}$ [m/s]	$\widehat{I_{1D}}$ [%]
<i>Original grid</i>	1.00	0.01	1.6
<i>Panel 1</i>	1.01	0.10	1.5
<i>Panel 2</i>	1.01	0.11	2.5
<i>Panel 3</i>	1.02	0.18	2.5

Table 1: Mean velocity, 1D turbulent intensity, and maximum velocity difference over the rotor height.

209 3. Shear flow effect on a tidal turbine

210 3.1. Effect on turbine global performance

211 In this section, the global tidal turbine performance is analysed and compared between
 212 the cases. A relevant criterion to quantify the turbine performance is the power coefficient C_p ,

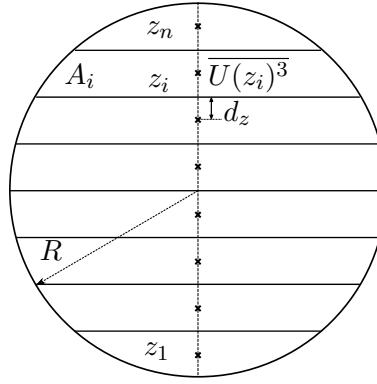


Figure 7: Methodology to obtain $\widehat{U^3}$, the mean value of $\overline{U^3}$ over the swept area. In our calculation, $n = 16$, $dz = 0.025$ m.

213 which is defined as:

$$C_p = \frac{\overline{Q\omega}}{\frac{1}{2}\rho A \widehat{U^3}} \quad (3)$$

214 with A the area swept by the blades ($A = \pi R^2$), $\overline{\omega}$ the rotational speed of the turbine and ρ
 215 the water density. \overline{Q} is the rotor mean torque measured on the rotation axis and $\widehat{U^3}$ is the
 216 mean flow velocity view by the turbine, calculated as follow:

$$\widehat{U^3} = \frac{1}{A} \sum_{i=1}^n \overline{U(z_i)^3} A_i \quad (4)$$

217 with z_i the i^{th} slice where the velocity is considered as constant and A_i its area ($A = \sum_{i=1}^n A_i$).
 218 n is the number of slices used for the calculation. The number of slices is strongly dependent
 219 on the case-study. In our case, the value of \widehat{U} , $\widehat{U^2}$ and $\widehat{U^3}$ are not significantly modified
 220 ($< 10^{-3}$) for $n \geq 12$, corresponding to a slice interval of 6.0 cm. In this study, $n = 16$. This
 221 equivalent velocity has been used before the C_p or kinetic energy calculations in wind shear
 222 cases, e.g. by [42, 2] and is imposed by IEC norms for tidal turbine [21]. To use this method,
 223 \overline{U} is assumed to be constant along the y -axis. Thus, using the velocity profiles established in
 224 part 2.2, $\overline{U(z_i)^3}$ is known at each height z_i and assume to be constant over the i^{th} slice. Please
 225 note that the cubing of velocity should be calculated before temporal and spatial averaging to
 226 obtain a correct C_p as explained by [5]. A schematic of the $\widehat{U^3}$ calculation method is presented
 227 in Figure 7.

228 In Figure 8, performance coefficients are plotted versus the TSR (Tip Speed Ratio) for the
 229 four cases. The TSR corresponds to a normalised rotational speed and is defined as follow:
 230 $TSR = \overline{\omega}R/\widehat{U}$. At first sight, the behaviour of C_p is the same whatever the shear with small
 231 fluctuations ($< 5\%$ of the mean value). For the highest sheared case, the C_p is slightly reduced
 232 (5%). The thrust coefficient shows an expected behavior, increasing with the TSR . For the
 233 *Original grid, Panel 1* and *Panel 2* cases, the thrust coefficient is similar. The C_t obtained for
 234 *Panel 3* case is a bit lower. These observations are the same than the one already observed for
 235 the C_p curve. The standard deviation of C_p and C_t coefficients also show similar trends. They
 236 represent less than 5% of the mean value and slightly increase with the TSR , as presented
 237 in Gaurier et al. [19] for the same turbine model. The only exception is for $TSR = 2.5$,
 238 where the standard-deviation of the C_p coefficient presents a steep gradient. At this point, the
 239 controller of the turbine has difficulties to regulate the rotation speed of the turbine, causing

240 thus higher standard deviation value for all *Panel* cases. Finally, the presence of a vertical
 241 velocity gradient does not impact the mean turbine behaviour, as seen in Vinod et al. [40].

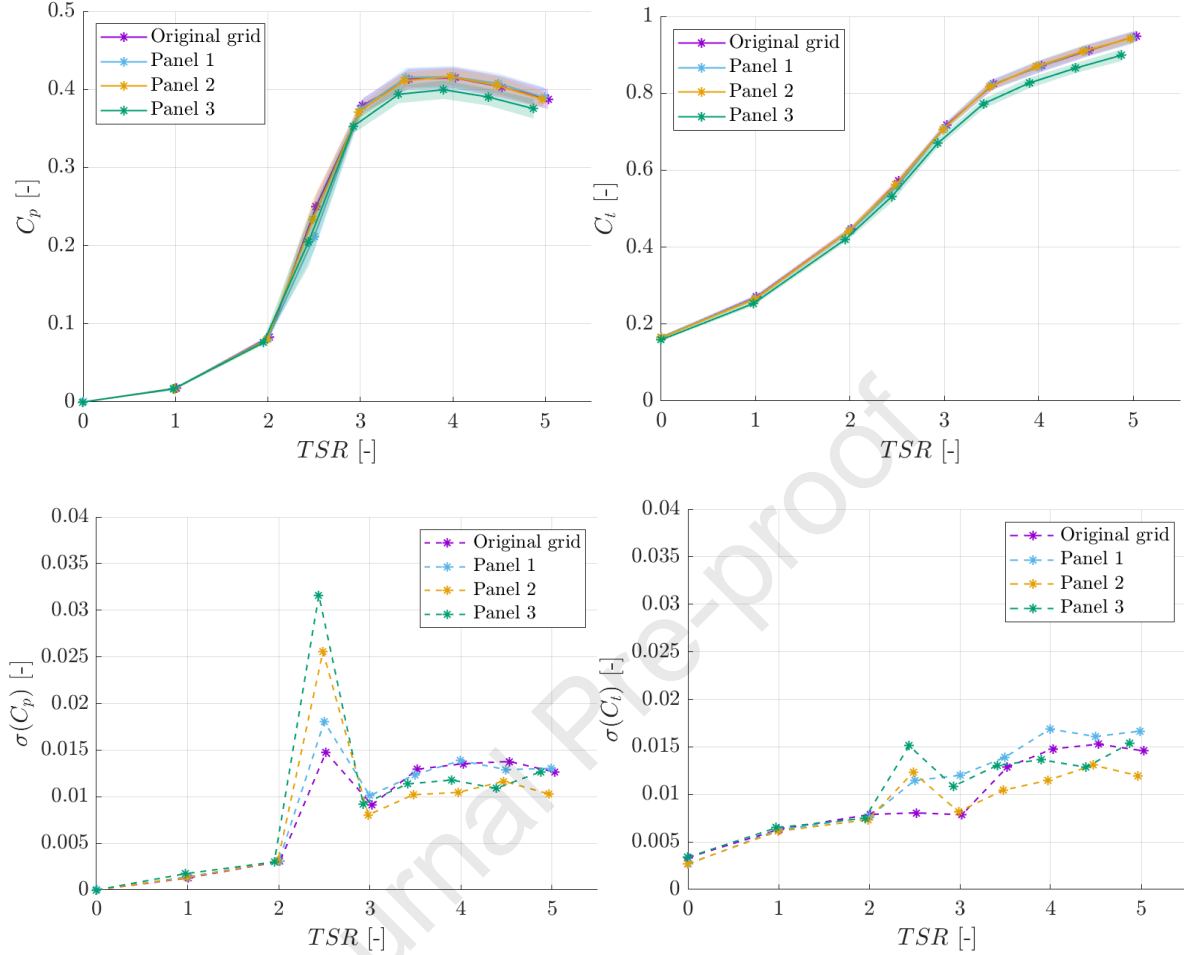


Figure 8: Power curves for the four cases. Top line: Power coefficient C_p (left) and thrust coefficient C_t (right). The shaded areas represent their standard deviation. Bottom line: Standard deviation of C_p (left) and of C_t (right).

242 This conclusion depends on the choice of the characteristic velocity, as shown in table 2.
 243 This remark shows the importance of using velocity over the entire swept area \widehat{U}^3 and \widehat{U} instead
 244 of its value at the rotor centre height only. As the velocity gradient is not constant, $\overline{U}(z = 1 \text{ m})$
 245 is not representative of the velocity perceived by the blades. For example, taking the *Panel 1*
 246 case, the low-velocity zone at $z = 1 \text{ m}$ leads to an underestimation of the velocity seen by
 247 the blades. For our cases, if $\overline{U}(z = 1 \text{ m})$ is considered for the C_p calculation, the difference
 248 on C_p values would be in the range 3% to 7%. These relative differences are summed up in
 249 Table 2. According to these results, the obtained values of C_p are more impacted by the way
 250 it is calculated than by the presence of a vertical velocity shear. The calculation of the C_p
 251 coefficient has thus to be made very cautiously: the specificities of the velocity perceived by
 252 the turbine, e.g. shear inflow, play a decisive role. Accounting for these specificities, the C_p
 253 coefficient enables the real turbine performance to be calculated. Finally, it shows that if the
 254 incoming velocity average over the rotor area is the same, the shear does not affect the turbine
 255 mean performance, as previously demonstrated for wind turbine [2, 42].

Case	C_p at $TSR4$, calculated with $\overline{U}(z = 1\text{m})$	C_p at $TSR4$, calculated with \widehat{U}	Difference of C_p for $TSR \in [3.5 : 5]$
Ori. grid	0.42	0.41	3%
<i>Panel 1</i>	0.45	0.42	7%
<i>Panel 2</i>	0.40	0.42	4%
<i>Panel 3</i>	0.42	0.40	5%

Table 2: Relative differences on C_p depending on how the cubed velocity is chosen.

256 3.2. Effect on blade loadings

257 Although velocity shear does not change global turbine performance, it may impact the
 258 instantaneous behaviour, especially the variation of blade loadings. In this part, the focus is
 259 done on blade 1 (see Figure 3), knowing that the results are equivalent for the three blades.
 260 The turbine is studied at its operating point $TSR = 4$. The acquisition of F_{x1} lasts 180 s.
 261 This time is required to obtain a converged mean value. In Figure 9, the fluctuating part
 262 F'_{x1} is plotted and some periodic variations are seen with smaller fluctuations due to other
 263 flow variations. To quantify F_{x1} over the entire acquisition duration, the mean value and its
 264 variations are summed up, for the four cases, in Table 3. It appears that both mean values
 265 and variations are bigger for the *Panel 3* case, while *Panel 1* and *Panel 2* cases present similar
 266 behaviours. The shear induced by *Panel 3* seems to have a more pronounced impact than the
 267 two other cases. Thus, the incoming shear velocity profile has a greater influence on blade
 268 load than on global performance C_p .

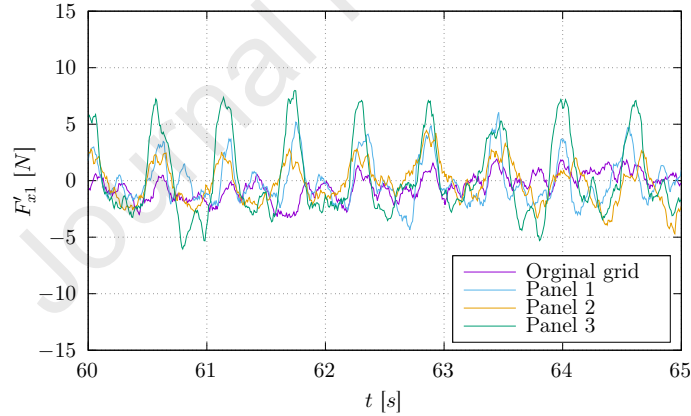


Figure 9: Evolution of the blade 1 load fluctuating part F'_{x1} with the time, between 60 s and 65 s, when the turbine rotates at $TSR = 4$. For more readability of the figure, $F'_{x1}(t)$ signals have been re-phase using phase lag from cross-correlation presented in table 5.

Case	$\overline{F_{x1}}$	$\sigma(F_{x1})/\overline{F_{x1}}$ [%]
<i>Original grid</i>	55.7 N	2.2%
<i>Panel 1</i>	56.9 N	3.5%
<i>Panel 2</i>	57.0 N	3.6%
<i>Panel 3</i>	59.7 N	6.2%

Table 3: Mean load and proportion of the standard deviation.

269 To investigate the spectral behaviour of the load F_{x1} , a Fast Fourier Transform (FFT)

270 analysis is conducted. On the FFT decomposition presented in Figure 10, there is a peak
 271 at the frequency 1.8 Hz for the *Panel 1*, *2*, and *3* cases. This frequency corresponds to the
 272 blade passing frequency f_r . The peak amplitude is more important in the *Panel 3* case: the
 273 magnitude of the variation is higher and reaches 4 N while it is less than 2 N in other cases.
 274 Moreover, in the *Original grid* case and the *Panel 1* case, a peak appears at the first sub-
 275 harmonic ($2 \times f_r$) of the blade rotation frequency. It is the signature, in the frequency domain,
 276 of the low velocity zone centred at $z \approx 1$ m, where the blades pass twice per revolution, at
 277 $\theta \approx \pi/2$ and at $\theta \approx -\pi/2$. In *Panel 2* and *Panel 3* cases, this low velocity zone is not present
 278 and the peak at $2 \times f_r$ is significantly smaller than the one at f_r , on the contrary to the two
 279 other cases where $F_{x1}(2f_r) > F_{x1}(f_r)$. A phenomenon at $2 \times f_r$ also appears in *Panel 3* case
 280 but it is less pronounced than at f_r . Finally, a frequency peak appears at $3 \times f_r$ in *Panel 1*
 281 case, quite as high as the peaks at f_r and $2 \times f_r$, coming from global tri-bladed rotor effects.
 282 Thus, the impact of the velocity profile is visible on the spectrum since it changes the emerging
 283 frequency and magnitude of spectrum peaks.

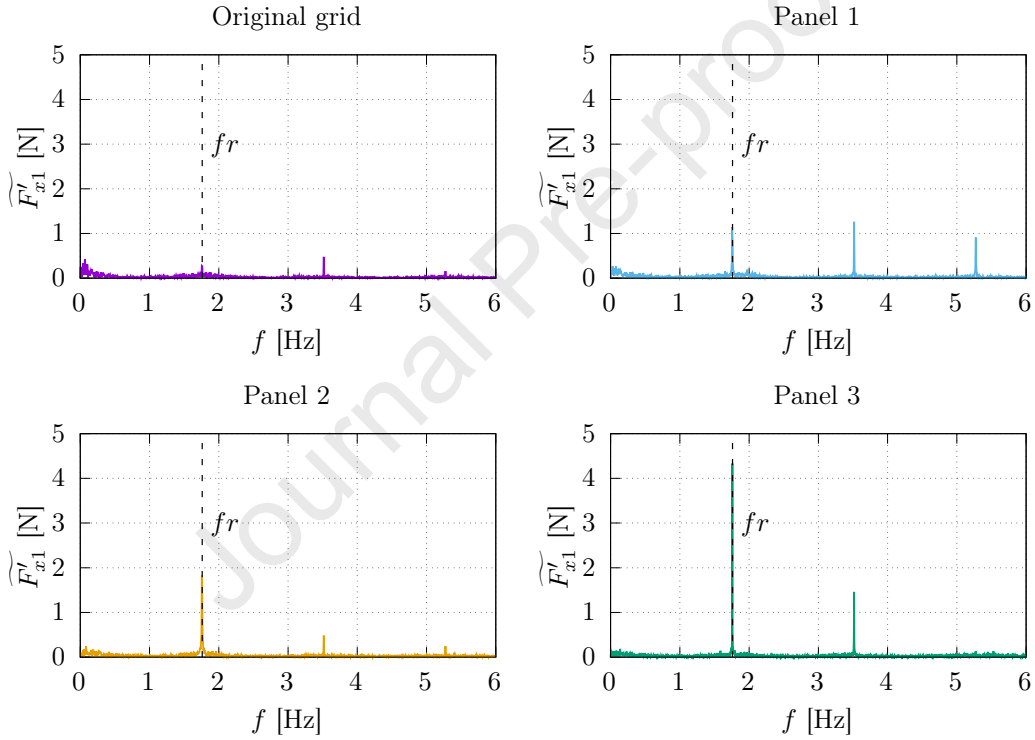


Figure 10: Fast Fourier Transform (FFT) of the local load fluctuating part F'_{x1} when the blade rotates at $TSR = 4$.

284 F_{x1} spectra have shown that load variations are linked to the turbine rotation. It is then
 285 interesting to relate the streamwise load variation of blade 1 to its angular position. A scatter
 286 plot is obtained and can be interpolated to calculate the angular phase average $\mathcal{F}_{x1}(\theta)$, for
 287 each discretized angular position. This phase average $\mathcal{F}_{x1}(\theta)$ is presented in Figure 11. In the
 288 following, \mathcal{F}_x and \mathcal{U} represent the angular phase average of the corresponding quantities and
 289 are only dependent on the angular position θ of the rotor.

290 For the *Original grid* case, $\mathcal{F}_{x1}(\theta)$ is nearly independent on θ . For the three other cases,
 291 $\mathcal{F}_{x1}(\theta)$ varies with the blade angular position: shear velocity profiles impact the phase average
 292 of the streamwise load. For *Panels 1* and *3* cases, $\mathcal{F}_{x1}(\theta)$ presents a maximum at $\theta \approx -\pi/4$,
 293 which is particularly significant for *Panel 3* case. In fact, this maximum appears just after (in

294 the rotational direction) the position where the blade is at the top dead centre ($\theta = 0$ rad), i.e.
 295 where \bar{U} is maximal. The phase average of the streamwise load \mathcal{F}_{x1} obtained for *Panel 1* and
 296 *3* cases are similar, even if the magnitude of the angular variation is smaller than in *Panel 1*
 297 case. Result obtained for the *Panel 2* case is relatively different from the other cases, with a
 298 lower maximum value, which is positioned at $\theta = 0$ rad.

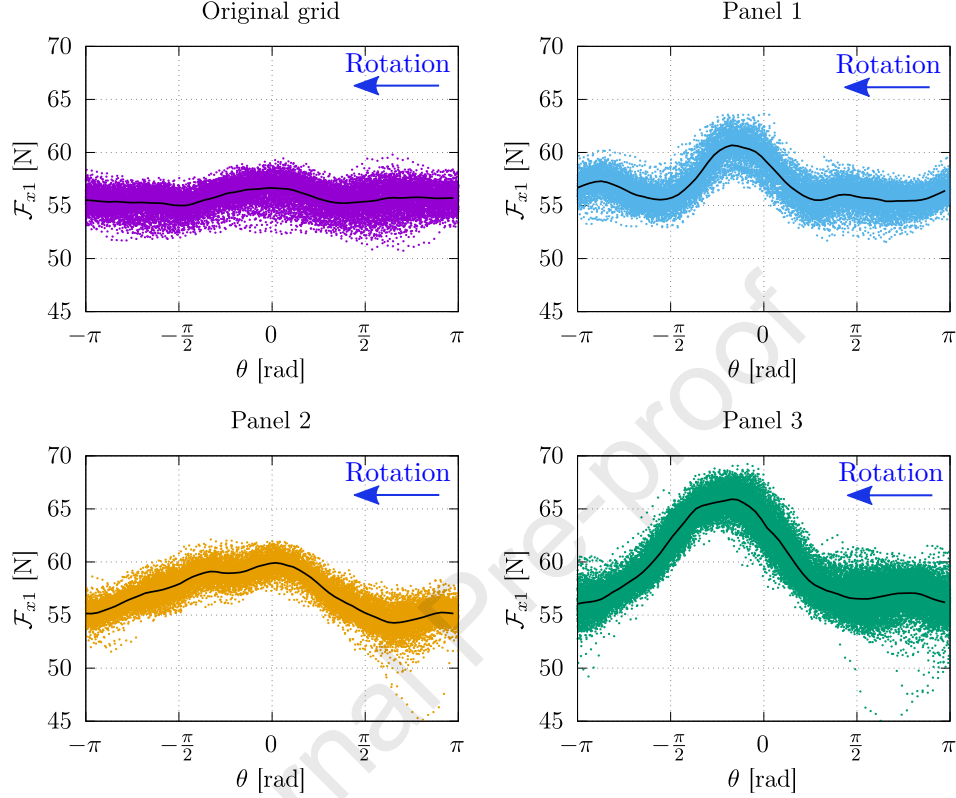


Figure 11: Angular repartition of blade 1 load F_{x1} measurement points (in N) when the turbine rotates at $TSR = 4$. The solid line represents its phase average $\mathcal{F}_{x1}(\theta)$. The direction of rotation is indicated by the blue arrow and corresponds to a negative direction.

299 According to these presented results, when the velocity profile is sheared, the link between
 300 the blade passing frequency and the phase average streamwise load is more pronounced. Glob-
 301 ally, it appears that $\mathcal{F}_{x1}(\theta)$ is maximum near $\theta = 0$ rad and minimum at $\theta = -\pi$ rad, when
 302 the velocity reaches the corresponding extrema. In the following, the blade streamwise loads
 303 are phase averaged and analysed.

304 3.3. Angular correlation between velocity and load variation

305 In the previous section, the temporal and angular variations of the blade loading have been
 306 analysed, for the four cases. This highlights the link between streamwise loads and streamwise
 307 velocity which can be expressed as [4, 6, 8]:

$$F_{tot}(t) = KU^2(t) \quad (5)$$

308 where K is assumed to be constant. Using the Reynolds' decomposition, equation 5 becomes:

$$F_{tot}(t) = K(\bar{U} + u'(t))^2 \quad (6)$$

310

$$F_{tot}(t) = K(\bar{U}^2 + 2\bar{U}u'(t) + u'^2(t)) \quad (7)$$

311 As measurements are not synchronised, only the time average of the equation is kept:

$$\overline{F_{tot}} = K(\overline{U}^2 + \overline{u'^2}) \quad (8)$$

312 Moreover, it was shown in part 2.2 that $\sqrt{\overline{u'^2}}$ represents less than 4% of \overline{U} , and can be
313 neglected:

$$\overline{F_{tot}} \approx K\overline{U}^2 \quad (9)$$

314 From that point and as done in the previous section, the focus is made on blade 1 only.
315 Results are however similar for blades 2 and 3. The load-cell which measures the streamwise
316 component of the load F_{x1} measures the integrated pressure exercised by the flow over the
317 blade's surface, from the foot to the tip. This load is thus linked to the variation of the
318 perceived velocity which depends on the angular position of the blade θ . Mathematically,
319 the velocity perceived by the blade $\mathcal{U}(\theta)$ is defined as the time average velocity \overline{U} from LDV
320 measurements integrated on the blade surface, depending on its position θ . To stay consistent
321 with phase average velocity $\mathcal{U}(\theta)$ perceived by blades, the blade streamwise load has to be a
322 phase average: $\mathcal{F}_{x1}(\theta)$. Equation 9 thus becomes:

$$\mathcal{F}_{x1}(\theta) \approx K\mathcal{U}^2(\theta) \quad (10)$$

323 This mathematical link is experimentally studied in the following, to explain the impact of
324 angular velocity variations on the blade load during the rotation.

325 3.3.1. Angular velocity perceived by the blade calculation

326 To compare the streamwise blade phase average load $\mathcal{F}_{x1}(\theta)$ to the squared velocity per-
327 ceived by the blade $\mathcal{U}^2(\theta)$, this velocity has to be calculated first. LDV measurements have
328 been done over the tank height to obtain time averaged velocity as plotted in Figure 5. The
329 velocity is supposed to be constant along the y -axis, thus a 2D velocity cartography is obtained
330 on the rotor plane by extruding the vertical velocity profile (interpolated along z -axis) along
331 y -axis as plotted in Figure 12. From this part, we choose the turbine rotation axis as origin
332 of the coordinate system.

333 The blade rotation angle is noted θ in the following (see Figure 13). Then, polar coordinates
334 are used. $\overline{U}(r, \theta) = \overline{U}(z)$ is the velocity in this coordinates system, with $z = r \cos(\theta)$. $\overline{U}(r, \theta)$
335 is not dependent on y because the assumption has been done that the velocity is constant over
336 y -axis.

337 To calculate the velocity $\mathcal{U}(\theta)$ perceived by the blade on a revolution, the blade is assumed
338 to be linear, with zero thickness (red dashed line in Figure 13). Note that we compared the
339 velocity calculated from the blade surface to the velocity calculated from the blade central line
340 (retain calculation) and that the obtained velocity is almost equal. With these approximations,
341 the velocity perceived by the blade is expressed as:

$$\mathcal{U}(\theta) = \frac{1}{R} \int_0^R \overline{U}(r, \theta) dr \quad (11)$$

342 To numerically calculate $\mathcal{U}(\theta)$, the space is discretised. In cartesian coordinates, $z = z_1 +$
343 $d_z n_z$ with $z_1 = -0.35$ m. In polar coordinates, $\theta = -\pi + d_\theta n_\theta$ and $r = d_r n_r$, $R = d_r N_r$. The
344 velocity integrated on the blade thus becomes:

$$\mathcal{U}[n_\theta] = \frac{1}{N_r} \sum_{n_r=1}^{N_r} \overline{U}[n_r, n_\theta] \quad (12)$$

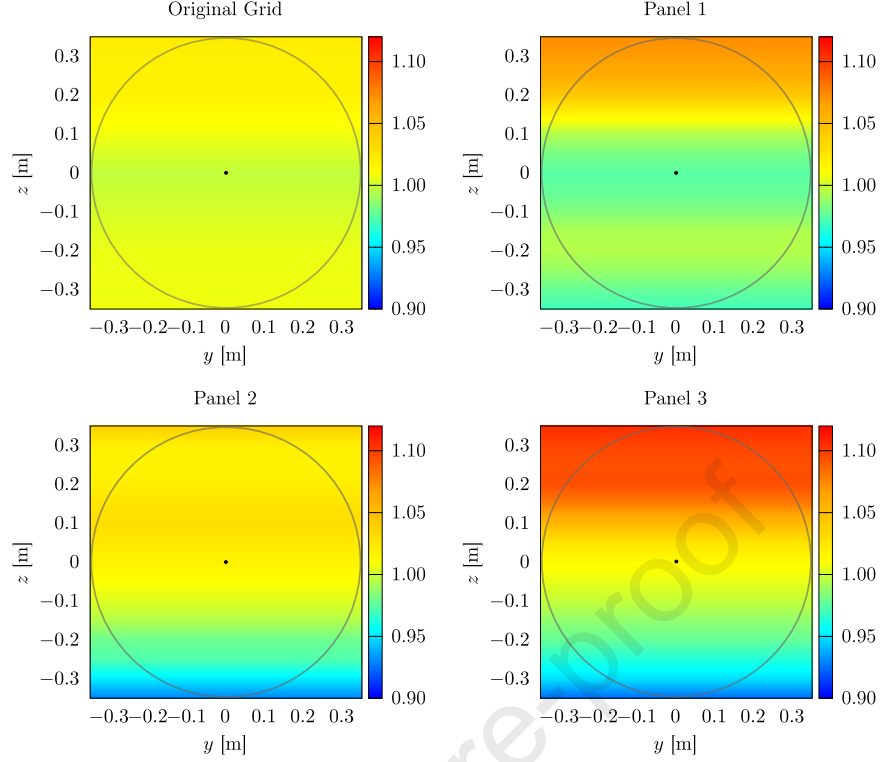


Figure 12: Cartography of $\bar{U}(z)$ on the swept area in the four cases. Note that the origin of the coordinate system move to the centre of the turbine for more simplicity.

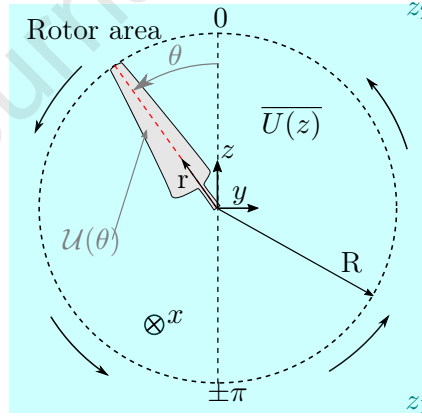


Figure 13: Definition of the notation used to calculate the velocity perceived by the blade.

345 The incoming velocity in the rotor plane have also to be discretised as function of cartesian
 346 and polar coordinates.

$$\begin{aligned} \overline{U}[n_z] &= \overline{U}(z_1 + d_z n_z) \\ \overline{U}[n_r, n_\theta] &= \overline{U}(d_r n_r - \pi + d_\theta n_\theta) \end{aligned}$$

348 Finally, to have $\overline{U}[n_r, n_\theta] = \overline{U}[n_z]$, n_z has to be equal to: $n_z = \text{int}((n_r d_r \cos(-\pi + d_\theta n_\theta) -$
 349 $z_1) \times d_z)$, with $\text{int}()$ returning the closer integer. This can then be substitute in equation 12
 350 to calculate the velocity perceived by the blade \mathcal{U} , as function of its angular position θ .

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The quality of calculation of the angular velocity $\mathcal{U}(\theta)$ depends on the assumption that U is homogeneous along the y -axis. This assumption has been verified with previously acquired LDV measurements presented in [13]. A 2D cartography with 38 measurement points overall the turbine swept area has been carried out for the *Original grid* case and for a turbulent and shear case. Looking at the velocity cartographies, the mean velocity variations along the y -axis are small. Then, the velocity $\mathcal{U}(\theta)$ is calculated taking all the measurement points (over the entire rotor area) or just the points of the central line of the rotor and extruding it (as done in this paper). For the *Original grid* case, there is less than 1% difference between $\mathcal{U}(\theta)$ calculated from the central line and $\mathcal{U}(\theta)$ calculated from $\overline{U}(y, z)$. When the flow is sheared and turbulent, the difference is a bit larger: 2.5%. Thus, this assumption is correct and is responsible for less than 3% of error in the estimation of $\mathcal{U}(\theta)$.

The apparent velocities in the reference frame of the blade $\mathcal{U}(\theta)$ are presented in Figure 14. This figure shows that, for the three shear cases, the blade encounters different velocities while rotating. The velocity perceived by the blade $\mathcal{U}(\theta)$ is maximum for $\theta = 0$ rad, when the blade is at the top dead centre. For the *Panel 3* case, the velocity increases when the blade goes up, and decreases when the blade goes down. The difference between extreme values of $\mathcal{U}(\theta)$ is 0.09 m/s, which represents almost 10% of the mean value. However, results obtained for the *Panels 1* and *2* cases are more complex: some local peaks appears. A local minimum at $\theta = \pm\pi/2$ rad, i.e. when the blade is horizontally oriented, is observed for *Panel 1* and *Original grid*. At these positions, the entire surface of the blade is in the low-velocity area, observed in Figure 12. In the same way, a low-velocity zone appears around to $\theta = 0$ rad for the *Panel 2* case (see Figure 5). Consequently, the velocity perceived by the blade stays constant at $\mathcal{U} \simeq 1.02$ m/s, for $\theta \in [-\pi/2; \pi/2]$ rad.

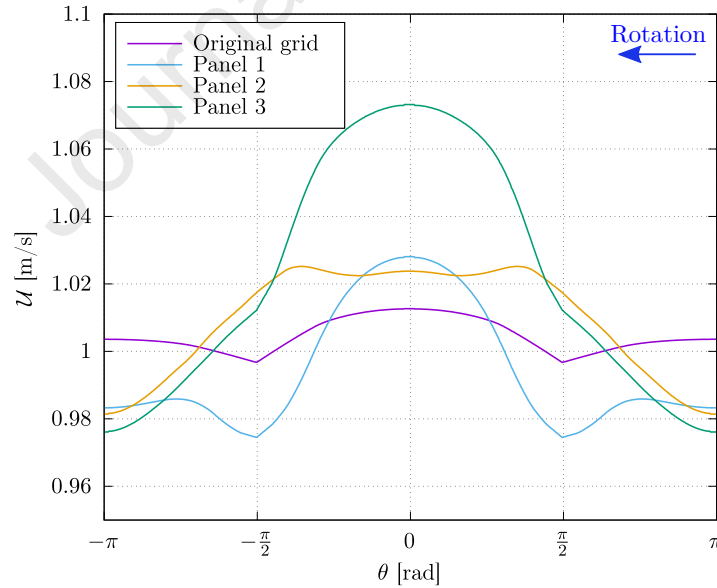


Figure 14: $\mathcal{U}(\theta)$ for blade 1 during its rotation, depending on θ . The direction of rotation is indicated by the blue arrow and corresponds to a negative direction.

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To help the understanding of the velocity \mathcal{U} evolution, two ideal cases are added. The first case is a perfectly constant velocity profile over the turbine height. The second case is a power-law presented in part 2.2. These both theoretical profiles with their corresponding measured profiles, i.e. *Original grid* and *Panel 3* cases respectively, are plotted in Figure 15.

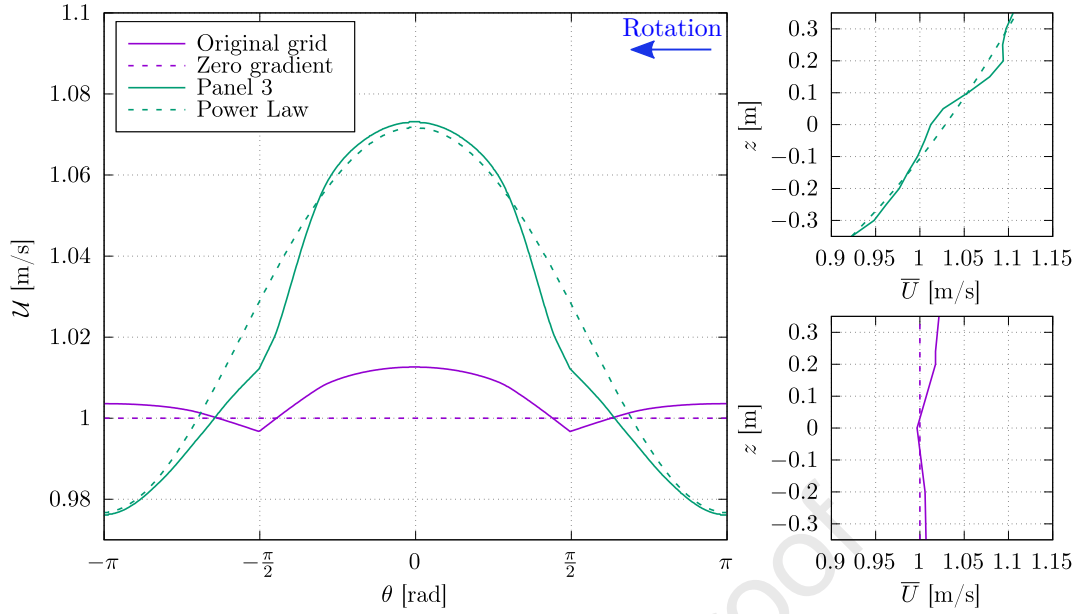


Figure 15: Superimposition of $U(\theta)$ velocities computed from the *Original grid* and *Panel 3* cases and approximations (left). Approximated velocity profiles are also plotted (right). The direction of rotation is indicated by the blue arrow and corresponds to a negative direction.

380 When comparing $U(\theta)$ in the case of the *Original grid* and a constant velocity profile
 381 (Figure 15), it appears that the *Original grid* creates small variations around $\theta = \pm\pi/2$ rad,
 382 which are explained by the low-velocity area around $z = 0$ m. For the *Panel 3* case, the power-
 383 law phase averaged velocity is very close to the real one. This approximation is relevant if we
 384 focus on the magnitude of variation during the blade rotation. The phenomena occurring at
 385 $\theta = -\pi/2$ rad and $\theta = +\pi/2$ rad are however not present in the power-law variation, because
 386 at these angles ($z \approx 0$ m) the velocity profile of *Panel 3* differs from the power-law velocity
 387 profile.

388 The velocity perceived by the blade while rotating varies because there is a vertical gradient.
 389 In fact, $U(\theta)$ is maximal when the blade is oriented towards the surface and minimal when it
 390 is oriented towards the bottom. This observation can be made for *Panel 1*, *2* and *3* cases, but
 391 there are other local extrema for the *Panel 1* and *2* cases.

392 3.3.2. Shear flow effect on blade loading

393 Figures 16 and 17 present the evolution of $\mathcal{F}_{x1}(\theta)$ and $U^2(\theta)$ for the *Original grid* case and
 394 *Panel 1* to *3* cases. For the *Original grid* case, the amplitude of variation of $\mathcal{F}_{x1}(\theta)$ represents
 395 2 N (3% of the mean value \bar{F}_{x1}). For the *Panel 3* case, the amplitude of variations of $\mathcal{F}_{x1}(\theta)$
 396 is larger. It represents 10 N that corresponds to 17% of \bar{F}_{x1} . For both cases, the behaviour
 397 of the loads $\mathcal{F}_{x1}(\theta)$ follows the behaviour of the velocity $U^2(\theta)$, but a varying phase delay is
 398 noticeable when the flow is sheared. For *Panel 3* case, this phase lag appears over the entire
 399 revolution and depends on the angular position θ of the studied blade.

400 Looking at *Panel 1* and *Panel 2* cases (Figure 17), the amplitude of variation of load
 401 and velocity are smaller than for *Panel 3*, representing approximately 5 N for the load that
 402 corresponds to 9% of \bar{F}_{x1} . There are also noticeably less similarities between both quantities
 403 but they still have globally a similar behaviour. For the *Panel 1* case, a phase lag between
 404 the highest load and the highest velocity is observed as for the *Panel 3* case. A local minima
 405 of the velocity appears as well for $\theta = \pm\pi/2$ rad. For $\theta = -\pi/2$ rad, load phase average is
 406 synchronised with this velocity local minimum but it is not the case for $\theta = +\pi/2$ rad. A

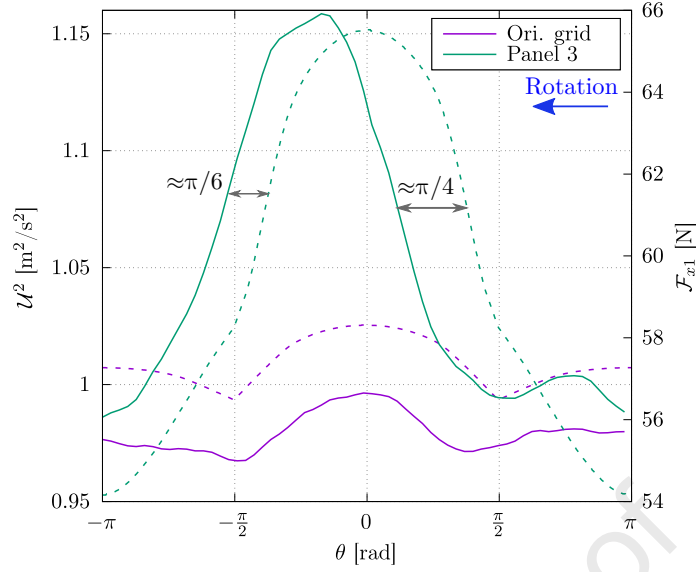


Figure 16: Load phase average on blade 1 $\mathcal{F}_{x1}(\theta)$ at $TSR = 4$ (solid line) compared with the squared velocity perceived by blade during its rotation $\mathcal{U}^2(\theta)$ (dashed-line) for *Original grid* and *Panel 3* cases. Horizontal grey arrows show how we estimate upward and downward phase lag. The direction of rotation is indicated by the blue arrow and corresponds to a negative direction.

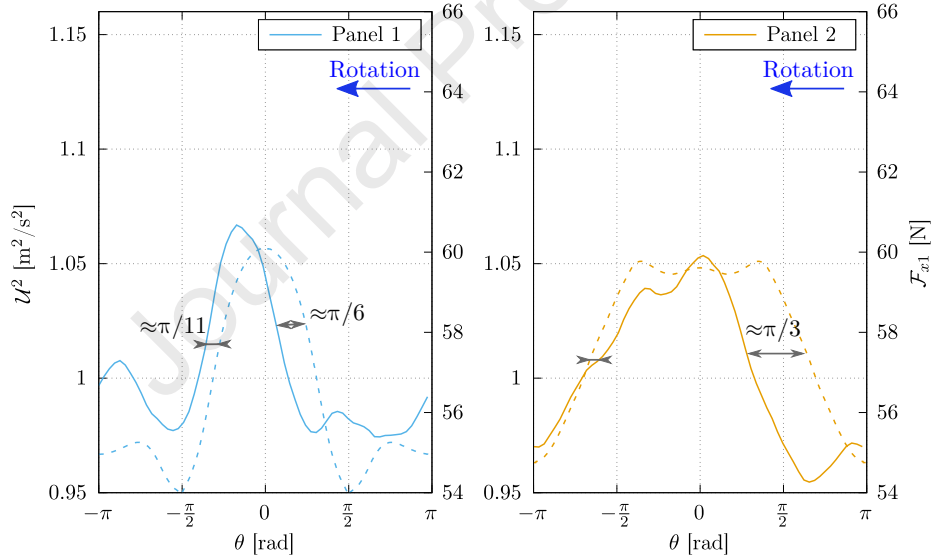


Figure 17: Load phase average on blade 1 $\mathcal{F}_x(\theta)$ at $TSR = 4$ (solid line) compared with the squared velocity seen by blade during its rotation $\mathcal{U}^2(\theta)$ (dashed-line) for *Panel 1* (left) and *Panel 2* (right) cases. Horizontal grey arrows show how we estimate upward and downward phase lag. The direction of rotation is indicated by the blue arrow and corresponds to a negative direction.

407 variable phase lag between both quantities appears as for *Panel 3*. For *Panel 2* case, the link
 408 between the load phase average and the squared velocity perceived by the blade is not as clear
 409 as for the three other cases. The main behaviour, with a maximum around $\theta \approx 0$ rad and a
 410 minimum around $\theta \approx \pm\pi$ rad, remains the same between load and squared velocity. For this
 411 case however, a global phase lag is difficult to identify as the shape of the two quantities differs.

412

413 These phase lags are then studied as a function of the blade movement. Upward and

414 downward phase lags are read in Figures 16 and 17 (horizontal grey arrows) and are summed
 415 up in table 4 for all *Panels* case. When $TSR = 4$, the turbine turns at $\omega = 11$ rad/s. So, the
 416 revolution period is 0.57 s. For all cases, the upward phase delay is larger than the downward
 417 phase delay. Depending on the case, the upward phase lag can represent up to $1/6^{\text{th}}$ of a
 418 revolution. The downward phase lag can represent up to $1/12^{\text{th}}$ of a revolution. This means
 419 that the load peak around $\theta = \pi/4$ rad is narrower (extend on a smaller range of θ) than the
 420 velocity peak centred around $\theta = 0$ rad.

Case	Upward phase delay	Downward phase delay
<i>Panel 1</i>	$\approx \pi/6$ rad \Leftrightarrow 0.05 s	$\approx \pi/11$ rad \Leftrightarrow 0.03 s
<i>Panel 2</i>	$\approx \pi/3$ rad \Leftrightarrow 0.10 s	—
<i>Panel 3</i>	$\approx \pi/4$ rad \Leftrightarrow 0.07 s	$\approx \pi/6$ rad \Leftrightarrow 0.05 s

Table 4: Phase delay estimation from Figures 16 and 17

421 To go deeper into this phase average comparison, the cross-correlation coefficient is calcu-
 422 lated between $\mathcal{F}_x(\theta)$ and $\mathcal{U}^2(\theta)$. For the sheared cases (*Panel 1*, *2* and *3*), a mean phase lag
 423 is read on the cross-correlation curve looking at the position of the maximum of correlation.
 424 These results are summed up in Table 5.

425 For the 3 cases, the maxima of cross-correlation coefficients are above 0.8. So, the phase
 426 average loads $\mathcal{F}_{x1}(\theta)$ are very similar to the phase squared velocities perceived by the blade
 427 $\mathcal{U}^2(\theta)$. The position of this maximum indicates the phase lag that enables the best similarity
 428 between these two compared quantities to be determined. The phase lag differs between the
 429 cases. These global phase lags, calculated from the cross-correlation, do not correspond to
 430 the upward and downward phase lag read on the Figures 16 and 17 (presented in table 4)
 431 as they are averaged over a revolution. For the *Panel 1* and *Panel 3* cases, a quite good
 432 correlation coefficient (≈ 0.9) is obtained between phase average loads and velocities. For the
 433 *Panel 2* case, even if velocity and load are less correlated, the signals stay strongly linked. This
 434 slightly lower cross-correlation coefficient is something expected looking at Figure 17, where
 435 the variations of the load are really different from the ones obtained for the velocity. In fact,
 436 the *Panel 2* velocity profile leads to more instationarities, explaining this lower correlation,
 437 due to its low velocity area at the rotor depth. These results show that the lag between $\mathcal{F}_{x1}(\theta)$
 438 and $\mathcal{U}^2(\theta)$ depends on the shear of the velocity profile.

Case (at $TSR = 4$)	Maximum correlation coefficient ρ_M [-]	Lag at ρ_M [s] or [rad]
<i>Panel 1</i>	0.91	0.3 $\approx \pi/10$
<i>Panel 2</i>	0.81	0.2 $\approx \pi/15$
<i>Panel 3</i>	0.88	0.4 $\approx \pi/8$

Table 5: Angular lag and correlation coefficient between squared velocity and load on blade 1, obtained with a cross-correlation, in the three gradient cases at $TSR = 4$.

439 For a better understanding of this phase lag phenomenon, $\mathcal{F}_{x1}(\theta)$ is plotted for different
 440 TSR and is again compared to $\mathcal{U}^2(\theta)$ for *Panel 3* case (Figure 18). This figure shows that,
 441 until $TSR4$, the phase lag between $\mathcal{F}_{x1}(\theta)$ and $\mathcal{U}^2(\theta)$ increases when the rotational speed
 442 of the turbine increases. Also, when the rotational speed of the turbine increases, the load
 443 amplitude increases as well. This exactly corresponds to the thrust coefficient which increases
 444 with the TSR . Looking at what happens when the TSR is high, the turbine blade perceives
 445 larger load fluctuations at a higher frequency than for lower TSR . Consequently, these two
 446 phenomena add up so that it leads to worse the effects for the turbine blade, especially in a

447 material fatigue point of view. These conclusions are also observed for *Panel 1* case, but it
 448 is less obvious for the *Panel 2* case.

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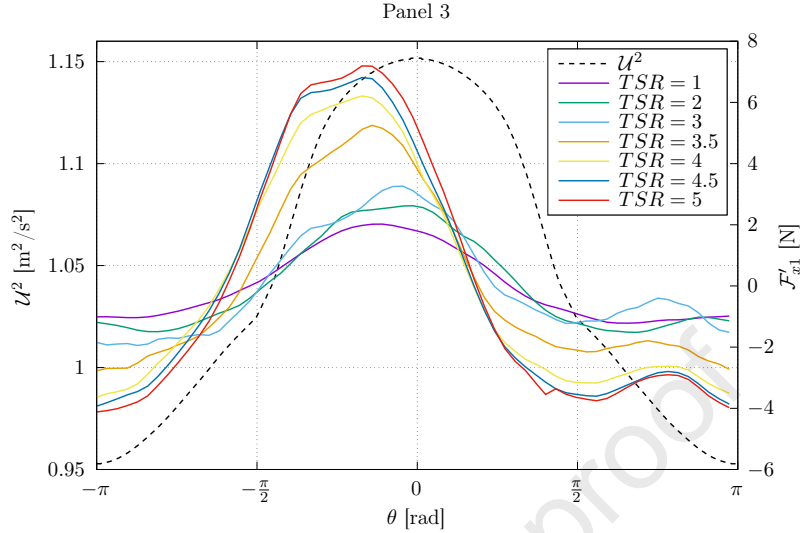


Figure 18: Load phase average on blade 1 $\mathcal{F}_{x1}(\theta)$ (solid line) compared with the squared velocity seen by blade during its rotation $U^2(\theta)$ (dashed-line) for *Panel 3* case.

450 The phase lag observed between $\mathcal{F}_{x1}(\theta)$ and $U^2(\theta)$ depends in fact of many parameters.
 451 First of all, the velocity profile used to calculate the velocity perceived by the blade have been
 452 measured without the turbine in the flow. However, the presence of the turbine strongly modify
 453 and slow down the flow in front of it. This speed reduction is directly linked to the solidity of
 454 the rotor, so depends on the probability of occurrence of the blades and on the hub geometry.
 455 This is thus non homogeneous over the turbine rotor and modifies the incoming velocity profile
 456 [15, 8]. Moreover, the turbine drives a part of the surrounding flow in rotation. The flow is
 457 deflected from its original direction. This effect has been observed before both numerically
 458 and experimentally by Payne et al. [33] and Mason-Jones et al. [26]. The combination of these
 459 two effects is called the induction effect of the turbine [28].

460 In concrete more terms, this deflection of the flow by the turbine is certainly dependent on
 461 its rotational speed. In addition, the way the flow is slowed down by the solidity of the turbine
 462 depends on the incoming flow velocity profile and on the turbine rotational speed. Combining
 463 both effects, as they are interdependent, the shape of the velocity profile is homogeneously
 464 modified along the r -axis, thus along the y and z -axis. The velocity gradient wrap around
 465 the turbine in the rotation direction, toward $-\theta$. The velocity perceived by the blade is thus
 466 maximum a bit after $\theta = 0$ rad, so at $\theta < 0$ rad.

467 The induction effect of the turbine does not however fully explain:

- 468 • the evolution of the phase lag between $\mathcal{F}_{x1}(\theta)$ and $U^2(\theta)$ versus θ ,
- 469 • the difference between the θ range width where $\mathcal{F}_{x1}(\theta)$ and $U^2(\theta)$ are high.

470 In fact, this reduction of the load peak width is likely due to a combination of the phenomena
 471 previously exposed and the fact that the blade's lift evolves during a revolution, due to the
 472 apparent velocity of the blade which changes during a revolution. This complex hydrodynamic
 473 phenomena are linked to the blade profile, the pitch and the turbine rotational speed and need
 474 further investigations to deeper understand these points.

475 4. Conclusion

476 The common generated flow in the IFREMER flume tank presents a low turbulence level,
 477 and a uniform vertical velocity profile over the tank height, excepted in the boundary layer.
 478 Three grid arrangements, named *Panels*, have been created to modify the vertical velocity
 479 profile of the tank, which have been characterized thanks to a 3C LDV system. *Panel 3*
 480 recreates a power-law profile ($\alpha = 4$), corresponding to the *in-situ* most sheared profiles. The
 481 two others, *Panels 1* and *2*, create more complex vertical velocity profiles as they present low-
 482 velocity at some specific heights. When looking at these velocity profiles on the area swept
 483 by the studied tidal turbine, these four cases are comparable in terms of mean velocity and
 484 turbulence intensity level. Thus, it enables the impact of shear incoming velocity profile on a
 485 horizontal-axis three-bladed tidal turbine to be studied.

486 The first step of the study is to evaluate the turbine global performance, using the power
 487 coefficient C_p . The calculation of the C_p requires to choose a characteristic velocity. This
 488 velocity is generally taken at the hub height, but in our case, velocity profiles are sheared over
 489 the rotor height. Thus, the velocity at the centre of the rotor is non-representative of the
 490 velocity perceived by the turbine. To overcome this problem, we use an equivalent velocity
 491 defined as the velocity averaged on the rotor height pondered by the area swept by blades.
 492 We show that, under this assumption, C_p is the same in the four cases, so the shape of the
 493 velocity profile does not impact the global turbine performance, providing the mean velocity
 494 remains similar in all cases, as it has been found for wind turbines.

495 Then, the focus is done on the horizontal load F_x on one blade. When the flow is sheared,
 496 the time evolution of F_x is partially periodic, and the amplitude of variations increases with
 497 the shear. The spectral analysis confirms that load is linked to the turbine rotation cycle as
 498 a peak appears at 1 to 3 times the rotation frequency of the turbine. Owing to this link, we
 499 calculate the phase average of F_x . We thus conclude that when the flow is sheared, $\mathcal{F}_x(\theta)$
 500 presents a maximum between $\theta = -\pi/4$ rad and $\theta = 0$ rad which seems to be linked to an
 501 azimuthal velocity component due to the blade rotation.

502 Given that vertical velocity gradient has an impact on blade loading, we investigate the
 503 link between velocity perceived by a blade and its corresponding load. To do so, we calculate
 504 the velocity perceived by the blade at each rotation angle $\mathcal{U}(\theta)$ from the velocity profile coming
 505 from LDV measurements and knowing that $\bar{U}(z)$ is almost constant along the y -axis. First,
 506 we show that in the ideal case where the velocity profile follows a power-law, $\mathcal{U}(\theta)$ varies to
 507 reach a maximum at $\theta = 0$ rad, with a variation amplitude of 10%. Next, the phase average
 508 of load is compared with the squared velocity perceived by the blade, and it appears that
 509 the variation of these two quantities are very similar. Consequently, the cross-correlation co-
 510 efficient between $\mathcal{F}_x(\theta)$ and $\mathcal{U}^2(\theta)$ is calculated. This coefficient reaches maximum value of
 511 0.9 for a phase lag depending on the TSR and the incoming flow velocity profile. The link
 512 between the blade load and the squared velocity is thus established even if small differences
 513 are present. These differences are related to the turbine induction effects, which slow down
 514 the flow in front of the turbine in a inhomogeneous way and put it in rotation, and also to
 515 complex hydrodynamic phenomena around the blades.

516
 517 This study is a first step to understand the effect of shear velocity profiles on tidal turbines.
 518 The long-term goal is to estimate, from *in-situ* measurements of the velocity profile, the blade
 519 load range and the load behaviour as function of the position of the turbine in the flow and
 520 of the angular position θ of the blades. To reach this goal, a wider range of conditions have
 521 to be tested and compared such as other incoming velocity profiles, with high turbulence
 522 level, changes in the solidity (number of blades) of the rotor, not only for horizontal axis tidal
 523 turbine. Further studies have to be conducted as well, looking at the changes of velocity profile

524 due to the induction of the turbine, using PIV or LDV measurement just in front of the rotor
525 plane. Moreover, a fatigue study could be led to see how these very frequent and low intensity
526 load fluctuations impact the durability of the turbine blade and make it more sensible to other
527 external solicitations.

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Declaration of interests

- The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.
- The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

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