1 *Supplementary Information*

A transient CGCM simulation of the past 3 million years

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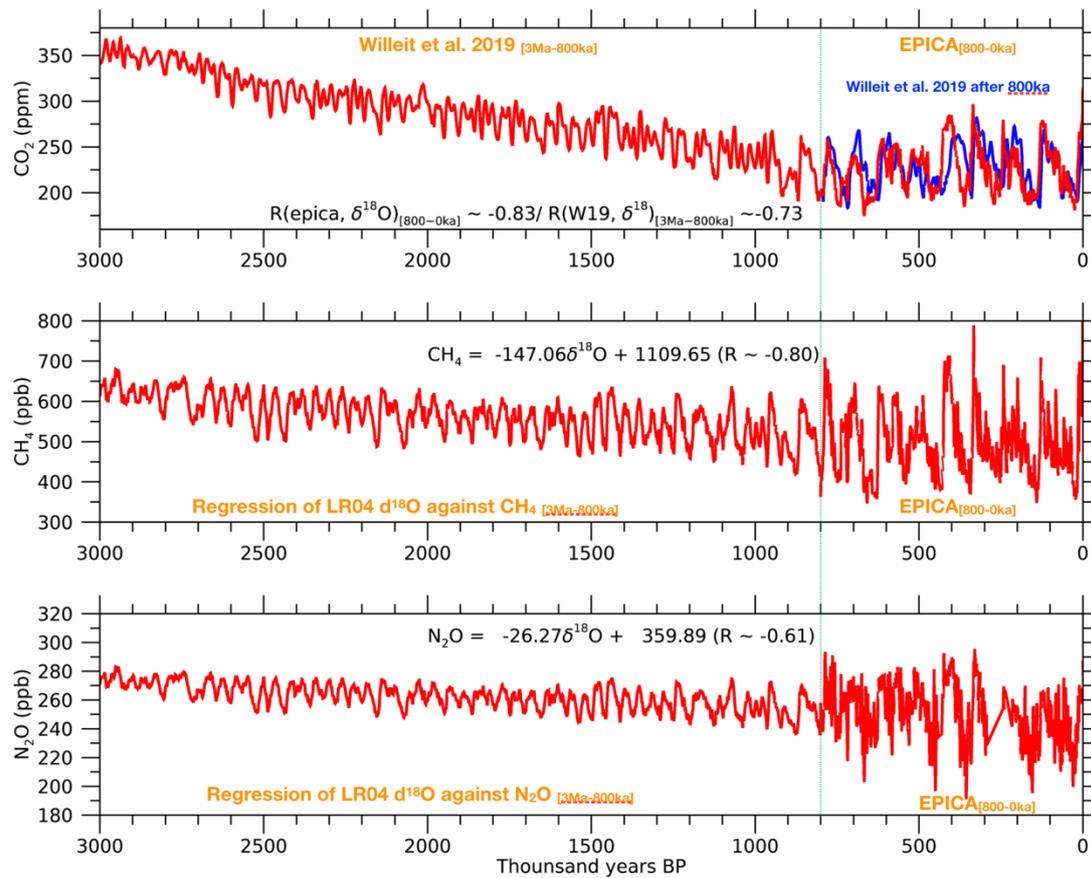
Figure S1 | Greenhouse-gases forcing. (a) Reconstructed CO_2 forcing (red) by combining two datasets of the European Project for Ice Coring in Antarctica (EPICA) Dome ice core data (Lüthi et al. 2008) after 800ka and Willeit et al. (2019) before 800ka. Blue line indicates the CO_2 forcing from Willeit et al. (2019). (b-c) Reconstructed (b) CH_4 and (c) N_2O forcings by combining two datasets of EPICA CH_4 (Loulergue et al. 2008) and N_2O (Spahni et al. 2005) data after 800ka and regression model before 800ka. Here, the regression was conducted using the linear relationship between LR04 stack (Lisiecki and Raymo 2005) and the greenhouse-gases during the EPICA 800 kyr. The regression coefficients were displayed by equation of each panel.

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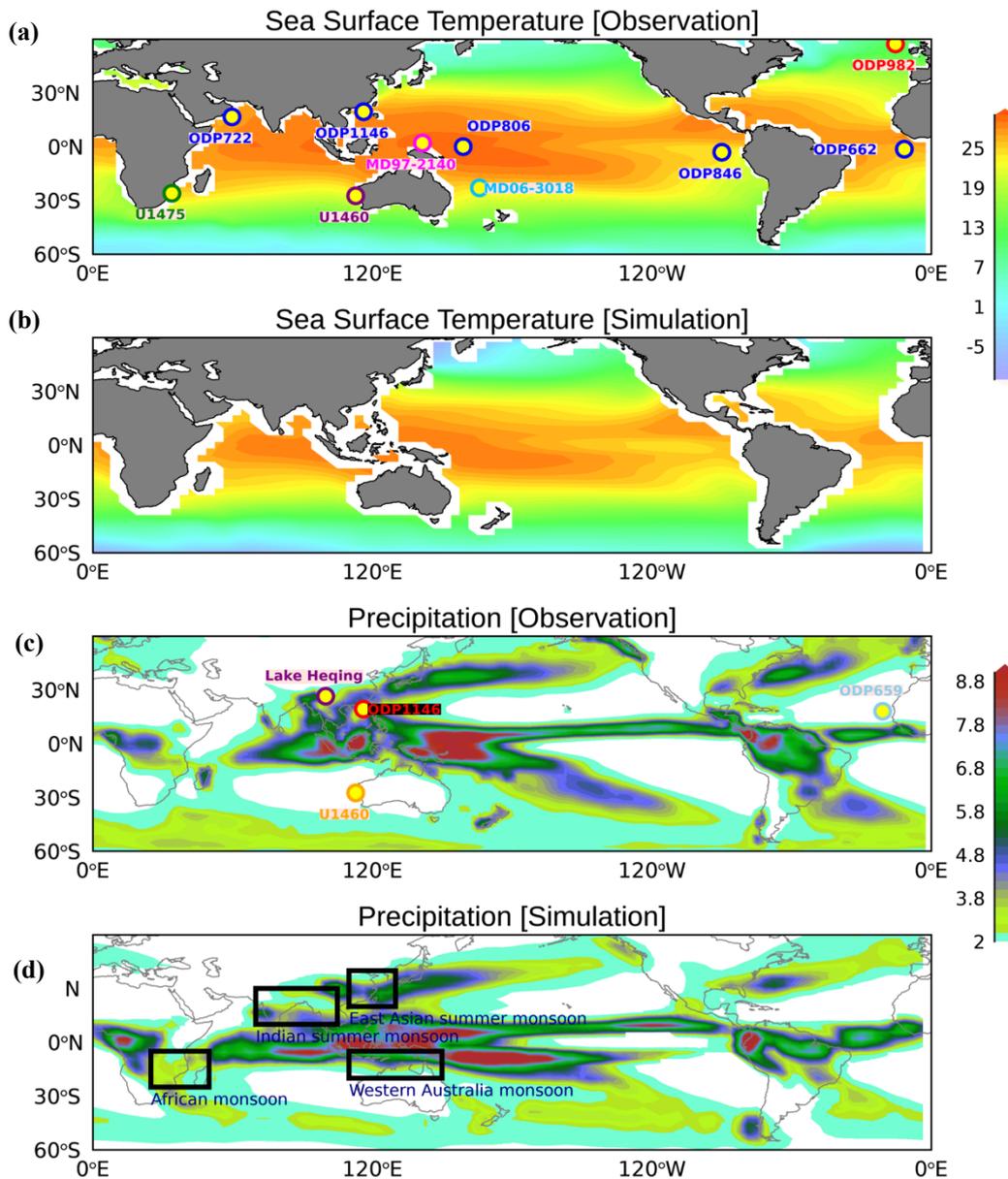
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Figure S2 | SST and precipitation pattern. (a) Observed SST pattern during 1979-2008 from ERSST5 and proxy locations used in this study. (b) Simulated SST pattern over the entire 3Myr. (c) Observed precipitation pattern during 1979-2008 from GPCP and proxy locations. (d) Simulated precipitation pattern over the 3Myr and monsoon domains used in this study.

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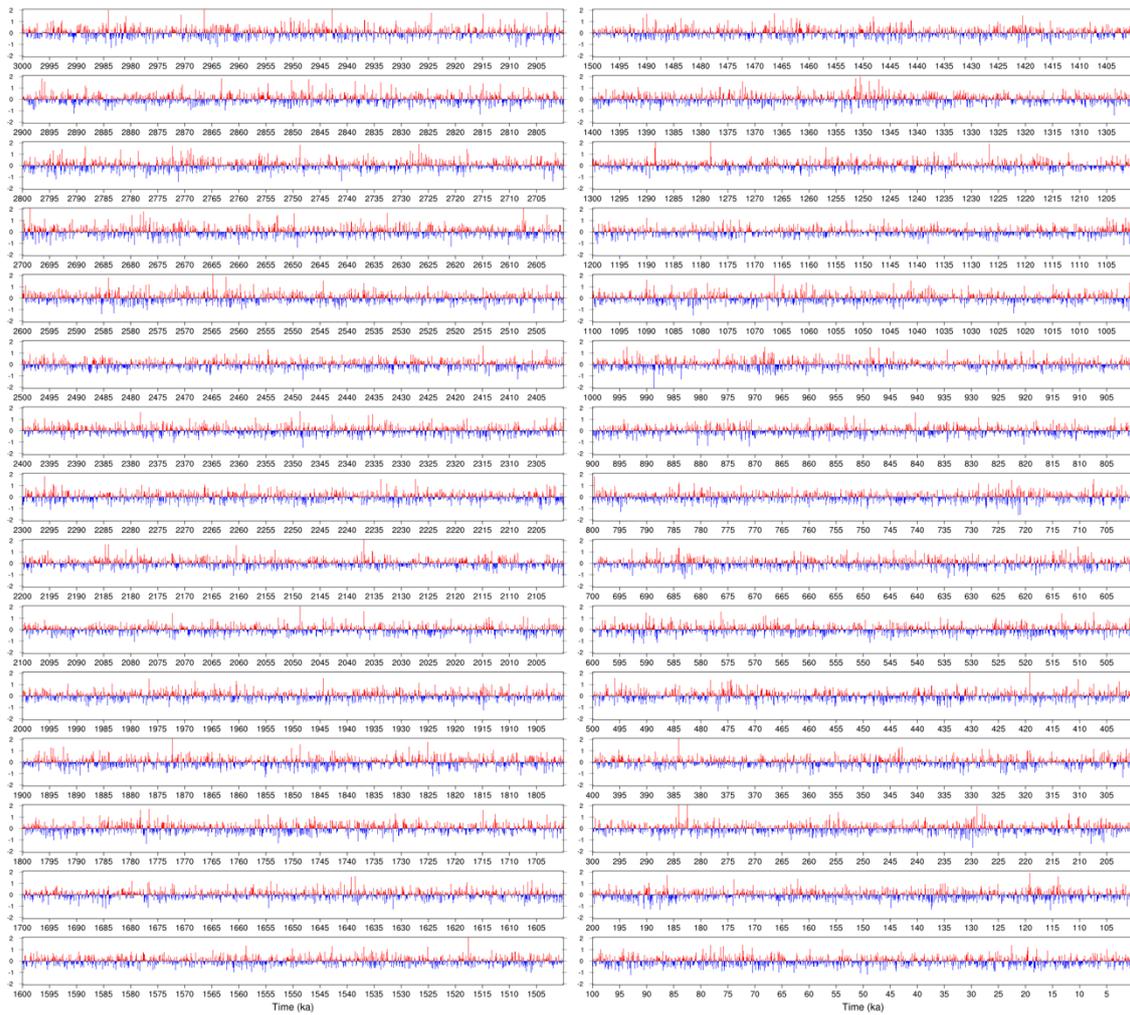
Figure S3 | Monthly ENSO variability. Timeseries of Niño 3 index defined as 1.5-7-year band-pass filtered Niño 3 SST.

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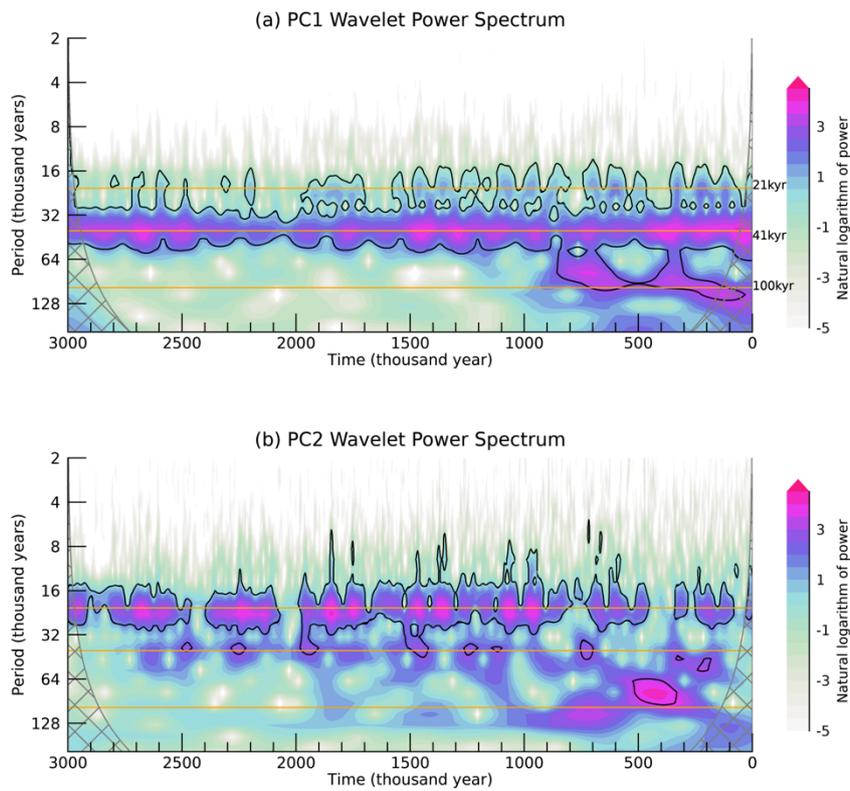
Figure S4 | Wavelet power spectrum of PCs of two dominant MHT modes. The wavelet power spectrum of (a) PC1, and (b) PC2. The black contour indicates the value significant at the 95% confidence level. The horizonal orange lines show 21-kyr (precession), 41-kyr (obliquity), and 100-kyr (eccentricity) periods.
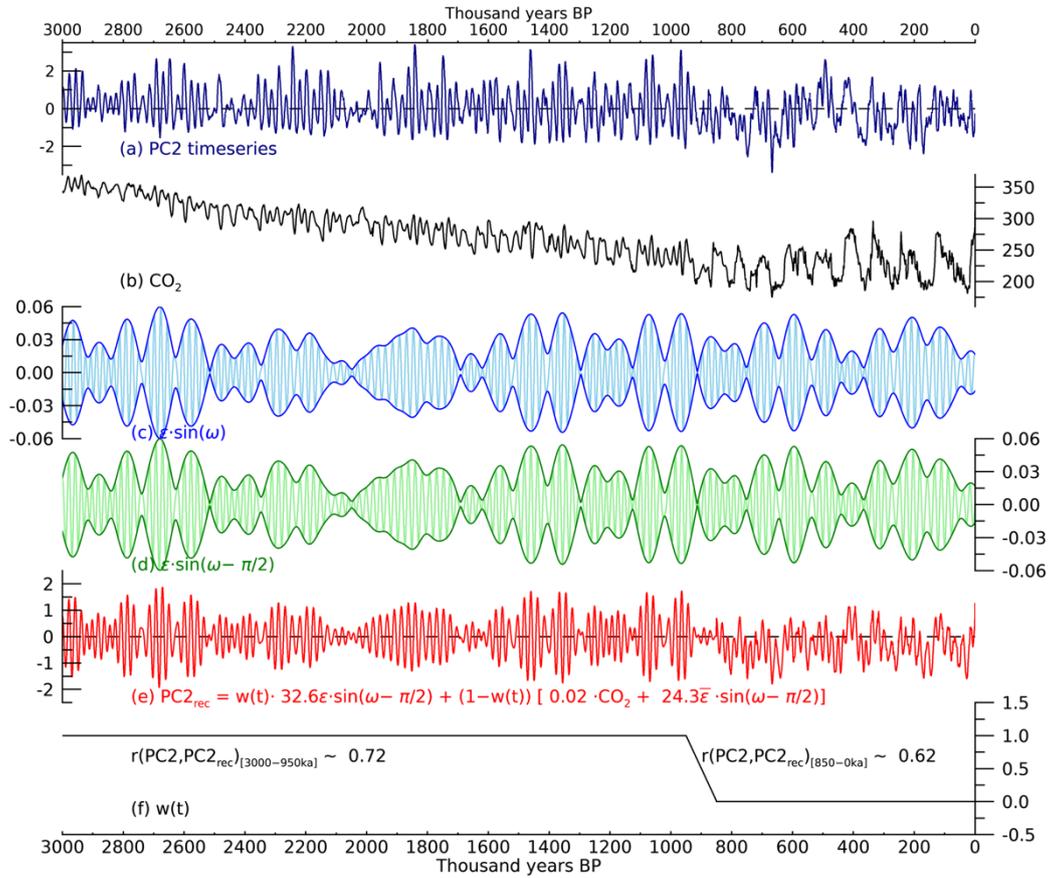
Figure S5 | A simple model for reconstruing PC2 time series using eccentricity-modulated precession and CO₂. (a) Original PC2 time series, (b) CO_2 forcing, (c) eccentricity (blue)-modulated precession (sky blue) variability. (d) 90° out-of-phase precession variability, (e) reconstructed PC2 time series using 90° out-of-phase precession and CO_2 forcing, and (f) weight function in the reconstruction. The coefficients in (e) are obtained using a simple regression model against the PC2 time series.
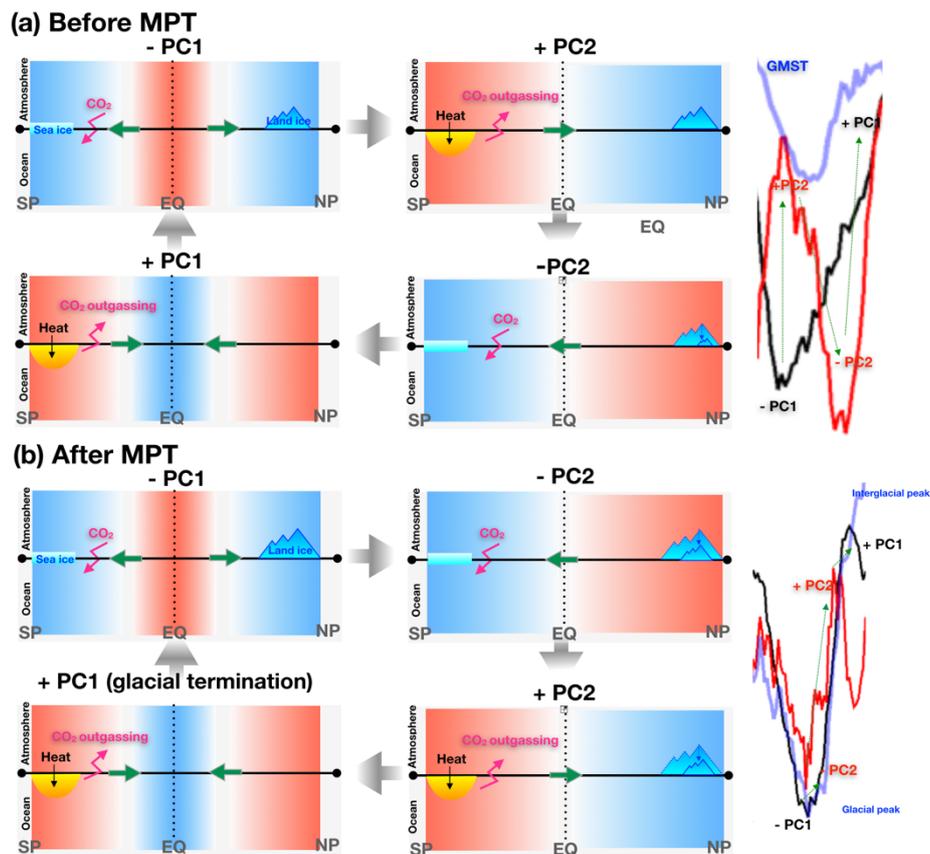
Figure S6 | PC1-PC2 cycle and the potential feedback with carbon cycle. The cycle of PC1 and PC2 (a) before the MPT and (b) after the MPT. Before the MPT, the negative PC1 tends to be followed by the positive PC2 and it becomes the other way around. Meanwhile, after the MPT, the negative PC1 tends to be followed by the negative PC2 during the glacial peak. The transition into positive phases of PC2 and PC1 is concurrent with the glacial termination. The negative phases of PC1 and PC2 are likely to enhance the Southern Ocean CO_2 sequestration into the ocean, associated with the sea ice/carbon cycle feedback (Stein et al. 2020). By contrast, the positive phases of PC1 and PC2 are related to the Southern Ocean warming and the enhanced CO_2 leak outgoing into the atmosphere. Here, blue (red) shading and green arrow show an anomalous cooling (warming) and direction of heat transport.

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