1	Improvements of a process-based model for 2- and 3-dimensional simulation of flow in
2	presence of various obstructions
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21 Abstract

In coastal areas, various types of biological and anthropic structures significantly influence 22 the flow and related sediment dynamics. In this paper we have developed a generic flow-23 24 obstruction module, designed to represent both upward or downward, rigid or flexible structures, using a limited number of parameters. This module can be integrated to any 25 hydrodynamic coastal model. The obstruction/flow interactions module can operate either in 26 3D or 2D mode. It calculates source terms used in momentum equation and in the k- ε 27 turbulent closure model (exclusive to 3D mode). Additionally, the module allows for the 28 incorporation of multiple obstructions within a single mesh, which is invaluable when 29 modelling realistic ecosystem dynamics. The module's validation was carried out using flume 30 experiments on seagrasses, as well as using numerical studies involving two anthropogenic 31 structures: mussel long-lines and oyster tables. The coupled hydrodynamic/obstruction model 32 yielded excellent results for 2D/3D velocity fields with minimal calibration efforts. This 33 module offers the potential to explore the future trajectories of vulnerable coastal systems in 34 response to global change, or to identify restoration measures in engineered coastal systems. 35

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Keywords: Obstructed flow, Submarine vegetation, Anthropic structures, Turbulence,
Hydrodynamic modelling

40 **1. Introduction**

In coastal areas, various types of biological and anthropic structures are prevalent, including 41 seagrass beds, salt-marshes vegetation, oyster tables, mussel posts, rafts, and lines, among 42 43 others. These structures interact significantly with hydrodynamics. They are directly influenced by the flow, and in turn, they locally and regionally modify (seagrass beds: 44 Fonseca and Fisher, 1986; Nepf, 1999; salt-marshes vegetation: Bouma et al., 2007; oyster 45 tables: Kervella et al., 2010; mussel posts: Delaux et al., 2011). By damping hydrodynamic 46 energy from tidal currents and waves, these obstructions strongly influence the transport of 47 dissolved and particulate substances, such as sediments, nutrients, pollutants and larvae. 48 Directly or indirectly, they also modulate erosion-deposition processes, thereby impacting the 49 morphological evolution of coastal ecosystems across various spatial and temporal scales 50 (Temmerman et al., 2005; Le Hir et al., 2007; Fagherazzi et al., 2012). 51

More specifically, seagrasses are often referred to as ecosystem engineers because they 52 locally attenuate currents and waves, promoting sediment deposition and retention (Ward et 53 al., 1984; Lacy and Wyllie-Echeverria, 2011; Ganthy et al., 2015). Increased water clarity 54 resulting from this sediment trapping enhances light penetration, fostering their 55 photosynthetic activity and potential growth (Carr et al., 2010). Oyster and mussels farming 56 techniques lead to sediment accumulation beneath and around the structures (Sornin, 1981), 57 attributable to both reduced flow energy and bio-deposition (Kaiser et al., 1998). This induces 58 cascading effects on nutrient fluxes, benthic fauna and shellfish production itself (Harstein et 59 al., 2004; Giles et al., 2006; Weise et al., 2009). 60

In the context of global change, evaluating and predicting changes in the status of coastal habitats and ecosystems has become increasingly important for coastal managers and scientists (Montefalcone, 2009). Considering the effects of various obstructions on

hydrodynamics and, subsequently, on the transport of dissolved and particulate matter is 64 critical for estimating the ecological and morphological status and trajectories of coastal 65 ecosystems. However, due to the inherent complexity of coastal ecosystems (e.g., complex 66 morphology, spatio-temporal variations in vegetation distribution and/or shellfish farming 67 structures, non-linearity between hydro-sedimentary processes), laboratory or field data 68 cannot be directly extrapolated to a large coastal scale. Coastal numerical models offer 69 powerful complementary capabilities to investigate these complex processes and the potential 70 ecosystem response to future changes in environmental forcing or human pressures. 71

Over the past few decades, several studies have simulated the effects of various benthic 72 vegetation (i.e., flexible/rigid, submerged/emerged) on flow (e.g., Morin et al., 2000; 73 Abdelrhman, 2003; Temmerman et al., 2005; Gao et al., 2011; Zhang et al., 2013; 74 Kombiadou et al., 2014; Weitzman et al., 2015; Beudin et al., 2017). However, most of these 75 studies were either species-specific or dedicated to small-scale investigations without being 76 applied at the scale of an entire coastal system. Only a few coastal models account for the 77 three-dimensional effects of benthic vegetation on mean and turbulent flows (Temmerman et 78 79 al., 2005; Kombiadou et al., 2014; Beudin et al., 2017; Donatelli et al., 2018). Even fewer studies have addressed the simulation of hydrodynamics in the presence of shellfish farming 80 structures (Delaux et al., 2011; Gaurier et al., 2011; Duarte et al., 2014), with similar 81 limitations observed in vegetation-flow modelling (i.e., only a few models dedicated to the 82 scale of a coastal system). Furthermore, no coastal model is currently capable of simulating 83 the three-dimensional cumulative effects of complex associations of flow obstructions (e.g., 84 85 seagrass beds located beneath oyster tables or mussel lines, multi-specific assemblages of 86 benthic vegetation) on water flow.

Within this context, the present work focuses on the comprehensive description of recent 87 improvements made to a generic flow-obstruction module previously described by 88 Kombiadou et al. (2014) for the specific case of the seagrass Zostera noltei and applied to the 89 Arcachon Bay. These module improvements include: (1) the development of a generic 90 module adapted to various types of natural and anthropogenic obstructions found in coastal 91 ecosystems (i.e., rigid/flexible, submerged/emerged, upward/downward); (2) the ability to 92 define multiple obstruction types within the same grid cell; and (3) the utilization of a 93 minimal, optimized number of empirical calibration parameters. The present paper 94 encompasses small-scale module validation, sensitivity analysis, and a discussion on potential 95 module limitations and future improvements. 96

97 **2. Methods**

The flow-obstruction module, referred to as the OBSTRUCTIONS module, was initially 98 99 implemented within the MARS model (Model for Application at Regional Scale; Lazure and Dumas, 2008). The MARS model is a three-dimensional, primitive equations, split implicit 100 free surface, sigma coordinate hydrodynamic model designed to simulate flows across various 101 coastal areas, ranging from regional scales (i.e., continental shelves) to local scales (i.e., small 102 bays and estuaries). The OBSTRUCTIONS module has been designed for easy coupling with 103 any hydrodynamic model that shares similar specifications and is currently being integrated 104 into the CROCO model (https://croco-ocean.org/). 105

106 The MARS model couples barotropic and baroclinic modes and solves the primitive equations 107 (Navier-Stokes equations based on the classic Boussinesq and hydrostatic hypotheses) using a 108 semi-implicit scheme with finite differences on an Arakawa C grid. Bottom friction is 109 computed based on the approximation of constant turbulent stress between the first computed 110 velocity level and the bottom, leading to a user-defined roughness length (z_0). Additionally, 111 the vertical turbulence closure scheme is formulated in a unified manner (Generic Length 112 Scale) according to Umlauf and Burchard (2003), encompassing k-kl, k- ε , or k- ω 113 formulations.

To prevent the creation of very thin sigma layers at low water depths, the baroclinic mode is terminated below a user-defined water level threshold value. In such cases, advection is performed as depth-averaged, and vertical velocity profiles are theoretically computed based on the classical Law of the Wall method.

The MARS modelling platform (https://mars3d.ifremer.fr; in French) also includes additional modules that allow for the coupling of hydrodynamics, sediment dynamics, biogeochemical cycles, and ecological models for phytoplankton and seagrass growth (see, among others, Guillaud *et al.*, 2000; Plus *et al.*, 2003; Le Hir *et al.*, 2011; Huret *et al.*, 2013; Mengual *et al.*, 2017). The present work represents a significant advancement in the development of an integrated, fully coupled ecosystem model, bridging the gap between physics, ecology, and human impacts.

125 **2.1. Description of the OBSTRUCTIONS module**

The OBSTRUCTIONS module has been integrated with the hydrodynamic MARS model. 126 Initially designed to characterize the three-dimensional hydrodynamic effects of flexible 127 seagrass Zostera noltei on flow (Kombiadou et al., 2014), the module has been updated to 128 allow the simulation of various types of obstructions (Figure 1). The numerical scheme has 129 also been modified to accommodate multiple obstructions within the same grid cell (e.g., 130 131 seagrass and oyster tables), and the computation procedure for the height of flexible obstructions has been refined. Additionally, a theoretical velocity profile has been introduced 132 for cases where baroclinic computation is terminated due to shallow water depths. This 133

enhancement aims to better replicate bottom velocities used to compute bottom shear stresswhen simulating sediment dynamics. These new developments are detailed below.

- 136 Currently, the module can account for three generic types of obstructions (Figure 1a):
- *Upward obstructions* (UP): Obstructions that start from the seabed and extend
 upwards towards the water surface (*e.g.*, vegetation, mussel posts). These
 obstructions can be either rigid or flexible.
- *Downward obstructions* (DO): Obstructions that start from the water surface and
 hang downwards towards the seabed (*e.g.*, mussel/oyster lines). Similar to UP
 types, these obstructions can be either rigid or flexible.
- *Three-dimensional obstructions* (O3D): A specific subtype of the upward type,
 O3D describes obstructions located in mid-water, without structures near the
 seabed or surface. This particular type is typically used to represent oyster bags
 and is associated with an UP obstruction to simulate oyster tables.



Figure 1: (a.) simplified representation of the three types of obstructions allowed within the
module and (b.) pictures of real obstructions to be simulated: seagrass meadows (upper
right), mussel long-line (lower left) and oyster tables (lower right).

151

152 **2.1.1. 3D equations for obstruction/flow interactions**

The influence of obstruction elements on three-dimensional flow is accounted for by: i) the loss of momentum due to the drag exerted on obstruction elements, and ii) the balance between turbulence production and dissipation introduced within the k- ε turbulence closure scheme. This scheme is primarily used in coastal environments (Temmerman *et al.*, 2005; Casamitjana *et al.*, 2012) and is one of the simplest models suitable for flow-obstruction modeling (Uittenbogaard, 2003). Each obstruction element can be described in two ways depending on its geometry: cylinderlike (*e.g.*, reeds or mussel ropes, Figure 2a) or parallelepiped-like (*e.g.*, seagrass leaves, Figure 2b). For the cylinder-like case, obstructions are characterized by their diameter ($d_0(z)$, m) and the number of elements per unit area (n(z), m⁻²), referred to as element density hereafter. In the parallelepiped-like case, the diameter is replaced by the obstruction's width (w(z), m) and thickness ($t_0(z)$, m), where z refers to the height above the bed, corresponding to the vertical mesh grid of the hydrodynamic model.

a. Cylinder-like obstruction



b. Parallelepiped-like obstruction



167

Figure 2: Schematic representation of a single obstruction element, (a.) for cylinder-like
 element, and (b.) for parallelepiped-like element. For bent case, variables are described in
 section 2.1.3.

171 The drag induced by all obstruction elements is accounted for as a momentum loss term 172 (friction force) in x and y directions:

173
$$F_{u}(z) = -\frac{1}{2} \cdot C_{D} \cdot \rho \cdot d_{0}(z) \cdot n(z) \cdot u(z) \cdot \sqrt{u(z)^{2} + v(z)^{2}} \cdot f_{z}(z) \cdot f_{xy}(z)$$
(1a)

174
$$F_{v}(z) = -\frac{1}{2} \cdot C_{D} \cdot \rho \cdot d_{0}(z) \cdot n(z) \cdot v(z) \cdot \sqrt{u(z)^{2} + v(z)^{2}} \cdot f_{z}(z) \cdot f_{xy}(z)$$
 (1b)

In the equations above, corresponding to the cylinder-like case, C_D is the drag coefficient for 176 obstructions (-), ρ is the water density (kg.m⁻³), u(z) and v(z) are the horizontal flow velocities 177 (m.s⁻¹) in x and y directions, respectively, $f_z(z)$ and $f_{xy}(z)$ represent the vertical fraction of the 178 layer and the horizontal fraction of the grid cell effectively occupied by obstructions (-). For 179 the parallelepiped-like case, primarily used to represent seagrass leaves, $d_0(z)$ is substituted 180 by w(z) in equations (eq. 1a and 1b). Indeed, leaf inertia is considered to be weaker in the 181 direction perpendicular to its width, so that leaves are assumed to align with their width facing 182 the flow. 183

184 The influence of obstructions on turbulence leads to additional source terms in the equations 185 of the *k*- ε turbulence closure scheme (Temmerman *et al.*, 2005). The equations for turbulent 186 kinetic energy (*k*, m².s⁻², eq. 2) and the turbulent energy dissipation (ε , m².s⁻³, eq. 3) become:

187
$$\left(\frac{\partial k}{\partial t}\right)_{obstruction} = \frac{1}{1 - A(z)} \cdot \frac{\partial}{\partial z} \left\{ \left(1 - A(z)\right) \cdot \frac{\nu + \nu_t}{\sigma_k} \cdot \frac{\partial k}{\partial z} \right\} + T(z)$$
(2)

188
$$\left(\frac{\partial\varepsilon}{\partial t}\right)_{obstruction} = \frac{1}{1 - A(z)} \cdot \frac{\partial}{\partial z} \left\{ (1 - A(z)) \cdot \frac{\nu + \nu_t}{\sigma_{\varepsilon}} \cdot \frac{\partial\varepsilon}{\partial z} \right\} + T(z) \cdot \tau_{\varepsilon}^{-1}$$
(3)

Where A(z) is the horizontal cross-sectional obstruction area per unit area (-) at level z (eq. 4a for cylinder-like case and eq. 4b for parallelepiped-like case respectively), v and v_t are molecular and eddy viscosities (m².s⁻¹), σ_k and σ_{ε} are turbulent Prandtl-Schmidt numbers for self-mixing turbulence (σ_k =1 and σ_{ε} =1.3). T(z) represents the work spent by the fluid (m².s⁻³) at level z (eq. 5) and τ_{ε} is the energy dissipation timescale (eq. 6), which corresponds to the minimum value between the dissipation of free turbulence and the dissipation of eddies between obstruction elements.

196
$$A(z) = \frac{\pi}{4} \cdot d_0(z)^2 \cdot n(z) \cdot f_{xy}(z)$$
 (4a)

197
$$A(z) = w(z) \cdot t_0(z) \cdot n(z) \cdot f_{xy}(z)$$
(4b)
198
$$T(z) = \frac{\sqrt{(F_u(z) \cdot u(z))^2 + (F_v(z) \cdot v(z))^2}}{\rho}$$
(5)
199
$$\tau_{\varepsilon} = MIN\left[\frac{1}{c_{2\varepsilon}} \cdot \left(\frac{k}{\varepsilon}\right), \frac{1}{c_{2\varepsilon}} \cdot \sqrt{c_{\mu}} \cdot \left(\frac{L(z)^2}{T(z)}\right)^{\frac{1}{3}}\right]$$
(6)
200
$$L(z) = c_{lz} \cdot \sqrt{\frac{1 - A(z)}{n(z)}}$$
(7)

The values of coefficients
$$c_{2\varepsilon}$$
 and c_{μ} are 1.96 and 0.09, respectively (Temmerman *et al.*,
202 2005). $L(z)$ represents the typical size of eddies, which is limited by the smallest distance
203 between obstruction elements. For rigid vertical cylinders, $c_{lz}\approx 1.0$, whereas lower values
204 ($c_{lz}\approx 0.3$) have been found to be applicable for flexible vegetation (Uittenbogaard, 2003).

205

206 2.1.2. 2D equations for obstruction/flow interactions

In the barotropic mode, the friction terms ($F_u(z)$ and $F_v(z)$) are depth-averaged and introduced within the barotropic momentum equation. Additionally, for near-bed velocity analysis and sediment dynamics (i.e., computation of bottom shear stress), a theoretical computation of the velocity profile is conducted when the baroclinic mode is terminated. Currently, this is computed only for upward obstructions (UP).

When obstructions occupy more than 90% of the total water depth, they are considered as emergent or nearly emergent. In such cases, velocity profiles are computed using the userdefined roughness length (z_0 , m), in accordance with the classical Law of the Wall method. For emergent obstructions the bottom boundary layer is likely to develop near the bed, while no shear layer exists at the top of obstructions (Nepf and Vivoni, 2000). The decision not to differentiate between emergent (100% of water depth occupied by obstructions) and nearlyemergent (occupying 90% to 100% of water depth) was made to avoid spurious (excessively
high) velocities above obstructions, which could lead to numerical instabilities.

Note that the roughness-length (z_0) is defined as the bed roughness length, not the total roughness induced by both the bed and the obstructions. For obstructions occupying less than 90% of the total water-depth (considered fully submerged), velocity profiles are computed using the two-layer method fully described by Abdelrhman (2003) and summarized in Appendix A. The coefficient of proportionality (c) found in equations (5) to (7) in Abdelrhman (2003) will be referred to as $c_{z0,abd}$ later in this paper. This coefficient requires calibration.

227

228

2.1.3. Geometrical considerations on obstruction flexibility

In the case of flexible obstructions (*e.g.*, vegetation...), the obstruction elements interact with the ambient current flow while bending. This interaction leads to changes in obstruction height (*h*), element density (*n*(*z*)), and horizontal cross-sectional area (*A*(*z*)), depending on their bending angle ($\theta(z)$). After computing the bent obstruction height and bending angle, *A*(*z*) is then calculated, taking into account the geometrical modification of the projected horizontal surface area (Figure 2).

For cylinder-like case, A(z) is considered as an ellipsis, depending on $d_0(z)$, the obstruction diameter and $d_e(z)$, the projected obstruction diameter in the flow direction. Meanwhile for parallelepiped-like case, A(z) is considered as a rectangle, depending on w(z), the obstruction width, and $t_e(z)$, the projected obstruction thickness in the flow direction.

Regarding the calculation of bent height (h) and bending angle ($\theta(z)$), the obstruction height 240 in the previous version of the module was empirically parameterized for seagrass Zostera 241 noltei from flume data through a polynomial formulation that depended on depth-averaged 242 velocity and the Leaf Area Index (LAI) of the seagrass canopy (Kombiadou et al., 2014). 243 With this polynomial regression, the computed obstruction height had to be bounded to 244 prevent unrealistic (negative) obstruction heights. Following Ganthy et al. (2015), the 245 previous polynomial formulation has been replaced by a more robust empirical formulation 246 that corresponds to an exponential decrease in canopy height whith increasing depth-averaged 247 free-stream velocity: 248

249
$$h = h_0 \cdot \exp(-c_h \cdot U_\infty) \tag{8}$$

Where h_0 is the unbent obstruction height, c_h is a calibration coefficient (3.6 for seagrass Z. *noltei*, Ganthy *et al.*, 2015) and U_{∞} is the depth-averaged free-stream velocity. Using this empirical parameterization, the bending angle ($\theta(z)$, in radians) is considered constant for all layers occupied by obstructions, such that $\theta(z)=arccos(h/h_0)$.

As a second option, a physically-based formulation has also been implemented. This 254 formulation, fully described in Abdelrhman (2007) and summarized in Appendix B, is based 255 on the balance between drag, lift, friction, weight, and buoyancy forces on a single 256 obstruction element, subdivided into a user-defined number of segments (n_{seg} , Figure 3). This 257 method, which neglects elasticity of obstruction elements, is particularly adapted to highly 258 flexible obstructions like seagrasses. An iterative procedure computes the bending angle for 259 each element until the computed height of the total obstruction converges with the flow 260 velocity. Indeed, the vertical position of the elements above the bottom will change according 261 to their bending angle, leading them to experience different local velocities. Using this 262

263 procedure, the angle of obstruction segment $(\theta(z))$ is directly computed by the algorithm and

the bent height (h) is then geometrically reconstructed.



265

Figure 3: Representation of flexible obstruction element with effects of local current velocity
on forces acting on each element segment (adapted from Abdelrhman, 2007).

268

269 **2.1.4.** Multiple obstructions

270 When multiple types of obstructions are present within a grid cell, the total friction forces 271 $(F_u(z) \text{ and } F_v(z))$ and the projected horizontal surface area (A(z)) are computed as the sum of 272 the friction forces and projected horizontal surface area contributed by each obstruction:

273
$$F_{u,tot}(z) = \sum_{i=1}^{i=n_{obst}} F_{u,i}(z)$$
 (9a)

274
$$F_{v,tot}(z) = \sum_{i=1}^{i=n_{obst}} F_{v,i}(z)$$
 (9b)

275
$$A_{tot}(z) = \sum_{i=1}^{i=n_{obst}} A_i(z)$$
 (10)

In previous equations, *i* is the index of each obstruction type and n_{obst} is the total number of obstructions. Furthermore, the typical size of eddies (L(z), eq. 7) is then computed as follows:

278
$$L_{tot}(z) = \frac{\sum_{i=1}^{i=n_{obst}} f_{xy}(z) \cdot c_{lz,i}}{\sum_{i=1}^{i=n_{obst}} f_{xy}(z)} \cdot \sqrt{\frac{1 - A_{tot}(z)}{\sum_{i=1}^{i=n_{obst}} n(z)}}$$
(11)

We decided to average the coefficient c_{lz} over all obstructions occupying the cell, weighted by the horizontal cell fraction occupied by each i^{th} obstruction. Although this approach may be questioned, the sensitivity analysis demonstrated that the model's sensitivity to this coefficient is weak (see section 4.1.).

Finally, for very shallow waters, when the hydrodynamics model operates in 2D mode, the required theoretical velocity profiles are computed similarly to the c_{lz} coefficient. They are averaged from the velocity profiles computed for each obstruction, weighted by the horizontal cell fraction occupied by each obstruction.

- 287
- 288 2.2. Test case configurations

To test the model's behavior, accuracy, and sensitivity in simulating flow-obstructioninteractions, four setups were defined based on previous experimental or modeling studies:

- ZNcase (*Zostera noltei* case): (sections 2.2.1. and 3.1.) This setup reproduces the
 flume experiments conducted by Ganthy *et al.* (2015) for the seagrass *Zostera noltei*. It was used for module calibration.
- ZMcase (*Zostera marina* case): (section 2.2.2 and 3.2.) This setup replicates the
 flume experiments by Lefebvre *et al.* (2010) for the seagrass *Zostera marina*. It
 was used to validate the module.
- MLLcase (Mussel Long-Line case): (section 2.2.3 and 4.2.1) This setup is inspired
 by the modeling experiments of Delaux *et al.* (2011) concerning suspended
 shellfish structures. It was used to test the downward functionality.

OYcase (Oyster-farm case): (section 2.2.4 and 4.2.2) This setup is inspired by the
 modelling experiments of Gaurier *et al.* (2011) for oyster farming structures. This
 test was used to evaluate both the O3D obstructions functionality and the
 representation of multiple obstructions within the same grid cell.

304

305

2.2.1. Zostera noltei case (ZNcase)

This case aims at reproducing flume experiments conducted by Ganthy *et al.* (2015). These experiments were carried out in a recirculating straight flume, examining five contrasting seagrass development stages and four flow regimes (V1 to V4, Table 1). This led to twenty velocity profiles measured 0.45 m downstream from the leading edge of the vegetation patch (profile P3 in Ganthy *et al.*, 2005).

All experimental flume conditions, including the dimension of the flume and vegetated bed, water depth, seagrass characteristics, and flow velocities (as listed in Table 2), were simulated using the two-dimensional vertical (2DV) approximation. The horizontal discretization (dx) was set to 0.05 m, while 40 equidistant sigma layers (dz = 0.005 m) were used for vertical discretization. For all five seagrass characteristics and the four flow regimes, the model was run in both 3D mode and 2D modes (with the theoretical reconstruction of velocity profiles) to test the two different formulations.

In all cases, the canopy height was computed using the Abdelrhman (2007) method, where seagrass leaves were discretized into 4 segments, and ρ_{obst} (leaf bulk density) was set to 625 kg.m⁻³ (Auby, *pers. com.*). As indicated by Abdelrhman (2007), the drag coefficient (C_D) used here varies linearly from 1.2 for $\theta = \theta$ (erected leaves) to 0 for $\theta = 90^{\circ}$ (completely horizontally bent leaves). For the runs performed using 3D formulations, the coefficient c_{lz} (eq. 7) was set to 0.2, roughly corresponding to the ratio between the thickness (t_e) and the width (w) of seagrass leaves. For the runs using 2D formulation, the coefficient $c_{z0,abd}$ (see section 2.2.2, Appendix A and Abdelrhman (2003) for further details) was calibrated and parameterized depending on leaf length (h_0), canopy height (h), total leaf density (n) and leaf width (w):

328
$$c_{z0,abd} = 2.6 \cdot \frac{h_0^2}{h^2 \cdot n_0 \cdot w}$$
 (12)

Since leaf density naturally varies with height, a height-dependant distribution of seagrass leaf
density, derived from numerous field observations (Ganthy, 2011) was used (Figure 4). A
summary of the experimental and model parameters is provided in Table 1.

For each test and flow regime, the model was run during 2 minutes (with a time-step of 0.025 seconds) to surpass the equilibrium state, which was typically reached after 1 minute on average. Results were outputted at 1 Hz over the last 30 seconds of the run. High frequency output is required to capture the turbulence and possible undulation of flexible obstructions and its interaction with hydrodynamics. Model results are then time-averaged to filter this high frequency variability. This post-processing strategy is common to all test cases.



	Model s	ettings			
Total length of	1	.5			
Length of veg	etation bed	(m)		0	.9
Position of upstream ea	lge of vegeta	ation bed (i	m)	0	.5
Horizontal disc.	retization (a	lx, m)		0.	05
Water c	lepth (m)			0	.2
Vertical discre	etization (dz	, <i>m</i>)		0.0	005
Z0	(m)			0.0	002
Obst	ructions mo	dule param	neters		
C_I	o (-)			1	.2
n _{se}	rg (-)			4	4
$ ho_{obst}$ (kg.m ⁻³)			6.	25
c_{li}	. (-)			0.2	
$C_{z0,A}$	1 <i>bd</i> (-)			Eq. 12	
	Tested ve	elocities			
Identifier VI			V2	V3	V4
$U_{\infty}(m.s^{-l})$	0.2	0.3	0.4		
Zos	stera noltei d	characteris	tics		
Identifier	<i>T1</i>	<i>T2</i>	T3	Τ4	Τ5
Total leaf density (n_0, m^{-2})	26650	34190	42540	80940	51080
Leaf length (h_0, m)	0.056	0.072	0.076	0.063	0.15
Leaf width (w, m)	0.00056	0.00058	0.00063	0.00082	0.00121
Loaf thickness (t. m)	0.0002	0.0002	0.0002		

351

352 *Table 1. Model parameters and Zostera noltei characteristics for the ZNcase.*

353

354 2.2.2. Zostera marina case (ZMcase)

This case aims to reproduce the straight flume experiments conducted by Lefebvre *et al.* (2010) in terms of velocity profiles for their Patch-1 to Patch-4. For each test, two free stream velocity values (V1 and V2, as listed in Table 2) were applied on *Zostera marina* patches across three patch lengths and two leaf densities (also listed in Table 2). Similarly to the ZNcase, all experimental flume conditions - including the dimensions of the flume and vegetated bed, water depth, seagrass characteristics and flow velocities - were replicated using a two-dimensional vertical (2DV) model configuration, which was run both using 3D and 2D
modes.

The horizontal discretization (dx) was set to 0.05 m while 40 equidistant sigma layers (dz =363 364 0.01 m) were defined for vertical discretization. Since this case was used to investigate the generic model feature for a different seagrass species, all model parameters used for the 365 ZNcase were applied, except seagrass bulk density (ρ_{obst}) which was set to 700 kg.m⁻³, 366 according to Abdelrhman (2007). Model results were compared with flume data for profiles 367 P2 to P5 (in Lefebvre et al., 2010), which are located 0.15 m from the leading edge of the 368 seagrass bed to 1.5 m downstream of the end of the vegetated bed, depending on its length 369 (see Table 2 or Figure 1b in Lefebvre et al., 2010). 370

In the absence of data on the vertical distribution of leaf density for *Zostera marina*, the distribution used for the ZNcase (Figure 4) was applied. Additionally, since Lefebvre *et al.* (2010) provided information on shoot density but not the mean number of leaves per shoot, which is required to compute the leaf density, the mean number of leaves per shoot (3.4) was derived from data collected in the Arcachon Bay (SW France) from 2007 to 2017 for the Europeean Water Directive Framework (Auby *et al.*, 2018).

Finally, for each test and flow regime, the model was run for 5 minutes (with a time-step of 0.025 seconds) to surpass the equilibrium state, which was typically reached after 3 minutes on average. Results were outputted at 1 Hz over the last 30 seconds of the run and then timeaveraged.

381

382

1	Model settings				
Total length of the dom			5		
Position of upstream edge of ve	egetation bed (m)		1.	25	
Horizontal discretization	on (dx, m)		0.	05	
Water depth (m)		0	.4	
Vertical discretization	(dz, m)		0.0	005	
z_0 (m)			0.0	002	
Obstructi	ons module paran	neters			
С _D (-)			1	.2	
n _{seg} (-)				4	
ρ_{obst} (kg.m ⁻³)			7	00	
c _{lz} (-)			0	.2	
C _{z0,Abd} (-)			eq.	. 12	
T	ested velocities				
Identifier	V	71	V2		
$U_{\infty}(m.s^{-1})$ 0.1			0.2		
Test de	ependant paramet	ers			
Identifier	Patch 1	Patch 2	Patch 3	Patch 4	
Length of vegetation bed (m)	1.5	1.0	1.0	0.5	
Total leaf density (n_0, m^{-2})	3300	3300	1980	3300	
Leaf length (h_0, m)		0	284		
Leaf width (w, m) Leaf thickness (t_0 , m)			004		
			0075		
Position of velocity measureme	nts (m from upstr	eam edge of v	egetated bed)		
P2	0.15	0.15	0.15	0.15	
P3	0.75	0.75	0.75*	0.75*	
P4	1.35	1.35*	1.35*	1.35*	
P5	2.0*	2.0*	2.0*	2.0*	

384 *Table 2. Model parameters and Zostera marina characteristics for the ZMcase.*

385

386 2.2.3. Mussel Long-Line case (MLLcase)

This case, inspired from numerical experiments of Delaux *et al.* (2011), aims to investigate the model's capability to simulate 3D velocities (free-stream velocity of 0.25 m.s⁻¹) in and around suspended shellfish structures (mussels long-line). A group of 5 long-lines (each 100 m in length, 1.5 m in width, and spaced 30 m apart), along with their associated droppers aligned with the flow, is simulated as rigid downward cylindrical obstructions. To minimize

edge effects, the domain length and width were set to 800 and 400 m, respectively. The water 392 depth was set to 5 m, and the droppers were considered to occupy half of this depth. The 393 model resolution was set to 0.5 m horizontally (a compromise between grid size and 394 computation time), and vertically it was discretized into 50 equidistant layers, resulting in a 395 vertical resolution of 0.1 m. For each long-line, the dropper density (n_0) was set to 0.7 m⁻² 396 (and maintained constant vertically), and their diameter (d_0) was set to 0.25 m, consistent with 397 the values used by Delaux et al. (2011) in their numerical experiments. The drag coefficient 398 (C_D) was set to 1.2, consistent with values used in previous cases, and c_{lz} coefficient was set 399 0.8, a value determined to be applicable for cylinders by Uittenbogaard (2003). All model 400 401 settings are summarized in Table 3. The model was firstly run using 3D formulations, and then using 2D formulations to investigate how the simplification (in term of depth-averaged 402 velocities) affects the simulated results. 403

Finally, the model was run for 120 minutes (with a time-step of 0.25 seconds) to surpass the equilibrium state, which was reached after 100 minutes. Results were outputted at 0.2 Hz over the last 15 minutes of the run and then time-averaged.

407

412 413

Model settings	
Total length of the domain (m)	800
Domain length upstream long-lines (m)	150
Total width of the domain (m)	450
Horizontal discretization (dx, dy, m)	0.5
Water depth (m)	5
Vertical discretization (dz, m)	0.1
$z_0 (m)$	0.0005
Free-stream velocity (U_{∞} , m.s ⁻¹)	0.25
Obstructions module parameters	
С _D (-)	1.2
n _{seg} (-)	not used
ρ_{obst} (kg.m ⁻³)	not used
c _{lz} (-)	0.8
$c_{z0,Abd}$ (-)	not used
Long-line characteristics	
Length of long-lines (m)	100
Width of long-lines (m)	0.25
Number of long-lines aligned to flow	5
Spacing between each long-line (m)	20
Droppers depth (h_0, m)	2.5
Droppers diameter (d_0, m)	0.15
Droppers density (n_0, m^{-2})	0.7

415 *Table 3. Model parameters and long-line characteristics for the MLLcase.*

416

417 **2.2.4.** Oyster-farm case (OYcase)

418 This case, inspired by the numerical experiments of Gaurier et al. (2011) aims to investigate the model's capability to simulate 3D velocities (free-stream velocity of 0.25 m.s⁻¹) in and 419 around an oyster farming structure (comprising oyster tables and associated oyster bags). An 420 421 oyster structure (100 m in length, 1.2 m in width) aligned with the flow is simulated using a combination of two types of obstructions: rigid upward cylindrical obstructions for the legs of 422 the oyster table and a rigid O3D cylindrical obstruction for the oysters within the bags. To 423 424 minimize edge effects, the domain length and width were set to 230 and 100 m, respectively. 425 The water depth was set to 4 m, and the total height of the structure (table legs + oyster bags)

was set to 0.82 m (0.72 m for table legs + 0.1 m for oyster bags). To optimize both grid 426 resolution and computation cost, the horizontal grid discretization was not uniform in 427 longitudinal (dx) and lateral (dy) directions. dx was set to 0.4 m, while dy was set to 0.15 m as 428 higher resolution was needed to better simulate the two rows of table legs. The vertical 429 dimension was discretized into 100 equidistant layers, resulting in a vertical resolution of 0.04 430 m. For both table legs and oyster bags, obstructions characteristics (i.e. legs diameter, height, 431 and density, oyster diameter, density, and height of a bag) were set to values representatives 432 to those found in realistic oyster farming structures. However, the bag itself, generally 433 corresponding to a plastic net with variable meshes sizes (from 2 to 14 mm), was neglected. 434 435 The model settings and parameters are summarized in Table 4. Similarly to the MLLcase, the model was first run using 3D formulations and then using 2D formulations to investigate how 436 the simplification (in term of depth-averaged velocities) affects the model's predictions. 437

Finally, the model was run for 60 minutes (with a time-step of 0.25 seconds) to surpass the
equilibrium state, which was reached after 40 minutes. Results were outputted at 0.2 Hz over
the last 15 minutes of the run and then time-averaged.

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Model settings	
Total length of the domain (m)	230
Domain length upstream oyster table (m)	100
Total width of the domain (m)	100
Horizontal longitudinal discretization (dx, m)	0.4
Horizontal lateral discretization (dy, m)	0.15
Water depth (m)	4
Vertical discretization (dz, m)	0,04
$z_0 (m)$	0.005
Free-stream velocity (m.s ⁻¹)	0.25
Obstructions module parameters for table legs	
С _D (-)	1.2
n _{seg} (-)	not used
ρ_{obst} (kg.m ⁻³)	not used
c _{lz} (-)	0.8
C _{z0,Abd} (-)	not used
Table legs characteristics	
Domain length upstream oyster table (m)	100
Length of table (m)	100
Width of legs, each side (m)	0.15
Legs height (h_0, m)	0.72
Legs diameter (d_0, m)	0.016
Legs density $(n_0, m-2)$	1
Obstructions module parameters for oyster bags	
С _D (-)	1.2
n _{seg} (-)	not used
ρ_{obst} (kg.m ⁻³)	not used
c _{lz} (-)	0.8
C _{z0,Abd} (-)	not used
Obstruction related parameters for oyster bags	
Length of table (m)	100
Width of oyster bags (m)	1.2
Occupied height above the bed (m)	0.72 to 0.82
Oyster diameter in bag (d_0, m)	0,04
Oyster density in bags $(n_0, m-2)$	120

450

451 **2.3.** Settings for sensitivity analysis

452 A sensitivity analysis was conducted for the ZNcase. This case allows for testing most of the

453 model parameters, including those dedicated to flexible obstruction type, and encompasses a

broader panel of flow conditions and obstructions characteristics. The model parameters and
methods used to describe obstructions were grouped into four main groups:

- 456 (1) main model parameters: bottom roughness length (z_0) , obstruction drag 457 coefficient (C_D) , number of segments (n_{seg}) and obstruction bulk density (ρ_{obst}) for 458 canopy height computation using the Abdelrhman's procedure, the coefficient c_{lz} 459 for typical size of eddies (Eq 7) and the coefficient $c_{z0,abd}$ used for theoretical 460 computation of velocity profiles using 2D formulations.
- 461 (2) obstruction's variables: the total leaf density (n_0) , leaf length (h_0) , leaf width 462 (w) and leaf thickness (t_0) .
- 463 (3) methods used for obstruction description: using cylinder-like obstructions 464 instead of parallelepiped-like (*Cyl*), without using vertical-varying leaf density 465 (*Cst* n(z)) and empirical parameterization of canopy height (*h* param) instead of 466 following the Abdelrhman's procedure.
- 467 (4) domain discretization: horizontal (dx) and vertical (dz) discretizations.

Each model parameter or method was tested separately. For the main model parameters (1) and obstruction variables (2), each parameter was tested by changing its value by \pm 50% while keeping the others constant (refer to Table 1). For domain discretization (4), dx and dzwere multiplied by two (corresponding to $dx_2 = 0.1$ m and $dz_2 = 0.01$ m, respectively) or four (corresponding to $dx_4 = 0.2$ m and $dz_4 = 0.02$ m, respectively).

473

474

2.4. Statistics for numerical solution evaluations

475 Firstly, for each velocity profile (for ZNcase and ZMcase), the root mean square error (*RMSE*,
476 in m.s⁻¹) and the normalized root mean square error (NRMSE, in %) were computed as
477 follow:

478
$$RMSE = \sqrt{\frac{\sum_{j=1}^{N} (U_{mod(j)} - U_{mes(j)})^2}{N}}$$
 (13)

479
$$NRMSE = 100 \cdot \sqrt{\frac{\sum_{j=1}^{N} \left(\frac{U_{\text{mod}(j)} - U_{mes(j)}}{U_{\infty}}\right)^{2}}{N}}$$
 (14)

where U_{mod} and U_{mes} are the simulated (nearest grid cell from observation position) and measured velocities respectively, U_{∞} is the free-stream velocity, *j* represents the considered vertical point of the profile and *N* is the number of data point in the considered profile. For all cases, simulated velocity profiles are linearly interpolated on data measured at different heights above the bed.

In order to perform model-to-model comparison, for each simulation (i.e. tested parameter or method), the normalized difference of the normalized root mean square error ($\Delta NRMSE_{norm}$, expressed as a percentage of the reference run) was computed as follow:

$$488 \qquad \Delta NRMSE_{norm} = 100 \cdot \frac{NRMSE_{Run} - NRMSE_{REF}}{NRMSE_{REF}}$$
(15)

where $NRMSE_{Run}$ is the global normalized root mean square error (accross all tests: T1-T5 and V1-V4) resulting from the tested parameter change, and $NRMSE_{REF}$ is the global normalized root mean square error for the reference simulation (for the ZNcase). Therefore, positive values indicate that the model accuracy is lower compared with the reference simulation.

3. Results

495 **3.1. ZNcase**

A comparison between simulated and measured velocity profiles is given in Figure 5, and a 496 summary of the statistical parameters used for model evaluation is presented in Table 5. 497 Velocities simulated using the 3D formulations align closely with the measurements (Figure 498 5), both in terms of velocity reduction within the canopy and the development of the shear 499 layer at the top of canopy. The normalized root mean square error (NRMSE) ranges from 500 7.1% (for T5V4) to 22.2% (for T3V1), with an overall value of 11.5% (Table 5). For all 501 502 seagrass characteristics (T1-T5), the correlation coefficients are at least 0.98. Compared with results from the previous version of the model presented in Kombiadou et al. (2014), the 503 current model more accurately predicts the velocity reduction in the upper region of the 504 canopy. Kombiadou et al. (2014) indicated an underestimation of the velocity reduction 505 leading to a milder velocity gradient at the top of the canopy, whereas the present model 506 507 results are significantly closer from measurements. This improvement is likely due to a more physical approach of canopy height computation (i.e. Abdelhrman's procedure instead of an 508 empirical polynomial formulation). 509

Considering velocities simulated using the 2D formulations (theoretical computation of 510 velocity profiles, see section 2.1.2), NRMSE values range from 7.6% (T1V2) to 31.1% 511 (T4V1), with an overall value of 18.1%. This is higher than values obtained using the 3D 512 formulations (Figure 5). In general, for denser seagrasses (mainly for T4 and T5 tests) the 513 velocity reduction within the canopy is underestimated, particularly at low velocities. 514 515 Simulated velocities above the canopy are lower than observed, showing a logarithmic shape from the top of the canopy to the water surface. Although this theoretical method partially 516 failed to reproduce the shear layer, the correlation coefficients are always above 0.95 (Table 517 5). Near-bed velocities, which are used to compute the bottom-shear stress in the sediment 518

- transport module, are generally well reproduced and are considered very satisfactory given the
- 520 high level of simplification of the dynamics.



Figure 5: Measured and simulated velocity profiles for the ZNcase for the five seagrass characteristics (T1 to T5) and the four velocity treatments (V1 to V4) at 0.45 m from the upstream edge of the vegetated patch. Measured velocities (grey circles) are presented with their standard-deviation, velocities simulated using 3D formulations are dark blue (with their associated predicted canopy height in dark green), while 2D formulations are in grey-blue (with their associated predicted canopy height in light green); the normalized root mean square errors (%) are also indicated for both the two formulations.

Tests		T1	<i>T2</i>	Т3	Τ4	<i>T5</i>	Total
D2	3D	0.98	0.98	0.98	0.99	0.99	0.98
K ²	2D	0.98	0.96	0.95	0.98	0.96	0.96
DMCE (m ml)	3D	0.024	0.022	0.029	0.019	0.021	0.023
$KMSE(m.s^{-1})$	2D	0.025	0.040	0.045	0.028	0.051	0.042
NDMCE (0/)	3D	10.9	11.9	15.8	8.5	9.1	11.5
NRMSE (%)	2D	10.4	17.9	20.9	12.6	24.7	18.1

Table 5: Synthesis of statistics values between measured simulated velocities obtained for the
ZNcase: correlation coefficient (R²), root mean square error (RMSE) and normalized root
mean square error (NRMSE).

532

533 **3.2. ZMcase**

In this case, four different eelgrass patches were simulated at two velocities using both 3D and 2D formulations. Simulated velocity profiles were compared with those measured by Lefebvre *et al.* (2010) in their flume at four locations. To illustrate model results, an example of comparison between simulated and measured velocity profiles is provided in Figure 6 for Patch-1 (high eelgrass density) for the two free stream velocity values (0.1 and 0.2 $m.s^{-1}$). The statistical results obtained for all the four eelgrass patches and the two free stream velocity values are summarised in Table 6.

Regarding results obtained using the 3D formulations, the NRMSE ranges from 11.4% (Patch-541 1, P2) to 19.0% (Patch-4, P2), with an overall value around 15.4% considering all profiles 542 located within the seagrass bed (Table 6). The correlation coefficient also exhibits high 543 values, generally over 0.9, for all profiles located within seagrass beds. However, the model 544 appears less accurate when considering profiles located downstream of the seagrass bed 545 (profile P5 for all tests, P4 for test Path-2, Patch-3 and Patch-4, and P3 for test Patch-4). Even 546 though the velocity inside the canopy is slightly underestimated for profiles P3 and P4, 547 respectively located at 0.75 and 1.35 m downstream from the edge of the seagrass bed, the 548 main vertical pattern of the flow along the vegetation patch is well simulated with 3D 549

formulations (Figure 6 a1-a3 and b1-b3). In contrast, for profile P5 (0.5 m downstream from the vegetation patch, Figure 6 a4 and b4) the near-bed velocity attenuation is underestimated by the model, possibly due to the length of seagrass leaves (0.28 m), where bending may extend the distance over which near-bed velocity is attenuated.

Regarding simulated velocity profiles using 2D formulations, similarly to the ZNcase, both 554 RMSE and R² values (Table 6) indicate that the model is less accurate than using 3D 555 formulations. The less accurate results are obtained for profiles located downstream the 556 seagrass patch. In this case no obstructions are present and velocity profile simply consists in 557 a classical Law of the Wall (Figure 6 a4 and b4). Furthermore, as vertical advection is not 558 taken into account in 2D, the horizontal flow pattern at the leading edge of the seagrass patch 559 cannot be reproduced by the model, leading to an underestimation of near-bed velocities for 560 the profile P2 (Figure 6 a1. and b1.). However, considering profiles P3 and P4, located further 561 inside the seagrass patch, results remain very satisfactory (overall NRMSE of 19.7 and 16.1% 562 and R² of 0.98 and 0.97 respectively, Table 6, Figure 6 a2, a3, b2 and b3). 563

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	Profiles		P2	<i>P3</i>	<i>P4</i>	P5
	D2	3D	0.97	0.99	0.97	0.96*
	<i>K*</i>	2D	0.85	0.96	0.97	0.66*
D	DMCE (3D	0.017	0.018	0.021	0.036*
Patcn-1	$RMSE(m.s^{-1})$	2D	0.053	0.029	0.025	0.075*
	NDMCE (0/)	3D	11.4	14.0	14.4	23.9*
	NRMSE (%)	2D	36.6	20.2	16.1	50.7*
	D?	3D	0.87	0.98	0.96*	0.92*
	<i>K*</i>	2D	0.84	0.97	0.70*	0.70*
D	DMCE (3D	0.027	0.021	0.030*	0.039*
² atch-2	$RMSE(m.s^{-1})$	2D	0.053	0.028	0.063*	0.063*
	NDMCE (0/)	3D	18.0	15.6	20.1*	26.1*
	NRMSE (%)	2D	38.5	19.5	42.1*	42.6*
	R^2	3D	0.94	0.97	0.98*	0.96*
		2D	0.87	0.97	0.83*	0.83*
	RMSE (m.s ⁻¹)	3D	0.018	0.026	0.019*	0.024*
Patch-3		2D	0.047	0.025	0.043*	0.042*
	NRMSE (%)	3D	12.0	18.6	12.4*	16.8
		2D	33.5	19.3	30.4*	30.4*
	<i>R</i> ²	3D	0.96	0.97*	0.95*	0.95*
		2D	0.82	0.73*	0.77*	0.83*
		3D	0.020	0.023*	0.026*	0.033*
^s atcn-4	$RMSE(m.s^{-1})$	2D	0.052	0.037*	0.049*	0.058*
		3D	19.0	15.8*	17.4*	17.1*
	NRMSE (%)	2D	32.9	36.1*	33.3*	27.3*
	D?	3D	0.93	0.97 (0.98)	0.96 (0.9 7)	0.94*
	R^2	2D	0.84	0.89 (0.96)	0.82 (0.9 7)	0.74*
Total		3D	0.022	0.023 (0.022)	0.025 (0.021)	0.033*
10141	$KMSE(m.S^{-1})$	2D	0.052	0.037 (0.02 7)	0.049 (0.025)	0.058*
	NDMSE (0/)	3D	15.5	<i>16.1 (16.2)</i>	<i>16.3 (14.4)</i>	21.2*
	NRMSE (%)	2D	35.5	24.8 (19. 7)	31.9 (16.1)	38.3*

⁵⁷⁷ Table 6: Synthesis of statistics values between measured simulated velocities obtained for the

579 *patchs, values in bold indicates that the corresponding velocity profile was located within the*

seagrass patch, while those marked by a * indicates that the corresponding velocity profile

- 581 was located downstream the end of the seagrass patch. Considering total values, the main
- value corresponds to the overall value and the value in bold between parenthesis corresponds

583 to the value computed only within the seagrass patch.

- 584
- 585

⁵⁷⁸ ZMcase: correlation coefficient (R^2) and root mean square error (RMSE). For the different

586 **4. Discussion**

587

4.1. Model reliability and sensitivity

Compared to results obtained by Kombiadou et al. (2014), this new version of the 588 OBSTRUCTIONS module slightly improves the simulation of vertical velocity profiles 589 accross all tests. However, for tests with highly developed seagrass beds (tests T4 and T5), 590 the results demonstrate a significantly better model capability to simulate velocities in the 591 upper part of the canopy, with a more developed shear layer. In the previous model 592 version (Kombiadou et al., 2014) the velocity was overestimated near the top of the 593 canopy for tests with high leaf densities. This improvement can be attributed to (1) the 594 better representation of seagrass leaf morphology (parallelepipeds instead of cylinders) 595 and (2) the better simulation of canopy height (physical computation based on balance of 596 forced instead of a polynomial empirical formulation), as discussed hereinafter. 597

Results from the sensitivity analysis (ZNcase) are summarized in Figure 7a and 7b for the 598 3D and 2D formulations, respectively. Overall, the model appears more sensitive to the 599 tested parameters and methods using 3D formulations than using 2D ones, exhibiting a 600 similar pattern but different intensities. Although 11 parameters, variables and methods 601 (excluding horizontal and vertical model resolution) are needed to setup the 602 OBSTRUCTIONS module, the latter is mostly affected by parameters/variables/methods 603 representing the obstructions. Specifically, the model appears very sensitive to methods: 604 using cylinders instead of parallelepipeds, using parameterized canopy height instead of 605 physical formulation based on forces, and the use of a constant vertical distribution of 606 obstructions instead of a measured one. Regarding obstructions characteristics and 607 parameters, the model prediction appears mainly affected by leaf length (h_0) and the 608 obstructions bulk density (ρ_{obst}), and to a lesser extent by the obstruction's drag coefficient 609

 (C_D) , which are key parameters for canopy height computation using balance of forces. 610 The model's behaviour is consistent with previous studies. Boothroyd et al. (2016) 611 demonstrated the importance of accurately representing complex plant morphology in 612 hydraulic models. Furthermore, in their multi-specific flume and modelling experiments, 613 Weitzman et al. (2015) highlighted the important role of the vertical distribution of 614 biomass on the shape of velocity profile. Finally, compared with leaf density (n_0) which 615 has a very limited impact on model prediction, the computed canopy height strongly 616 affects model reliability. This is in agreement with results from Dijkstra and 617 Uittenbogaard (2010), who demonstrated that obstructions flexibility has a greater impact 618 619 on flow reduction within the canopy than element density, both in their flume and 620 numerical experiments.

Consequently, when simulating flow through flexible obstructions (*i.e.* vegetation), the 621 use of Abdelhrman's (2007) method appears to be the best approach to properly compute 622 canopy height. However, this method is only applicable to very flexible obstructions, 623 since element elasticity is not taken into account. Introducing an elasticity term based on 624 the elasticity modulus and moment of inertia within the bending algorithm would improve 625 flow prediction for obstructions with characteristics ranging between fully rigid to fully 626 flexible. Thus, as stated by Dijkstra and Uittenbogaard (2010), the model would then 627 require additional inputs of obstructions properties (such as the elasticity modulus). 628 However, such properties are neither easily nor usually measured for seagrass species and 629 the rare studies dealing with measurements (or proxy) of those parameters highlighted 630 significant spatio-temporal variability (Soissons et al., 2017). 631

632 Apart from variables and methods describing obstructions, the model is only sensitive to 633 two parameters: the drag coefficient (C_D) which can be calibrated and the obstruction bulk 634 density (ρ_{obst}) which can be obtained from measurements. Otherwise these parameters can be picked up in the literature. Values for the drag coefficients usually range from 1 to 1.5.
In our model, the use of an intermediate value of 1.2 provides reliable results, and no
additional calibration was performed. An improvement of the model, when applied to
seagrass meadows, would be to parameterize time-varying drag coefficient and
obstruction bulk density in order to account for seasonal epiphytes growth on seagrass
leaves, as epiphytes are likely to modify both the leaf drag and bulk density.

541 Due to the quasi-absence of calibration requirements to accurately simulate the seagrass-542 flow interactions, it can be expected that applying the model to other types of obstructions 543 would provide satisfactory results with minimum calibration effort, as long as obstructions 544 are properly described.

645



Figure 7: Results of the model sensitivity analysis performed on Obstructions module parameters (from C_D to $c_{z0,abd}$), obstructions characteristics (from n_0 to t_0), method describing obstructions (Cyl and Cst (z)) and grid discretization (dx and dz), in terms of normalized changes in normalized root mean square error (Δ NRMSE_{norm}) for (a.) 3D formulations and (b.) 2D formulations. Notice that $c_{z0,abd}$ is not used by 3D formulations, while c_{lz} is not used by 2D formulations.

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Finally, in contrast to horizontal discretization (dx), for which the sensitivity is negligible, the model demonstrated a significant sensitivity to vertical discretization, particularly when the vertical resolution was reduceded by a factor of four (dz4), *i.e.* from 5 mm to 20 mm. The effect of vertical discretization is illustrated in Figure 8 for two contrasting seagrass characteristics (see Table 1), using both 3D and 2D formulations. The impact of verticalresolution on the velocity profile appears to be stronger for 3D formulations than for 2D ones.

The vertical discretization needs to be carrefully defined depending on processes to be 661 662 investigated (e.g. shear layer) and/or on the purpose of the model application (e.g. sediment dynamics). However, few comments can be made: (1) it is advisable to define discretization 663 to ensure at least two layers within the canopy, (2) the first bottom layer should be as thin as 664 possible to obtained more reliable bottom velocities for bottom shear stress computation in 665 dynamics modelling, (3) refining the vertical grid in the shear layer at the top of the canopy 666 allows for an increase in the model time-step due to lower velocity gradients between 667 successive layers. 668



671 *resolution using 3D (a. and b.) and 2D (c. and d.) formulations for two contrasted seagrass*

672 *development stage, test T1 (winter development, a. and c.) and T5 (summer development, b. and d.).*

4.2. Application to different obstruction types

Physical obstructions in coastal systems come in various forms, ranging from various types of vegetation (e.g., seagrass meadows, seaweeds or mangroves) to human-made structures like aquaculture facilities (oyster and mussels farms), pontoons and piles. The present model was specifically designed to be able to represent most of these obstructions. This generic feature is illustrated and discussed below using two distinct examples of anthropogenic obstructions found in coastal systems: mussel long lines and oyster farms.

680 4.2.1. Application to mussel long-lines farming (MLLcase)

Mussel Long-Lines (MLL) are transectstructures with regularly-spaced vertical dropper lines from the surface, where mussels attach and grow. In the Delaux experiment, their typical dimensions are 0.5 m width and 2.5 m vertical lines. This type of structures is used worldwide as mussel farming technique (Plew *et al.*, 2005; Plew, 2010; Delaux *et al.*, 2011; McKindsey *et al.*, 2011).

MLL have a significant impact on depth-averaged current velocity along the long-line, 686 regardless of whether a 3D or 2D formulation is investigated. Our simulations show a 687 688 reduction of the depth-averaged velocity by up to 0.4 U_{∞} close the MLL (Figure 9). A wake clearly develops along the line and downstream, showing a flow velocity reduction of 0.6 U_{∞} 689 30 m downstream from the line's edge, and still reaching 0.8 U_{∞} 50 m downstream from the 690 structure. Additionally, there is a flow velocity acceleration between the lines of 1.2 U_{∞} in 691 692 2D. These results, both in terms of velocity reduction and wake spatial distribution are in good agreement with results from Delaux et al. (2011). However, depth-averaged or 3D 693 approaches show some discrepancies, either on the absolute velocity reduction, the inter-line 694 acceleration or the wake spreading, which is wider in 2D than in 3D. Lateral velocity is 695 stronger in 2D than in 3D, especially at the upstream and downstream edges of the long-line. 696

This difference can be attributed to the vertical flow deflection which is not taken into account
in 2D. In the 2D model, most of the flow is laterally deflected on both sides of long-lines,
while in 3D, the flow is deflected both vertically (below the long-line) and laterally.





Figure 9: Depth-averaged normalized velocities simulated for the MLLcase using 3D (a. and
d.) and 2D (b. and e.), as well as the differences of normalized velocities between 3D and 2D
simulations (c. and f.), for the longitudinal velocity component (U, left panel, a., b. and c.)
and for the lateral velocity component (V, right panel, d., e. and f.). Long-line locations are
indicated by black dotted lines.

The full 3D model reveals detailed consequences of the presence of MLL on the 3D velocity 707 field (Figure 10). The flow velocity is abruptly reduced by at least 0.2 U_{∞} within the MLL 708 709 canopy, showing values that are close but still larger values than the velocity reduction observed in-situ by Plew et al. (2005). These discrepancies in magnitude could be attributed 710 711 to differences in geometry configuration between *in-situ* experiments and numerical experiments, as well as the challenges in recording reliable measurements within the farm 712 (Plew et al., 2005). In our numerical configuration, a significant drop in velocity is observed 713 below the canopy down to the bottom, where the flow velocity reduction ranges from 0.7 U_{∞} 714 to 0.9 U_{∞} . This low-flow area would be favorable for pseudofaeces sedimentation, as 715 observed in-situ (Mc Kinsdey et al., 2011). Due to the development of wake turbulent 716 structures along the long-line, the velocity tends to weakly accelerate again in the latter half of 717 the long-line and more significantly below the canopy. Velocity increases rapidly downward 718 without reaching the upstream velocity, even after 200 m, as also highlighted by Delaux et al. 719 720 (2011).

Although depth-averaged velocity discrepancies between 2D and 3D formulations remains relatively low, the geometry of long-lines lead to complex 3D flow structures. This has direct impacts on sediment dynamics and biodeposition patterns. It is also highly recommended to use 3D formulations in such applications.



Figure 10: Normalized velocities simulated for the MLLcase using 3D formulations: (a.)
upper view of surface velocities, (b.) upper view of bottom velocities, and (c.) side view of
velocities at Y=0 (i.e. within the central long-line). Long-line locations are indicated by black
dotted lines.

730 **4.2.2.** Application to oyster tables (OYcase)

731 Oysters are generally cultivated using long-lines, similar to those discussed above for 732 mussels, or they are elevated above the bed using oyster table arrays organized in blocks 733 covering several squared kilometres in intertidal areas (Kervella *et al.*, 2010). For instance, in the Mont Saint-Michel Bay in France, each table array is 0.7 m high above the bed, 1 m wide, and 100 m long. Oysters are enclosed in meshed bags (0.1 m high) attached horizontally to the table. As described in section 2.2.4, the generic obstruction model was configured to represent a 100 m long table array, similarly to the numerical setup of Gaurier *et al.*, (2011) and closely resembling the experimental setup of Kervella *et al.* (2010), except the table array length, which was necessarily shorter due to limitation imposed by the experimental facility dimension.

The obstruction element parameters (table and oyster bags dimensions) were set according to 741 nature, without further specific calibration. Model results show very good qualitative and 742 quantitative agreement with both the laboratory experiment results from Kervella et al. (2010) 743 and the numerical experiment from Gaurier et al. (2011, Figure 11). Velocity within oyster 744 bags is strongly reduced compared to the free-stream velocity U_{∞} . This reduction tends to 745 746 increase from 0.4 U_{∞} at the upstream edge to reach 0.15 U_{∞} roughly 25 m inside the oyster bags (Figure 11a). Below table, a boundary layer can develop caused by oyster bag drag and 747 merges with the bottom boundary layer 20 m downstream the table leading edge. Over this 20 748 m distance, flow velocity below tables rapidly drops to reach 0.2 U_{∞} and stabilizes. Similarly, 749 a boundary layer develops above the table, leading to a decrease in velocity to 0.5 U_{∞} winthin 750 751 1 m around the structure at the trailing edge (Figure 11e). This decrease in velocities around and below oyster table, together with high settling velocity of pseudofaeces, has evident 752 implication on siltation and sediment accumulation nearby these structures, as observed in 753 Marennes-Oléron Bay (Sornin, 1981). 754

2D simulations were also conducted, and the main results and conclusions (Appendix C) are similar to the MLLcase: model results in 2D are broadly similar to 3D, while the wake around the table is more developed and flow velocity reduction is slightly stronger.



Figure 11: Normalized velocities simulated for the OYcase using 3D formulations: (a.) upper view of velocities at 0.75 m above the bed (i.e. at half height of oyster bags), (b.) upper view of bottom velocities, (c.) side view of velocities at Y=0 m (i.e. at half width of the oyster table), and cross view of velocities at X=2 m (d., 2 m downstream the leading edge of the

764 oyster table) and at X = 98 m (e., 2 m upstream the end of the oyster table). Table locations
765 (bags and tables legs) are indicated by black dotted lines.

766

767 4.3. Toward regional scale modelling

As demonstrated above, the OBSTRUCTIONS module is applicable and reliable for 768 simulating various type of flow-obstruction interactions at the obstruction scale, under steady 769 or unsteady forcing conditions. The main ambition is to upscale this module to regional scale 770 (bays, lagoons, estuaries) over annual to decadal scales, in order to evaluate the impact of 771 anthropogenic and natural obstructions on the hydrodynamics, the sediment dynamics, and 772 773 ultimately, ecosystem dynamics in the context of global change. While the OBSTRUCTIONS module is technically applicable to a regional scale, upscaling to larger grid cell (O(100 m)) 774 and longer running time (O(1 y)-O(10 y)) remains challenging and require adaptations to 775 776 overcome current limitations due to vertical and horizontal model description. The discussion will be illustrated using the Zostera noltei meadows-hydrodynamics interactions in the 777 Arcachon lagoon. However the discussion can be generalized to any other type of 778 obstructions. 779

780

781 **4.3.1.** Upscaling challenge #1: the vertical description

782 The primary criterion for an operational regional model is to utilize the largest time step and 783 the coarsest affordable vertical description to save computation time without a significant 784 compromise on process representation and result quality.

785 The sensitivity analysis of the 3D formulation presented above recommends carefully 786 defining the vertical sigma layer distribution. This includes using at least 2 vertical layers to

describe obstructions, establishing a thin first sigma layer to efficiently calculate bottom 787 velocity, and optionally refining the vertical mesh around the shear layer near the 788 obstructions. As Zostera noltei meadows mainly grow in intertidal areas, where water depth 789 can reach 2 to 3 m at highest spring tides, optimizing the sigma layer distribution accordingly 790 may not be straightforward. The stability of the OBSTRUCTIONS module in full 3D requires 791 reducing computation time steps (by 2 to 5) compared to the model without obstructions, 792 likely due to stronger horizontal and vertical velocity gradients near the obstruction elements. 793 The need for shorter time steps makes long-term simulations less affordable. 794

Using mixed 2D/3D calculations can be a solution to expedite model computation but with 795 significant consequences on simulated processes. As previously mentioned, Zostera noltei is 796 797 found in intertidal areas. Therefore, increasing the 2D/3D water depth threshold to the deepest vegetation depth at high spring tide (e.g., 2-3m in the Arcachon lagoon) implies solving all 798 dynamics (hydrodynamics, obstruction, and other processes) in 2D, while deeper areas like 799 tidal channels and offshore areas will still be computed in 3D. While this option can 800 significantly reduce computation time, it treats all intertidal dynamics as vertically mixed, 801 802 which can be a strong (and inaccurate) assumption. This also requires further adaptation of 803 sediment/obstruction interactions to account for sediment trapping, for instance.

Specifically for upward obstructions such as vegetation, a more radical but pragmatic solution is to replace the OBSTRCUTIONS module with an empirical "obstruction-representative" macro-roughness length in the 3D hydrodynamic model. This option, used in previous studies (Chen et al., 2007; Vargas-Luna et al., 2015), has no additional impact on the computation time step and is less complex to implement. However, it comes with several drawbacks. The vertical discretization must align with the roughness length, meaning the roughness length cannot exceed the first layer's thickness. While this method can reasonably and efficiently 811 simulate average dynamics, the complex vertical velocity profile, and typically the bottom 812 velocity, may not be accurately computed. This becomes problematic when coupled with 813 sediment dynamics or biogeochemical models.

The choice between full 3D, 3D/2D, or roughness length models is ultimately user-dependent, based on the main research question and its minimum requirements for key processes to reproduce.

817

4.3.2. Upscaling challenge #2: the horizontal description

Regional models typically encompass areas ranging from $O(100 \text{ km}^2)$ to $O(1000 \text{ km}^2)$ or larger, with typical mesh size is O(100 m). At this spatial scale, the sub-grid meadows' patchiness can be significant. The primary challenge lies in upscaling the effects of these patches to a larger scale. A straightforward initial solution is to multiply the meadow coverage fraction by the obstruction density. However, this assumes that patches interact independently with the flow, which is not the case when obstruction patches are relatively close to each other (El Allaoui *et al.*, 2016) or when they are sparse (Coulthard *et al.*, 2005).

A second option builds upon the previous solution by incorporating a non-linear transfer function. This would necessitate future or further investigations into the influence of patchiness at the grid cell scale, testing a wide variety of obstruction configurations and densities within a grid cell to establish a reliable transfer function. However, this function would be dependent on the type of obstruction.

A final method to consider involves downscaling the hydrodynamics model to match the resolution of the patchiness, based on the approach developed by Volp et al. (2013). This approach accounted for high-resolution bathymetry and bottom roughness at the subgrid scale. While this option would be tailored to our problem's scale, it would likely be moretime-consuming.

836

837 **5.** Conclusions

We have developed the generic OBSTRUCTIONS module designed to represent both upward 838 and downward, rigid or flexible vegetation, and anthropogenic structures such as shellfish 839 farms (long-line farms, oyster table blocks), windfarm piles, or pontoons. Obstructions can 840 take the form of cylinders or parallelepipeds and are described by a limited number of 841 parameters. This module can be integrated with any hydrodynamic coastal model, such as 842 MARS3D in the present study. The obstruction-flow interactions are based on a k-ɛ turbulent 843 closure model (Temmerman et al., 2005) and can be used in either 3D or 2D mode. Bending 844 is accounted for, and algorithms are available either based on empirical relationships derived 845 from experimental studies (Ganthy et al., 2015) or from an iterative multi-element physical 846 model (Abderhrman, 2007). This module allows for the incorporation of multiple obstructions 847 within a single mesh, which is valuable when modeling ecosystem dynamics. 848

The generic and reliable nature of this module was demonstrated by implementing four different obstruction types: short and long seagrass meadows, as well as two anthropogenic structures—mussel long-lines and oyster tables. Simulated velocities were compared with reference observations or numerical studies and yielded excellent results with minimal calibration efforts (i.e., only specifying obstruction features and using an average drag coefficient). Specific calibration for the drag coefficient can be considered to further improve model accuracy if necessary.

This module was developed with the aim of simulating integrated coastal ecosystem 856 dynamics, *i.e.*, coupling physical, biogeochemical, and ecological models. Upscaling 857 obstruction interactions from individual systems to regional scales requires careful attention to 858 limit computational costs. Further investigations are needed to account for the spatially 859 heterogeneous extension of obstructions, particularly large patch/block interactions within an 860 O(100x100) m² model cell, corresponding to the typical cell size used in coastal models. This 861 coupled model will then provide the opportunity to explore the future trajectories of 862 vulnerable coastal systems in response to global change, or to devise restoration measures for 863 engineered coastal systems. 864

866 Nomenclature

867	3D/2D	Three/Two dimensional
868	DO	Downward obstruction
869	FCT	Flux Corrected Transport
870	MARS	Model for Application at Regional Scale
871	O3D	Upward obstruction in mid-water
872	UP	Upward obstruction
873		
874	A	Horizontal cross-sectional obstruction area per unit area (-)
875	A_{tot}	Total (over all obstructions variables) horizontal cross-sectional obstruction area per unit area
876	(-)	
877	b	Frontal area of individual obstruction element (m ²)
878	$C_{2\varepsilon}, C_{\mu}$	Turbulence coefficients (-)
879	c_h	Coefficient for exponential decay of obstruction height (-)
880	C_{lz}	Coefficient for typical size of eddies (-)
881	$C, C_{z0,abd}$	Coefficient for obstructions roughness height
882	C_D	Drag coefficient for obstructions (-)
883	d_0	Diameter of obstruction element, in case of cylinder-like (m)
884	d_h	Displacement height of velocity profile (m)
885	dx, dy	Horizontal grid discretization in x and y direction (m)
886	dz	Vertical grid discretization (m)
887	f_{xy}	Horizontal fraction of grid cell occupied by obstructions (-)
888	f_z	Vertical fraction of layer occupied by obstructions (-)
889	F_{μ}, F_{ν}	Friction force acting on flow in x and y directions (N.m ⁻³)
890	$F_{u,tot}, F_{v,tot}$	Total (over all obstructions variables) friction force acting on flow in x and y directions (N.m ⁻³)
891	Fx, Fz	Horizontal (along the flow) and vertical forces acting on an obstruction element (N.m ⁻³)
892	Fxz	Force acting alongside of an obstruction element (N.m ⁻³)
893	g	Gravitational acceleration $(m.s^{-2})$
894	h	Effective bent height of obstruction (m)
895	h_0	Height of unbent obstruction (m)
896	Ĥ	Total water depth
897	i	Indice of obstruction variable
898	i	Indice of measured location in velocity profiles
899	k	Turbulent kinetic energy $(m^2.s^{-2})$
900	L	Typical size of eddies (m)
901	L _{tot}	Total (over all obstructions variables) typical size of eddies (m)
902	LAI	Leaf Area Index (-)
903	Ν	Sample size of model or observation values (-)
904	п	Number of obstruction elements per unit area (m^{-2})
905	n_0	Total number of obstruction elements per unit area (m^{-2})
906	nsea	Number of segment for a single obstruction element (-)
907	n _{obst}	Number of obstruction variables
908	NRMSE	Normalized root mean square error (%)
909	RMSE	Root mean square error $(m.s^{-1})$
910	S	Indices of the segment of obstruction element
911	t	Time
912	t_0	Thickness of an obstruction element in case of parallelepiped-like (m)
913	t _e	Effective projected thickness (along the flow) of an obstruction element in case of
914	parallelepiped-lil	ke (m)
915	Т	Work spent by the fluid $(m^2.s^{-3})$
916	Umes	Measured flow velocity (m.s ⁻¹)

917	U_{mod}	Simulated flow velocity (m.s ⁻¹)
918	U_{∞}	Depth averaged free stream velocity (m.s ⁻¹)
919	<i>u</i> , <i>v</i>	Flow velocity in x and y directions $(m.s^{-1})$
920	W	Width (across the flow) of an obstruction element in case of parallelepiped-like (m)
921	<i>x</i> , <i>y</i>	Horizontal position/coordinates (m)
922	Z	Height above the bed (m)
923	z_0	Bottom roughness length without obstructions (m)
924		
925	α	Attenuation coefficient for flow within the obstruction canopy
926	3	Turbulent energy dissipation (m ² .s ⁻³)
927	$\Delta RMSD$	Normalized difference of root-mean-square deviation (%)
928	θ	Deflection angle of obstruction from the vertical direction (radian)
929	κ	van Karman's constant
930	v	Molecular viscosity (m ² .s ⁻¹)
931	v_t	Eddy viscosity (m ² .s ⁻¹)
932	ρ	Water density (kg.m ⁻³)
933	$ ho_{obst}$	Obstruction density (kg.m ⁻³)
934	$\sigma_k, \sigma_{\varepsilon}$	Turbulent Prandtl-Schmidt coefficients for self-mixing turbulence (-)
935	$ au_arepsilon$	Energy dissipation timescale (s)

937 **CRediT statement**

Florian Ganthy: Conceptualization, Methodology, Software, Data Curation, Writing –
Original Draft. Romaric Verney: Conceptualization, Methodology, Writing – Review &
Editing. Franck Dumas: Methodology, Software, Writing – Review & Editing.

941

942 Acknowledgments

The authors acknowledge the Pôle de Calcul et de Données Marine (PCDM) for providing DATARMOR facilities (storage, data access and computational ressources). We would also like to thank Solène Le Gac for her careful proof reading as well as the reviewers for their constructive comments which helped us to improve the structure, style, and understanding of our manuscript.

948

949 Fundings

950 This research was supported by IFREMER (the French Institute for Research and Sea951 Exploitation) and by the French Research National Agency (ANR) in the frame of the

952 Investments for the Future Program, within the Cluster of Excellence COTE (ANR-10-

953 LABX), as part of ZODARSED project.

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1114 Appendix A: Description of the Abdelrhman's (2003) method for theoretical velocity

1115 profile computation

1116 The flow velocity above the obstruction canopy at a distance z above the bed $(u_{above}(z))$ is 1117 expressed as:

1118
$$u_{above}(z) = \frac{u_{can}^*}{\kappa} \cdot \log\left(\frac{z - d_h + z_0}{Z_0}\right)$$
(A1)

1119 where u_{can}^* is the friction velocity for the canopy, κ is von Karman's constant (0.4), d_h is the 1120 displacement height of velocity profile above the canopy and Z_0 is the roughness height for 1121 obstruction canopy.

1122 The displacement height of velocity profile (d_h) and the roughness height for obstruction 1123 canopy (Z_0) are then expressed as:

1124
$$d_h = \frac{c_{z0,abd} \cdot h^2 \cdot w}{(a + c_{z0,abd} \cdot h \cdot w)}$$
(A2)

1125
$$Z_0 = \frac{0.5 \cdot w \cdot h^2 \cdot a}{(a + c_{z0,abd} \cdot h \cdot w)^2}$$
(A3)

1126 Where $c_{z0,abd}$ is a calibration coefficient and *a* is the horizontal area per obstruction element (

1127
$$a = \pi \cdot \frac{w}{2} \cdot \frac{t_e}{2} \cdot \frac{h}{h_0}$$
 for cylinder-like obstructions and $a = w \cdot t_e \cdot \frac{h}{h_0}$ for parallelepiped-like

1128 obstructions).

1129 The flow velocity within the obstruction canopy at a distance z above the bed $(u_{can}(z))$ is 1130 expressed as:

1131
$$u_{can}(z) = u_h \cdot \exp\left[\alpha \cdot \left(\frac{z}{h} - 1\right)\right]$$
 (A4)

1132 Where u_h is the flow velocity at the top of the canopy (z=h) and α is an attenuation coefficient 1133 given by:

1134
$$\alpha = h \cdot \left(\frac{C_D \cdot b}{2 \cdot \lambda^2}\right)^{\frac{1}{3}}$$
(A5)

1135 Where *b* is the frontal area of the individual obstruction element $(b = w \cdot h)$ and λ is the 1136 mixing length of the turbulent flow within the obstruction, assumed to be equal to d_h .

1137 Finally, u_{can}^* is calculated from the conservation of fluid mass between the water column 1138 without and with obstruction:

1139
$$\int_{0}^{H} \frac{u^{*}}{\kappa} \cdot \log\left(\frac{z+z_{0}}{z_{0}}\right) \cdot dz = \int_{0}^{h} u_{h} \cdot \exp\left[\alpha \cdot \left(\frac{z}{h}\right) - 1\right] \cdot dz + \int_{h}^{H} \frac{u_{can}^{*}}{\kappa} \cdot \log\left(\frac{z-d_{h}+z_{0}}{Z_{0}}\right) \cdot dz$$
(A6)

1140 So that:

1141
$$u_{can}^{*} = \frac{u^{*} \left[(H + z_{0}) \cdot \log \left(\frac{H + z_{0}}{z_{0}} \right) - H \right]}{\frac{h}{\alpha} \cdot \log \left(\frac{h - d_{h} + z_{0}}{Z_{0}} \right) \left(1 - e^{\alpha} \right) + \left(H - d_{h} + z_{0} \right) \cdot \log \left(\frac{H - d_{h} + z_{0}}{Z_{0}} \right) - \left(h - d_{h} + z_{0} \right) \cdot \log \left(\frac{h - d_{h} + z_{0}}{Z_{0}} \right) + \left(H - h \right)}$$
1142 (A7)

1143 Where *H* is the total water depth, and u^* is friction velocity for bed without obstructions.

1144

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1146 Appendix B: Description of the Abdelrhman's (2007) method for the computation of

1147 bent obstruction height

1148 The algorithm to compute bending angle for flexible obstructions is based on the balance 1149 between drag, lift, friction, weight, and buoyancy forces on a single obstruction element, 1150 subdivided into a user-defined number of segment (n_{seg}). Each segment of obstruction element 1151 also has a length (l_{seg}):

1152
$$l_{seg} = h_0 / n_{seg}$$
 (B1)

1153 The net vertical force is computed as the difference between weight and buoyancy:

1154
$$F_{vertical} = (\rho - \rho_{obst}) \cdot g \cdot w \cdot t_0 \cdot l_{seg}$$
(B2)

1155 where ρ is water density, ρ_{obst} is obstruction's bulk density, and g is the gravitational 1156 acceleration.

1157 When flow passes around obstruction element it generates form drag in the direction of1158 motion. The form drag can be expressed by:

1159
$$F_{drag} = 0.5 \cdot \rho \cdot C_D \cdot uv(z)^2 \cdot w \cdot l_{seg} \cdot \cos(\theta)$$
(B4)

1160 where uv(z) is the free stream velocity at height z above the bed, and θ is the deflection angle 1161 of a segment from the horizontal. The angle θ remains unknown in this part of the analysis. 1162 Roughness on obstruction element's surface generates the skin friction drag force, which 1163 aligns in the direction of the element and can be expressed as:

1164
$$F_{skin} = 0.5 \cdot \rho \cdot C_f \cdot (uv(z) \cdot \sin(\theta))^2 \cdot 2 \cdot w \cdot l_{seg}$$
(B5)

1165 where C_f is the skin friction coefficient assumed to the same for the two sides of an 1166 obstruction element. The skin friction is computed from the Reynolds number (*R*):

1167
$$C_{lift} = 0.074 \cdot R^{-1/5}$$

1168
$$R = \frac{uv(z) \cdot w \cdot \rho}{\mu}$$

1169 where μ is the dynamic viscosity.

1170 Finally, a lift force (vertical) is produced when the flow passes around element:

1171
$$F_{lift} = 0.5 \cdot \rho \cdot C_{lift} \cdot uv(z)^2 \cdot w \cdot l_{seg} \cdot \sin(\theta)$$
(B8)

1172 where C_{lift} is the lift coefficient (0.1). For θ ranging between 0 and $\pi/2$ the lift force will be 1173 downward, on the contrary, for angle ranging between $\pi/2$ and π the lift force will be upward.

1174

1175 Then, the algorithm solves the balance of forces for each segment using a downward 1176 procedure. When the bending angle of a segment changes, its vertical location above the 1177 bottom will change accordingly, hence it will experience different local velocities. Both the 1178 bending angle of the segment (θ_s) and the local velocity uv_s at the s^{th} element are taken into 1179 account.

1180 At the highest segment (s=1), the segment is deflected by the resultant of drag, lift, skin, 1181 weight and buoyancy forces, which produces tensile force in the segment. All forces are then 1182 decomposed into horizontal (x) and vertical (z) components to calculate the magnitude and 1183 direction of the resultant force. All moments are summed at the lower segment joint and 1184 equated to zero, allowing to calculate the bending angle of the segment:

$$0.5 \cdot C_D \cdot \rho \cdot uv_{s=1}^2 \cdot w \cdot l_{seg} \cdot \frac{l_{seg}}{2} \cdot \cos(\theta_{s=1})^2 + 0.5 \cdot C_{lift} \cdot \rho \cdot uv_{s=1}^2 \cdot w \cdot l_{seg} \cdot \frac{l_{seg}}{2} \cdot \sin(\theta_{s=1})^2 - (\rho - \rho_{obst}) \cdot g \cdot w \cdot t_e \cdot l_{seg} \cdot \frac{l_{seg}}{2} \cdot \sin(\theta_{s=1}) = 0$$
(B9)

(B6)

(B7)

In eq. (B8), the only unknown is $\theta_{s=1}$ which is obtained iteratively. As the top-most segment only has a lower joint, so reaction $Fxz_{s=1}$ should fall in the direction of that segment. This implies for the segment to be stable that the summation of all components of force in the *x* and *z* directions should be equal to zero:

1190
$$Fx_{s=1} + 0.5 \cdot C_D \cdot \rho \cdot uv_{s=1}^2 \cdot w \cdot l_{seg} \cdot \cos(\theta_{s=1}) + 0.5 \cdot C_f \cdot \rho \cdot uv_{s=1}^2 \cdot w \cdot l_{seg} \cdot \sin(\theta_{s=1})^3 = 0$$
(B10)

1191
$$Fz_{s=1} - 0.5 \cdot C_{lift} \cdot \rho \cdot uv_{s=1}^{2} \cdot w \cdot l_{seg} \cdot \sin(\theta_{s=1}) + (\rho - \rho_{obst}) \cdot w \cdot l_{seg} \cdot t_{e} + 0.5 \cdot C_{f} \cdot \rho \cdot uv_{s=1}^{2} \cdot w \cdot l_{seg} \cdot \sin(\theta_{s=1})^{2} \cdot \cos(\theta_{s=1}) = 0$$
(B11)

1192 where $Fx_{s=1}$ and $Fz_{s=1}$ are the horizontal and vertical components, respectively, of the reaction 1193 at the lower joint. The reaction $Fxz_{s=1}$ alongside of a segment ($Fxz_{s=1} = (Fx_{s=1}^2 + Fz_{s=1}^2)^{\frac{1}{2}}$) is 1194 obtained by substituting the value of $\theta_{s=1}$ in (B9) and (B10). A force of equal magnitude but 1195 opposite direction to this reaction then transfers the effects of all forces on the top-most 1196 segment (*s*=1) to the next one (*s*=2). The same procedure is then applied to all segments. For 1197 an intermediate segment *s*, equations (B8), (B9) and (B10) become:

$$0.5 \cdot C_{D} \cdot \rho \cdot uv_{s}^{2} \cdot w \cdot l_{seg} \cdot \frac{l_{seg}}{2} \cdot \cos(\theta_{s})^{2} + 0.5 \cdot C_{lift} \cdot \rho \cdot uv_{s}^{2} \cdot w \cdot l_{seg} \cdot \frac{l_{seg}}{2} \cdot \sin(\theta_{s})^{2} - (\rho - \rho_{obst}) \cdot g \cdot w \cdot t_{e} \cdot l_{seg} \cdot \frac{l_{seg}}{2} \cdot \sin(\theta_{s}) + Fx_{s-1} \cdot l_{seg} \cdot \cos(\theta_{s}) - Fz_{s-1} \cdot l_{seg} \cdot \sin(\theta_{s}) = 0$$
(B12)

1199
$$Fx_s + 0.5 \cdot C_D \cdot \rho \cdot uv_s^2 \cdot w \cdot l_{seg} \cdot \cos(\theta_s) + 0.5 \cdot C_f \cdot \rho \cdot uv_s^2 \cdot w \cdot l_{seg} \cdot \sin(\theta_s)^3 + Fx_{s-1} = 0$$
(B13)

1200
$$\frac{Fz_s - 0.5 \cdot C_{lift} \cdot \rho \cdot uv_s^2 \cdot w \cdot l_{seg} \cdot \sin(\theta_s) + (\rho - \rho_{obst}) \cdot w \cdot l_{seg} \cdot t_e}{+ 0.5 \cdot C_f \cdot \rho \cdot uv_s^2 \cdot w \cdot l_{seg} \cdot \sin(\theta_s)^2 \cdot \cos(\theta_s) + Fz_{s-1} = 0}$$
(B14)

where Fx_s and Fz_s are the horizontal and vertical components of the reaction at the lower joint respectively. Equation (B11) is first solved iteratively to obtain the value of θ_s which is then substituted in (B12) and (B13) to obtain the reaction force that will act to the next segment.



1206 Appendix C: Velocity comparison between 3D and 2D formulations for the OYcase

